

# **Impact of Single-Neuron Dynamics on Transfer of Correlations from Common Input**

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*Evan L. Thilo, Wake Forest University*

*Eric Shea-Brown, University of Washington*

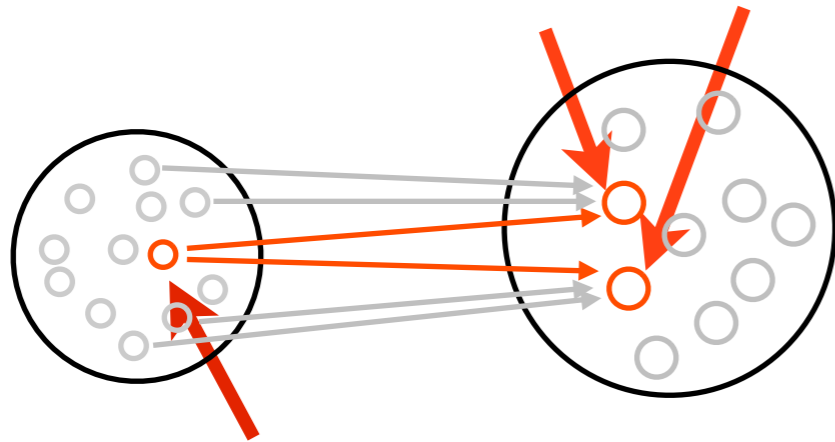
*Alessio Franci, University of Liege*

**CNS Workshop on *Stochastic Neural Dynamics***

**July 22, 2015**

# Common input from population coding creates correlations

These cells receive common synaptic input

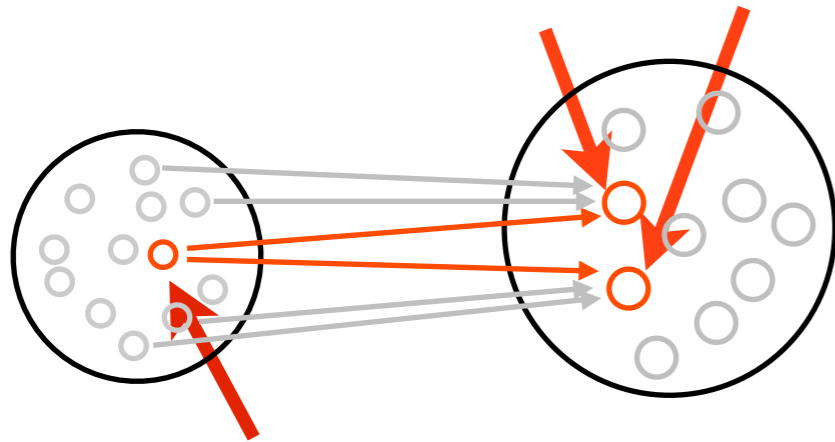


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Information flow

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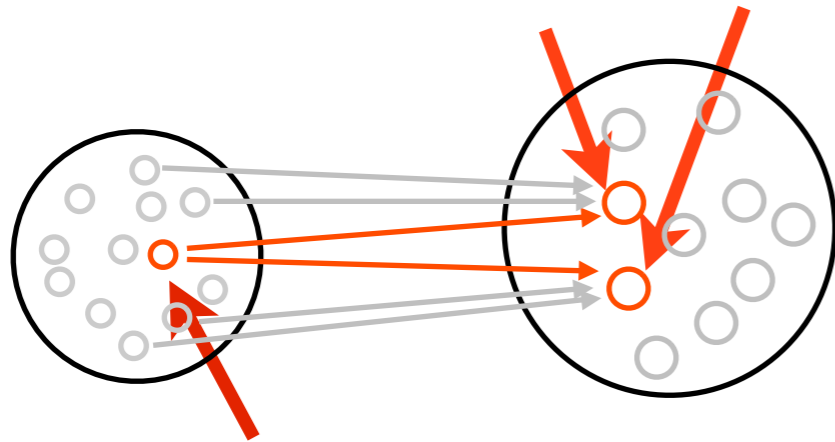
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$$\Rightarrow P(x_1, x_2 | s) \neq P(x_1 | s)P(x_2 | s)$$

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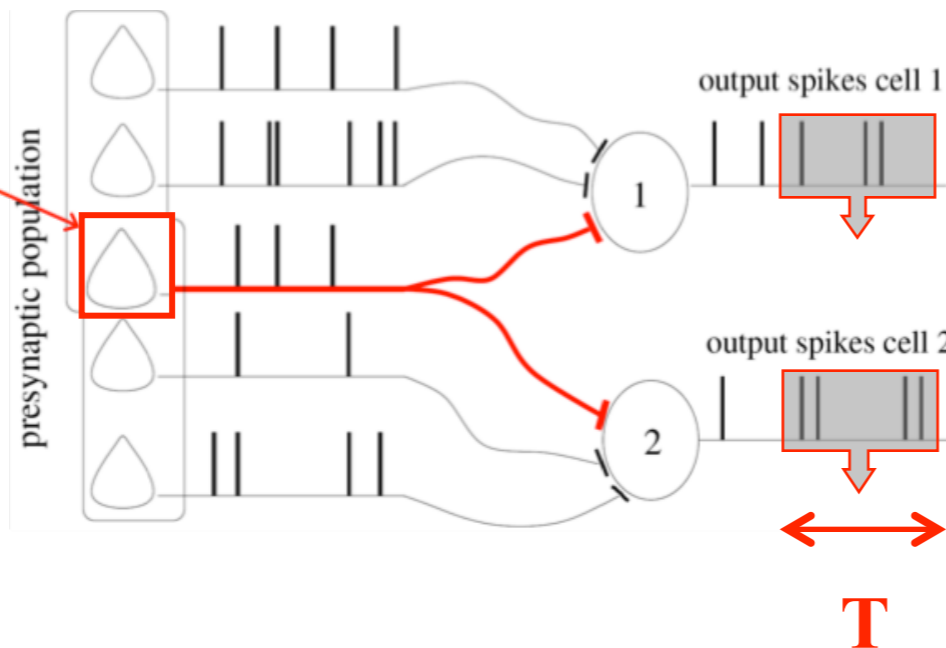


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shared fraction  $\sim c$

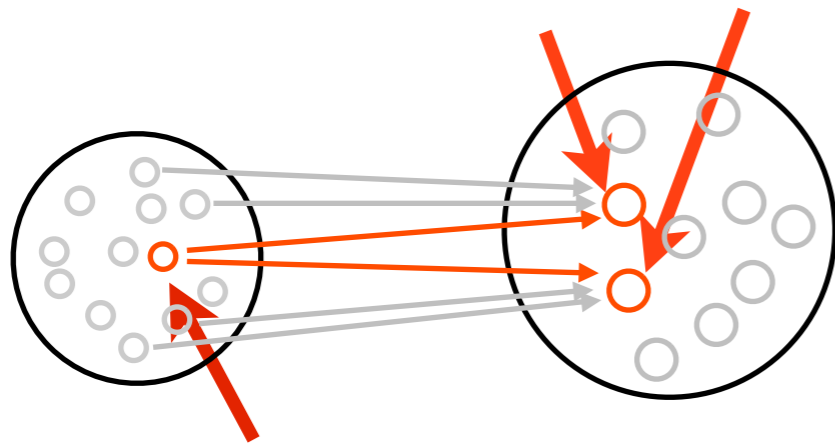


$$n_1 = 3$$

$$n_2 = 4$$

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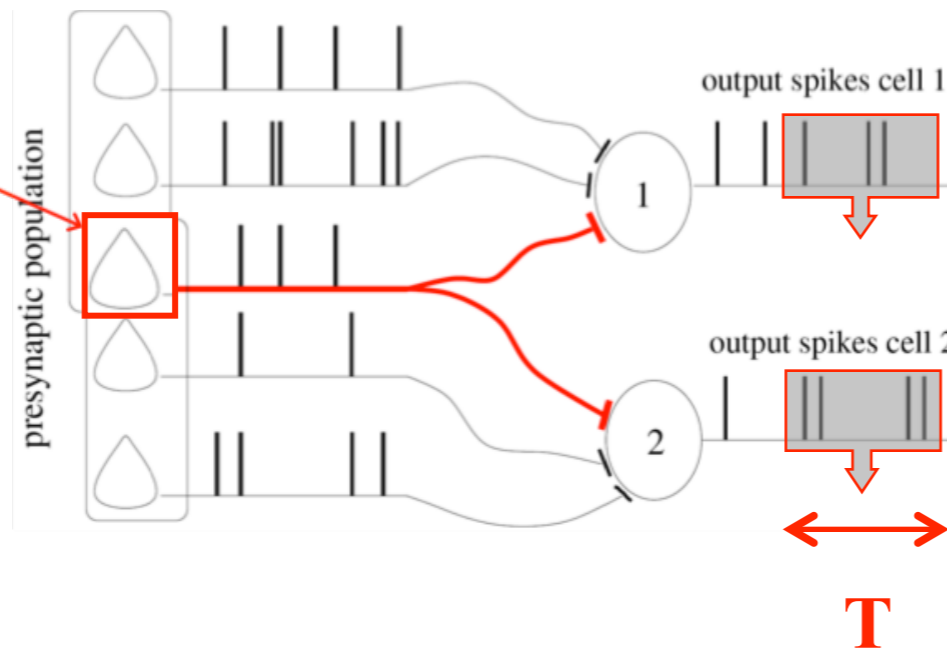
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$$\Rightarrow P(x_1, x_2 | s) \neq P(x_1 | s)P(x_2 | s)$$

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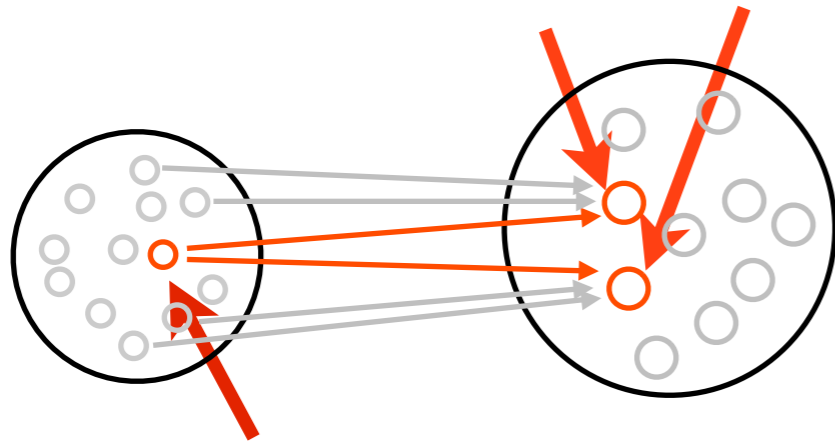


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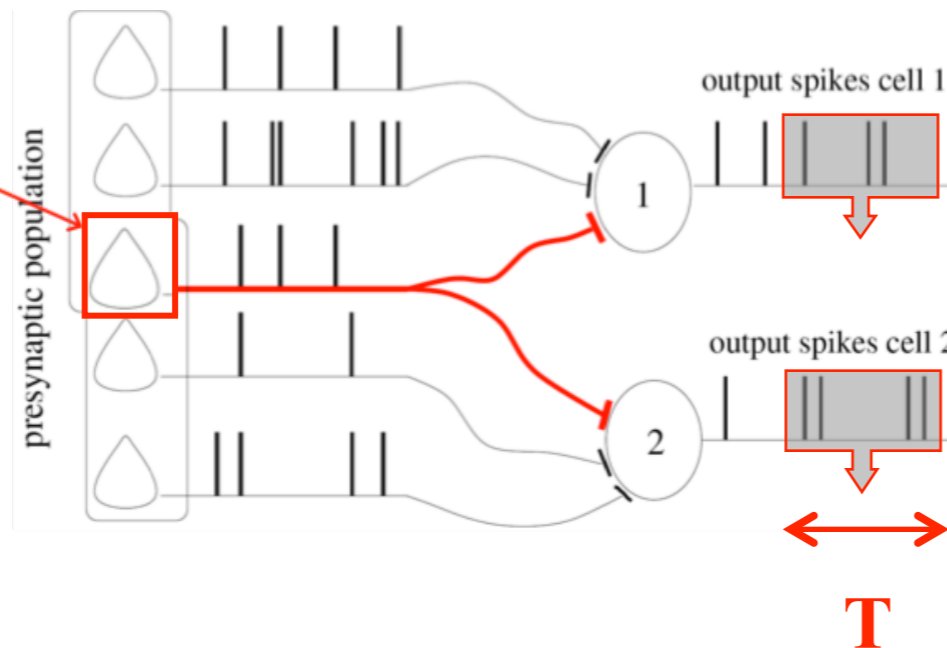
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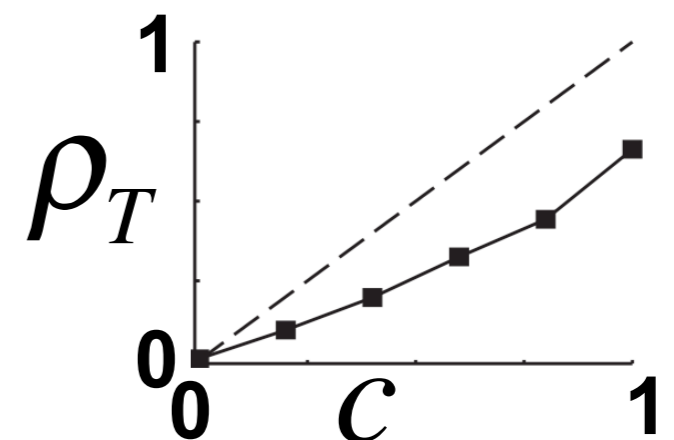
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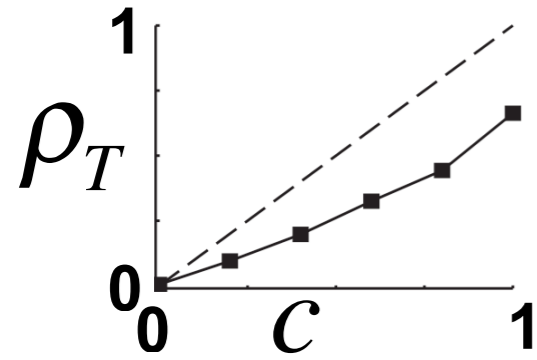


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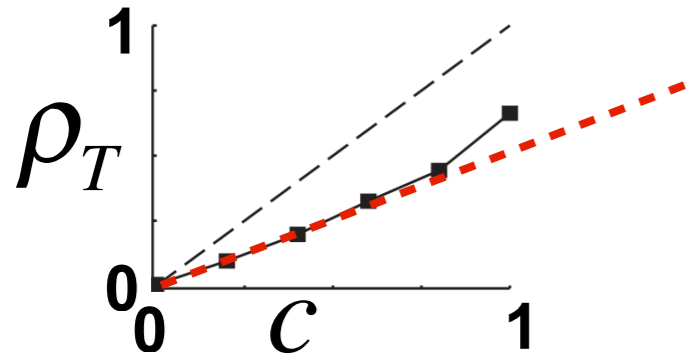
# How does this relationship depend on single cell dynamics?



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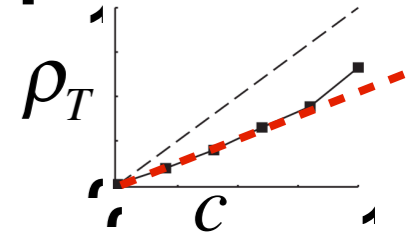
**Linear response theory: for small noise, linear in  $c$**  (cf. Lindner et al. 2005)



$$\rho_T \equiv \frac{\text{Cov}(n_1, n_2)}{\sqrt{\text{Var}(n_1)}\sqrt{\text{Var}(n_2)}} \approx c S_T$$



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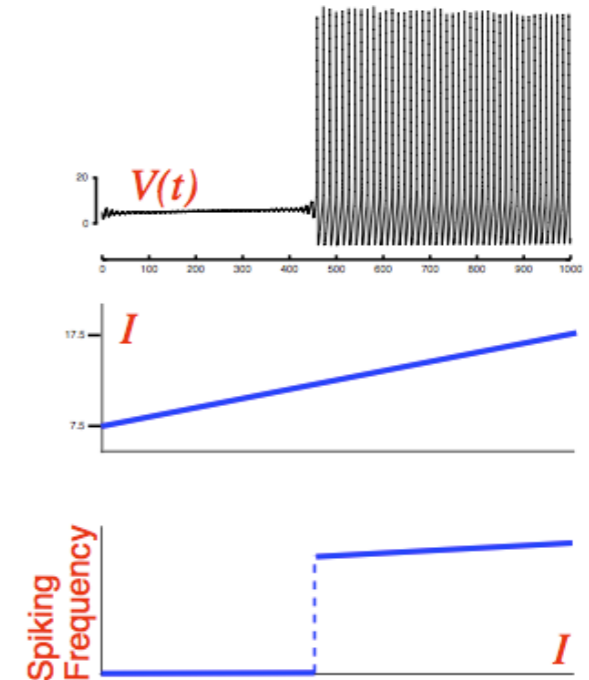
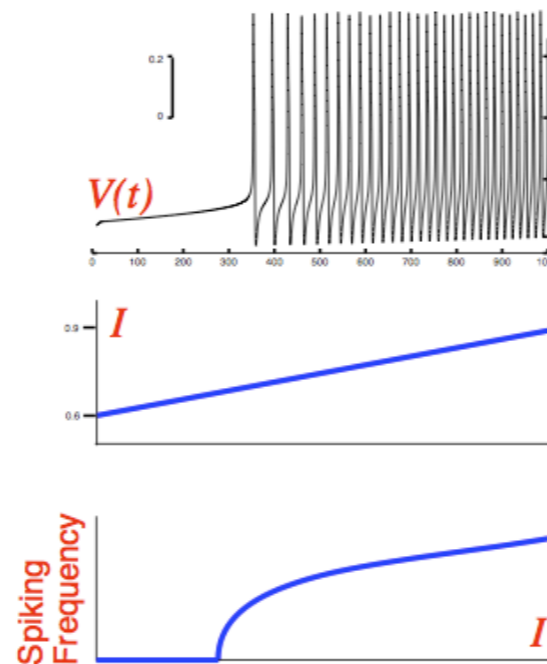
## One way to characterize neurons: resting-to-spiking excitability

$$C \frac{dV}{dt} = I - g_K n^4 (V - E_K) - g_{Na} m^3 h (V - E_{Na}) - g_L (V - E_L) + I_{app}$$

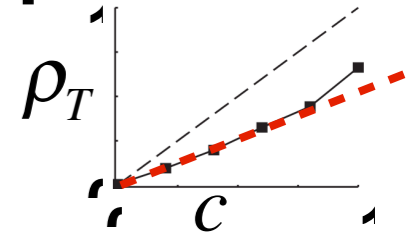
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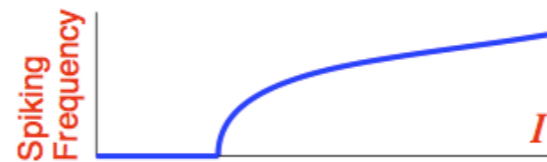
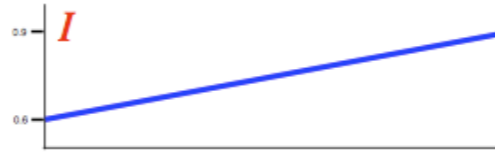
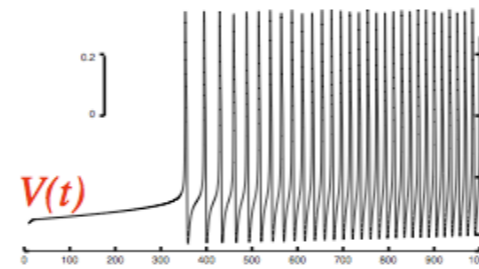
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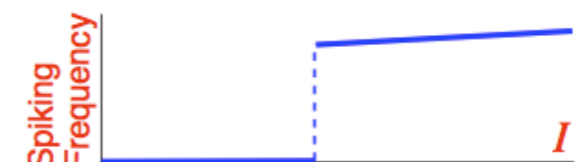
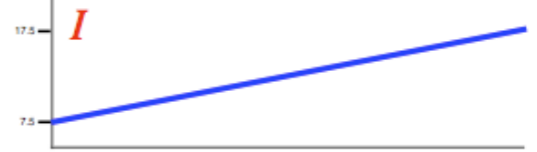
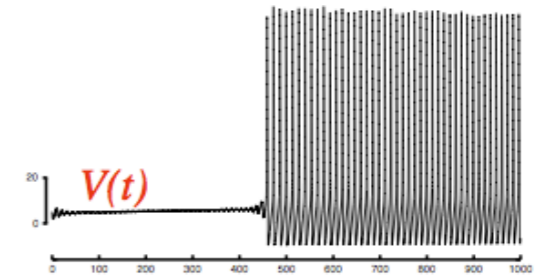
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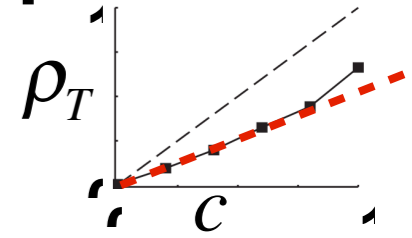


**Type I excitability**



**Type II excitability**

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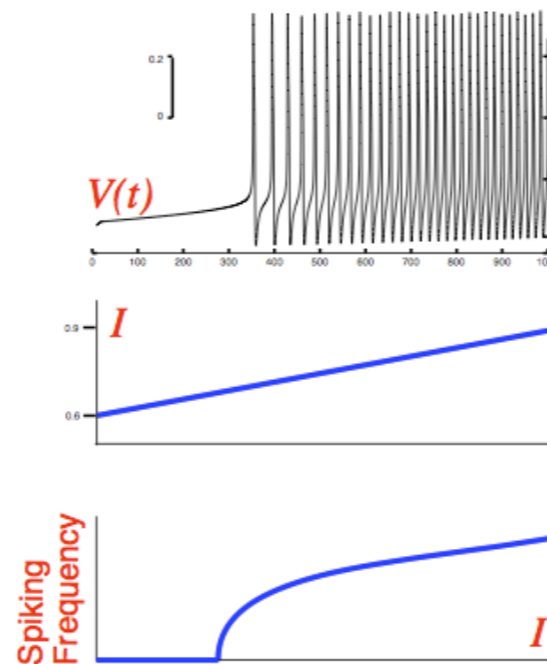
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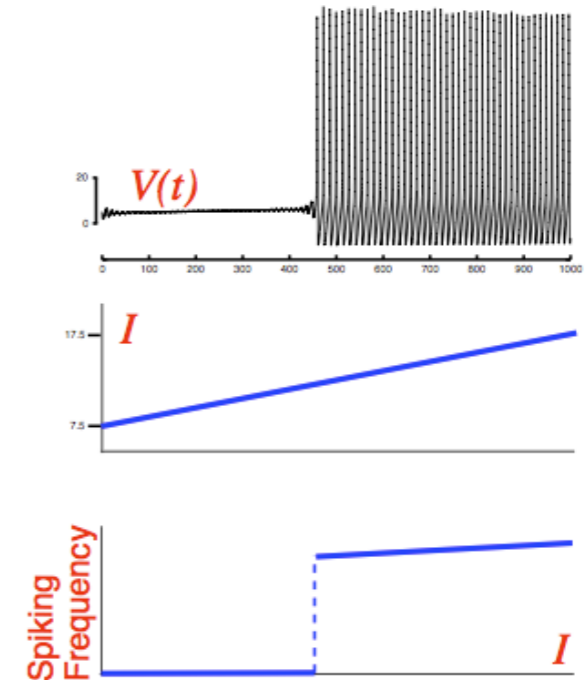
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**Type I excitability**



**Type II excitability**

## Compare Type I vs. Type II dynamics:

- Stimulus selectivity and neurocomputational properties: integrator vs. resonator (Agüera y Arcas et al. 2003; Mato and Samengo 2008)
- Synchronization properties (Ermentrout 1996; Hansel et al. 1995; Wang and Buzsáki 1996)
- Type I/II transition can be effected by regulating slow potassium currents (Ermentrout et al. 2001), such as by neuromodulators (Steifel et al. 2008a, 2008b) or level of background activity (Prescott et al. 2008)

# A neural model that shows both Type I and Type II excitability

## Connor-Stevens model

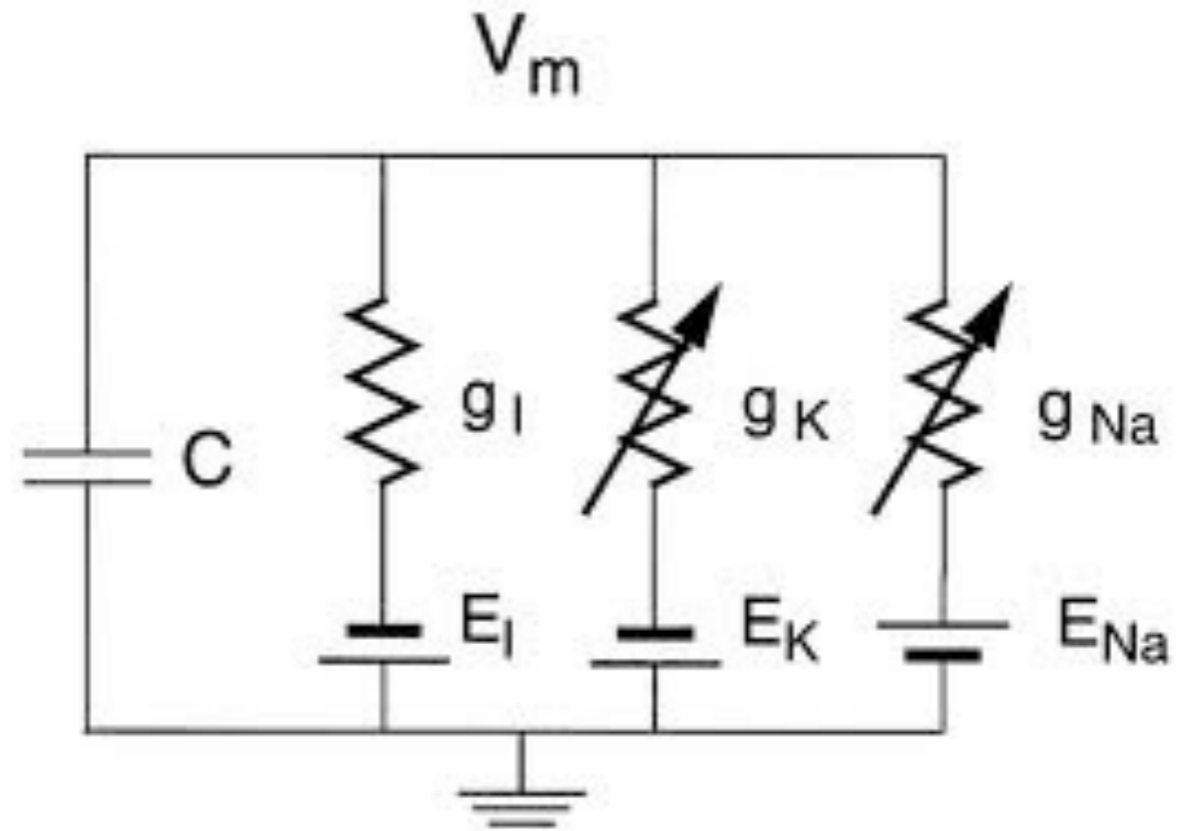
(Connor and Stevens 1971, Connor et al. 1977, Rush and Rinzel 1994)

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Hodgkin-Huxley

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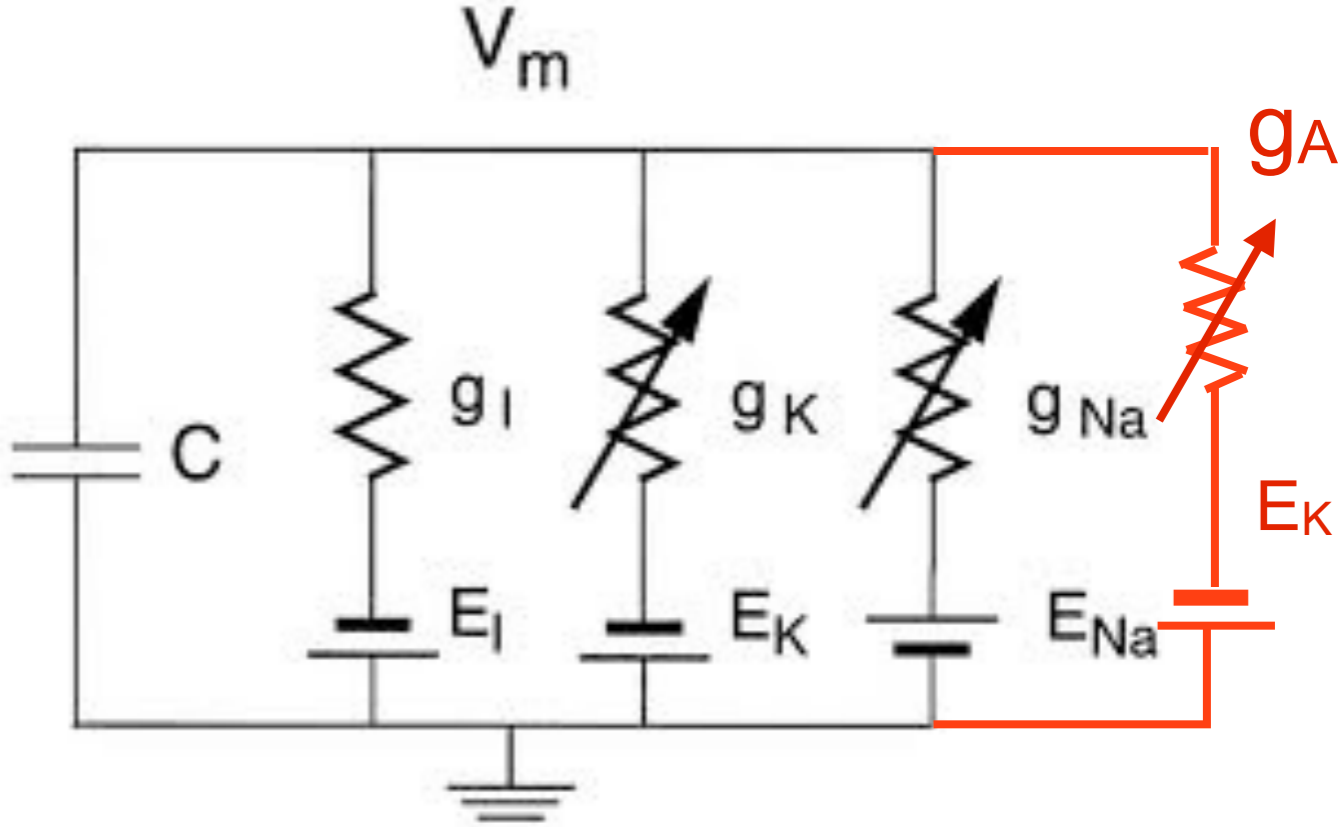
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Hodgkin-Huxley + transient A-current

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→  $-g_A a^3 b (V - E_K)$

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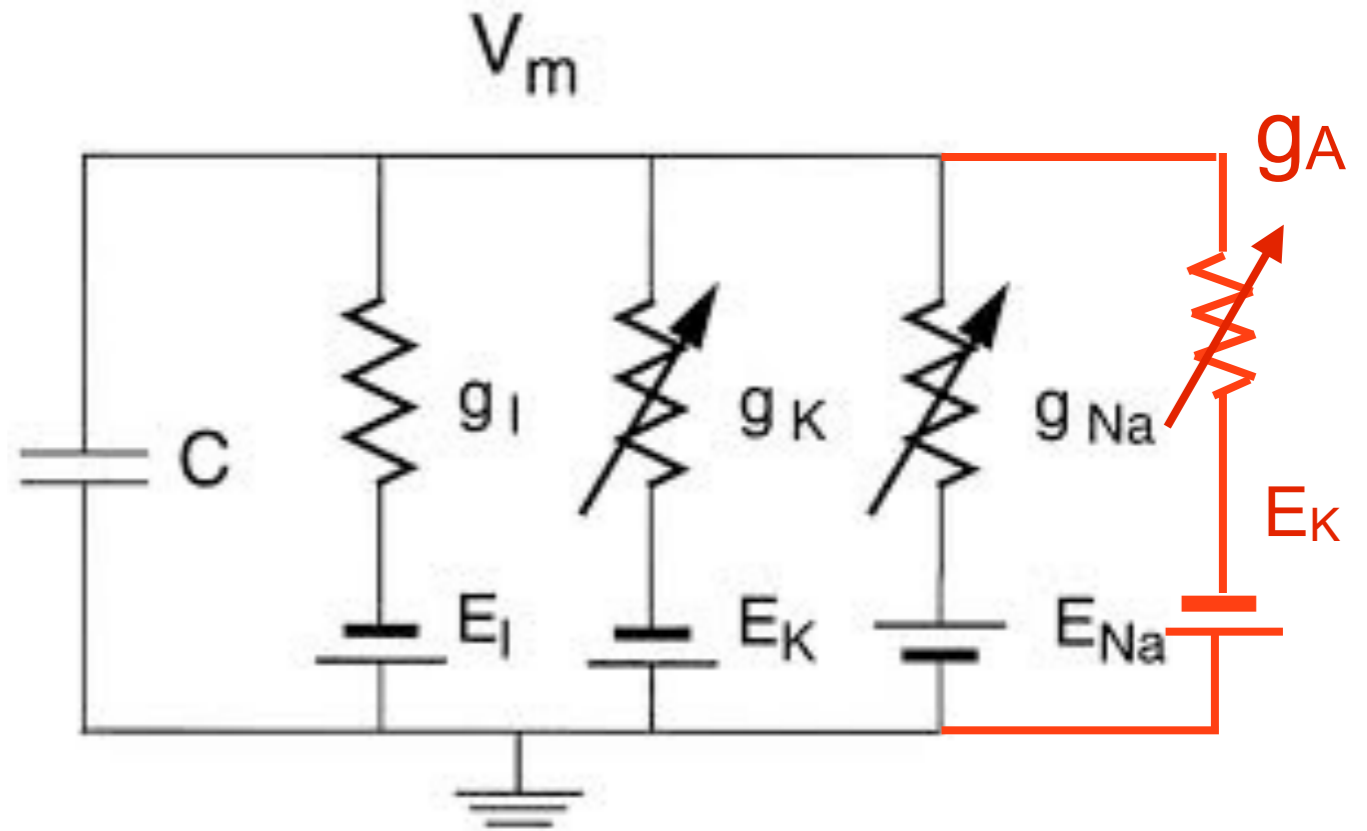
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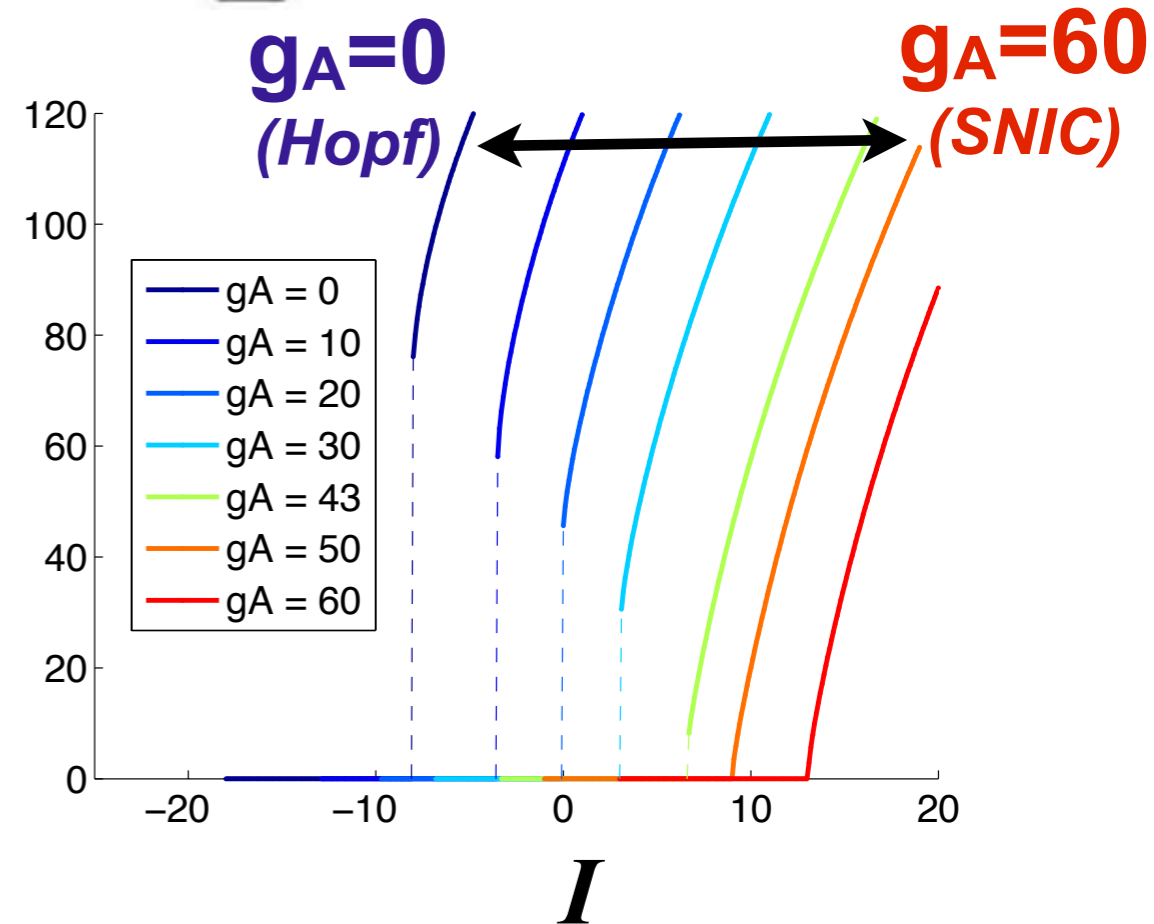
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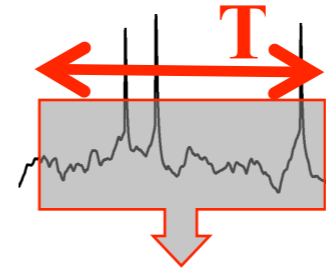
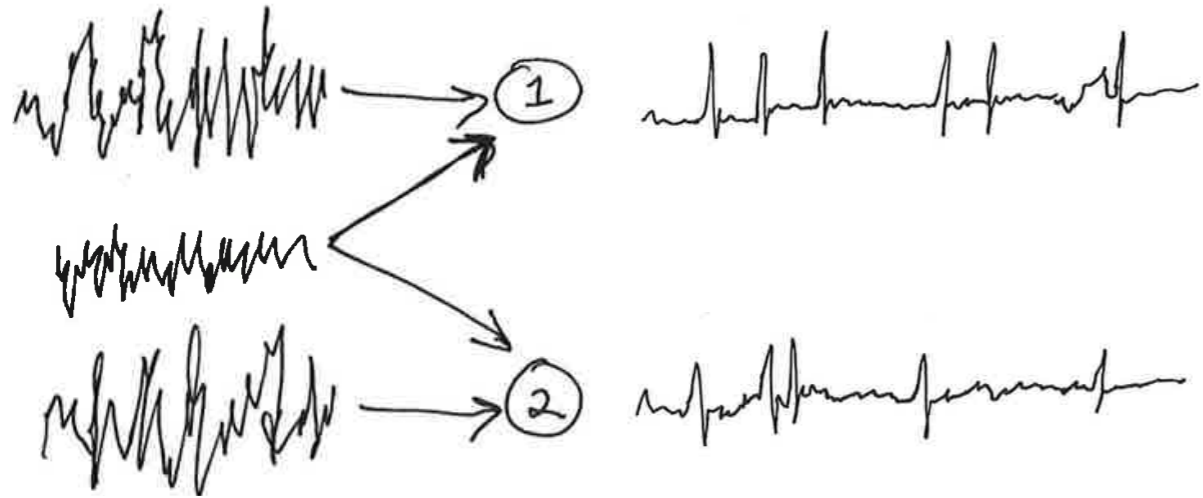
Hodgkin-Huxley + transient A-current



**firing rate**

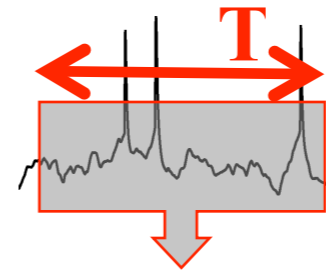
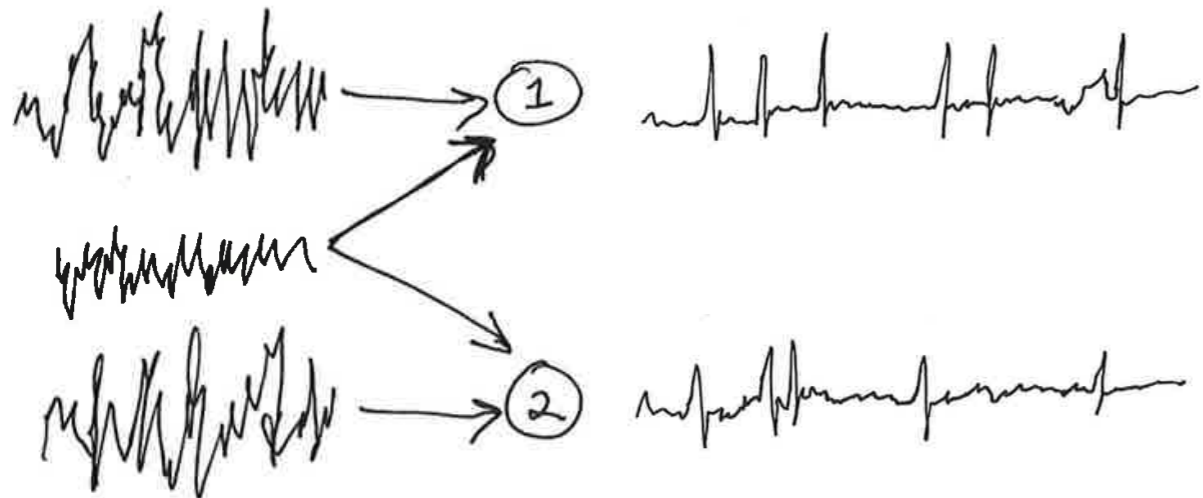


# Correlation transfer efficiency reverses, based on time scale

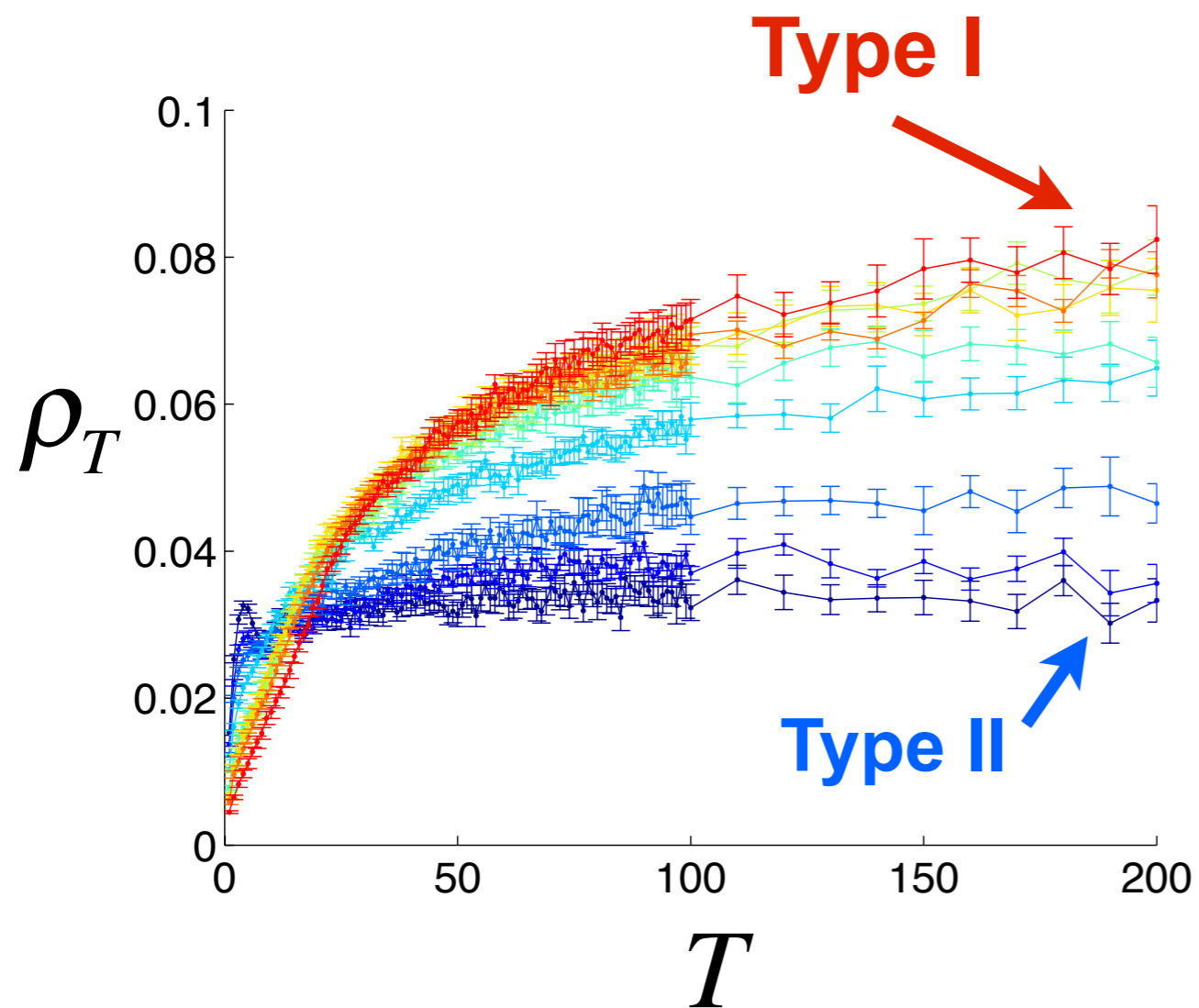


$$\rho_T = \frac{Cov(n_1, n_2)}{\sqrt{Var(n_1)Var(n_2)}}$$

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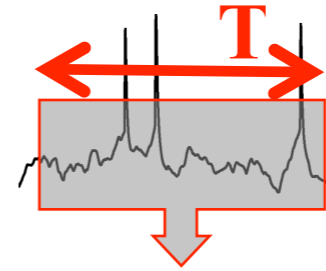
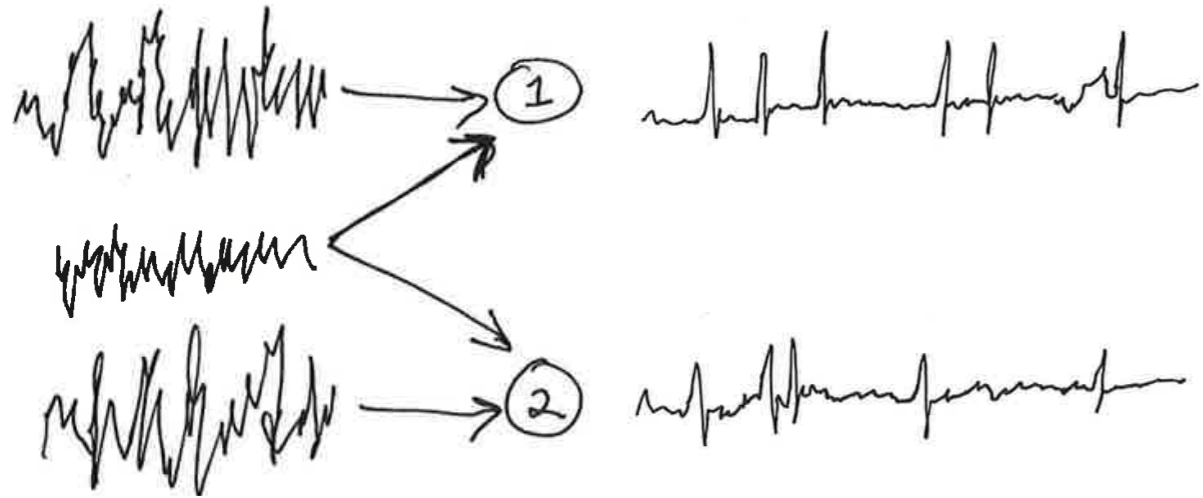


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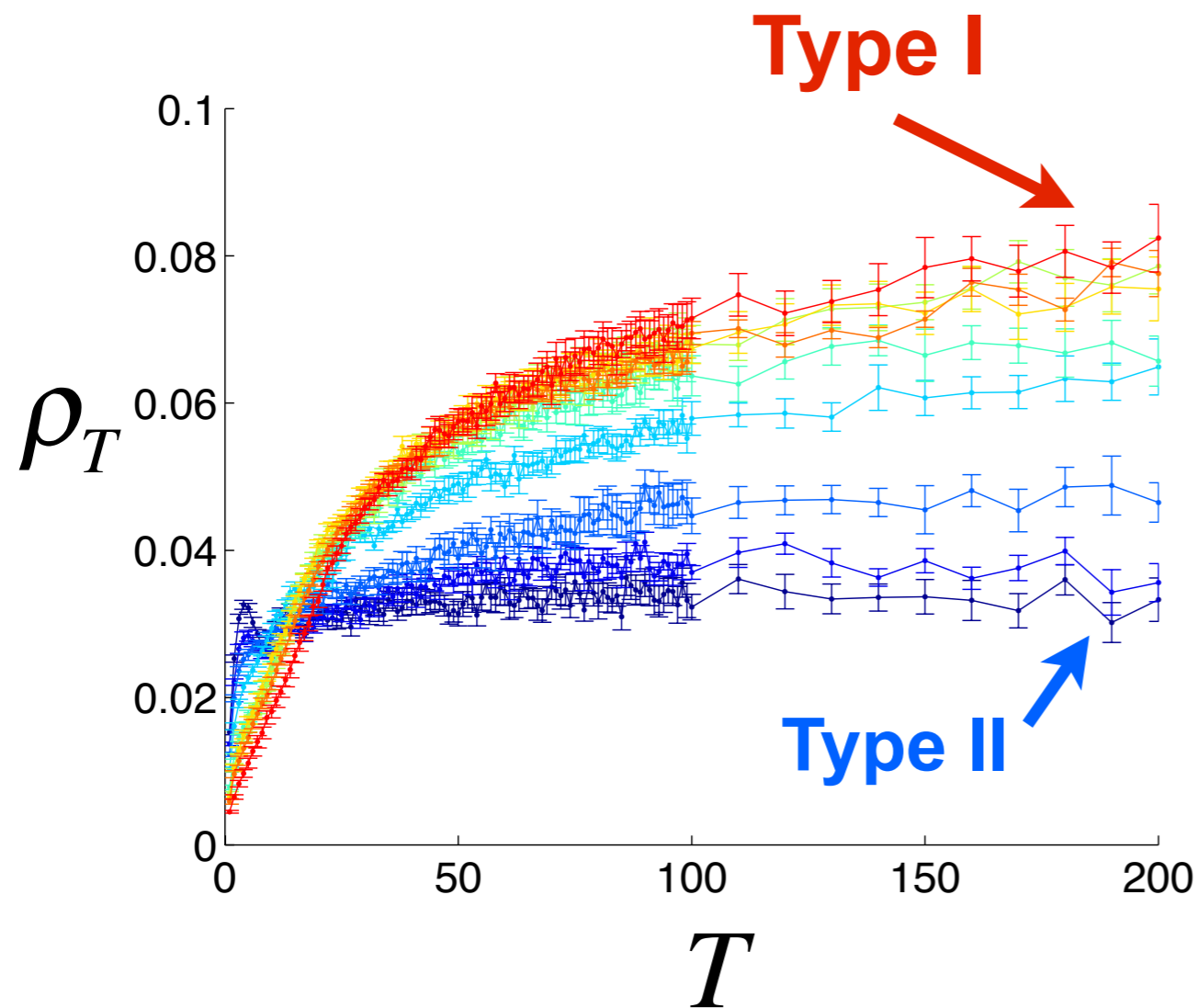




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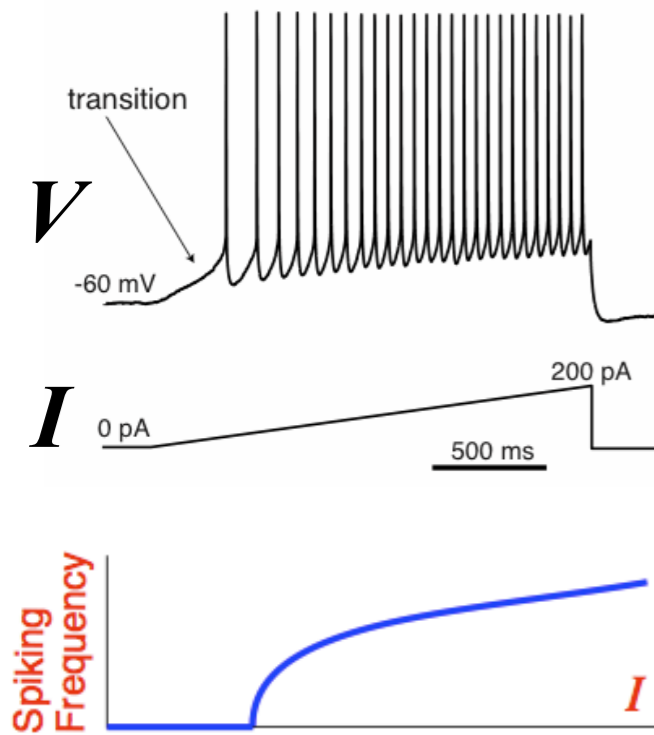
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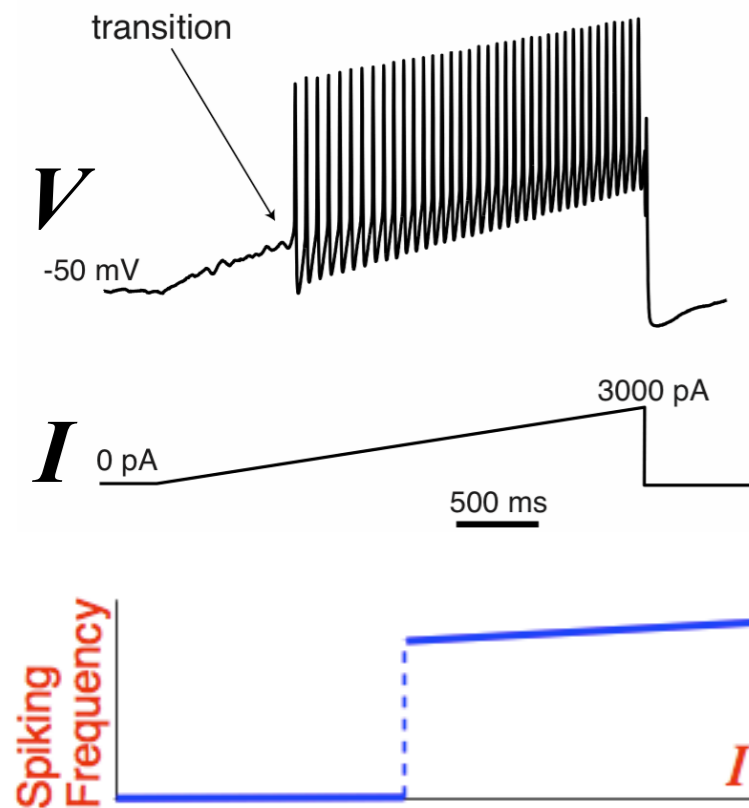
**Type II** cells transfer more correlation at *short* time scales;  
**Type I** cells transfer more correlation at *long* time scales

# How can we understand this mathematically?

## Reduced model for ODEs near a limit cycle



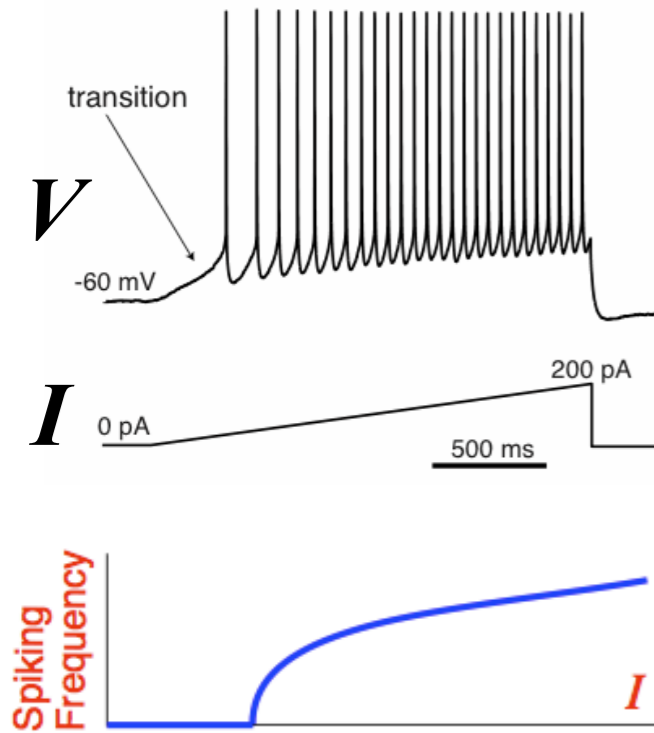
### Type I excitability (SNIC)



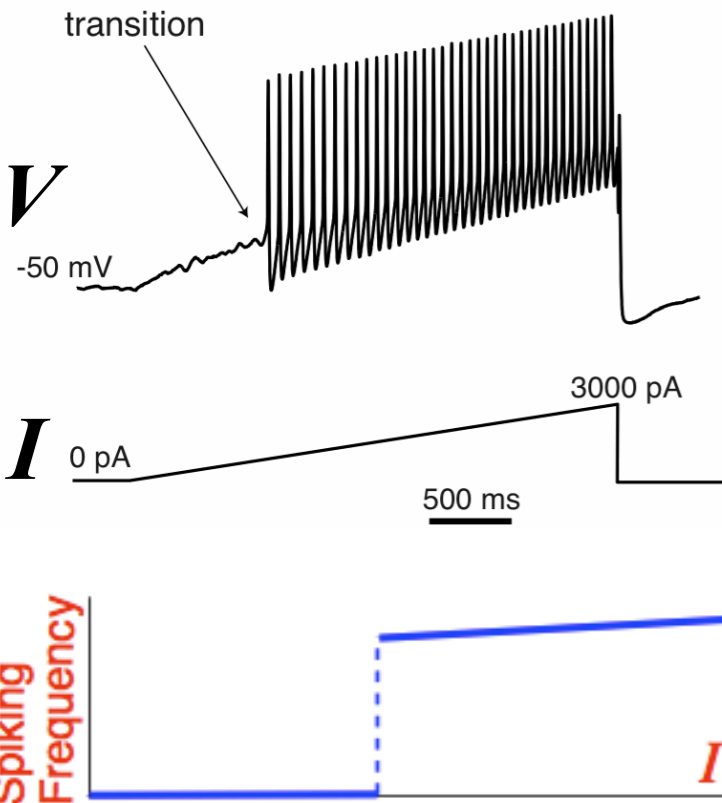
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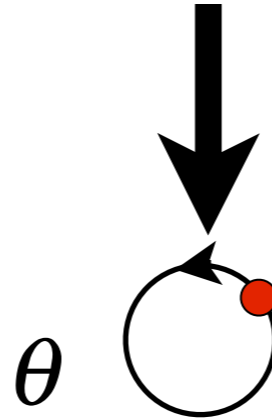


### Type I excitability (SNIC)



### Type II excitability (Hopf)

If the neuron is firing periodically (“tonic” firing)



$$\frac{\partial \theta}{\partial t} = \omega + Z(\theta) I_{fluc}(t)$$

$$\theta = 2\pi \rightarrow \textit{spike}$$

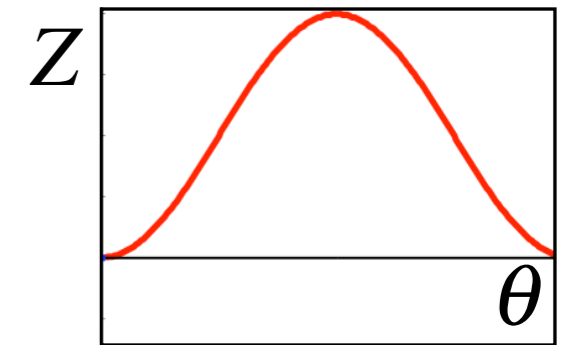
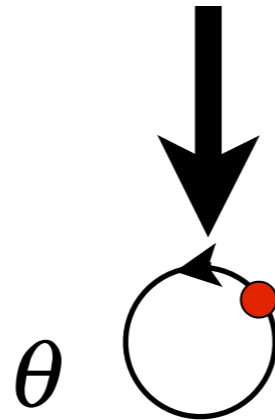
$Z(\theta)$  = phase response curve (PRC)

phase model

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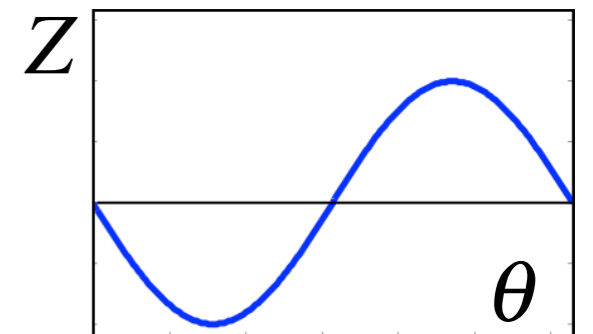
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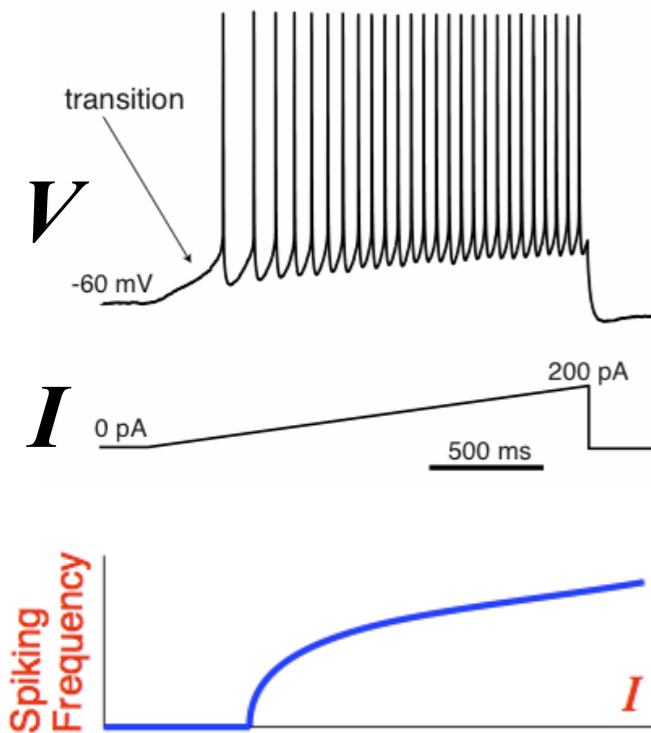
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**Type I excitability**



$$Z(\theta) = -\sin \theta$$

**Type II excitability**



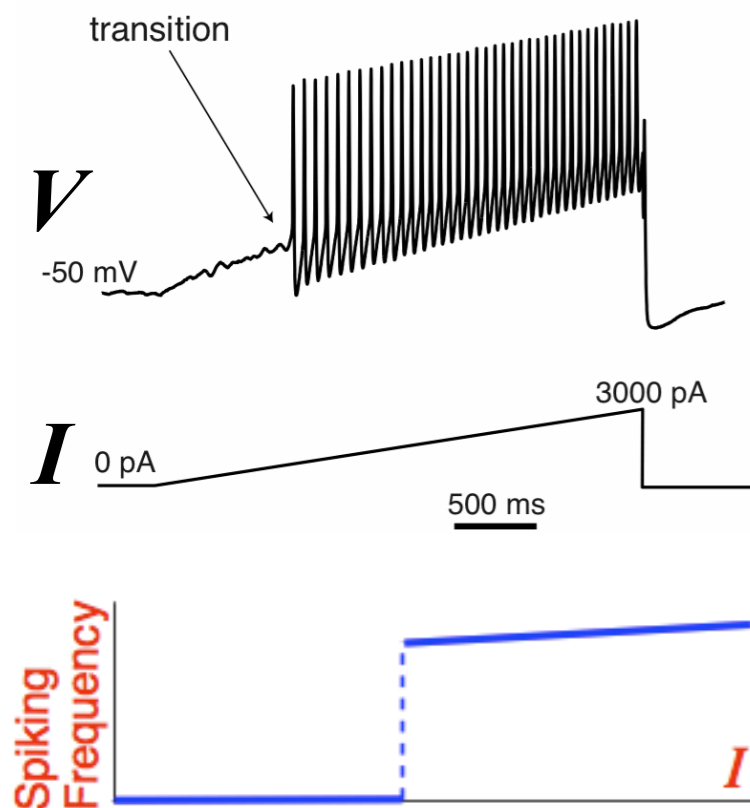
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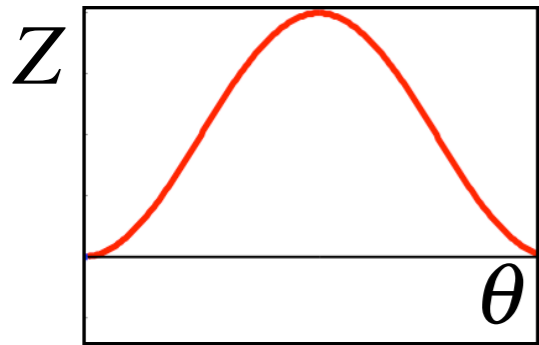
**phase model**



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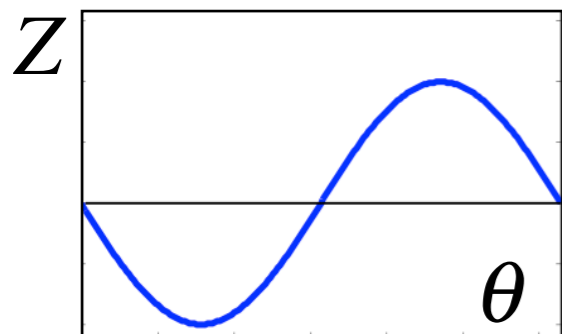
Rinzel and Ermentrout '89  
Ermentrout and Kopell '84  
Ermentrout '96

Not just an academic exercise: PRCs can be measured (and modulated) in real neurons



$$Z(\theta) = 1 - \cos \theta$$

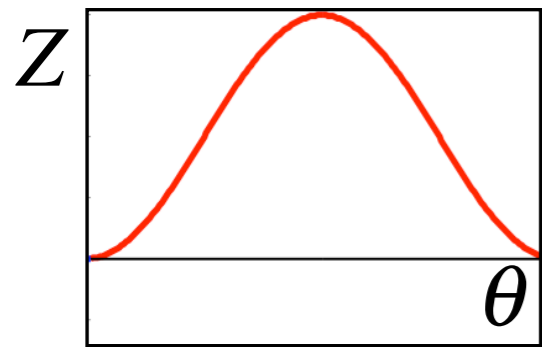
**Type I  
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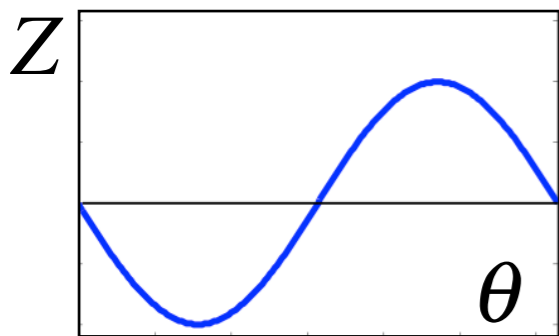
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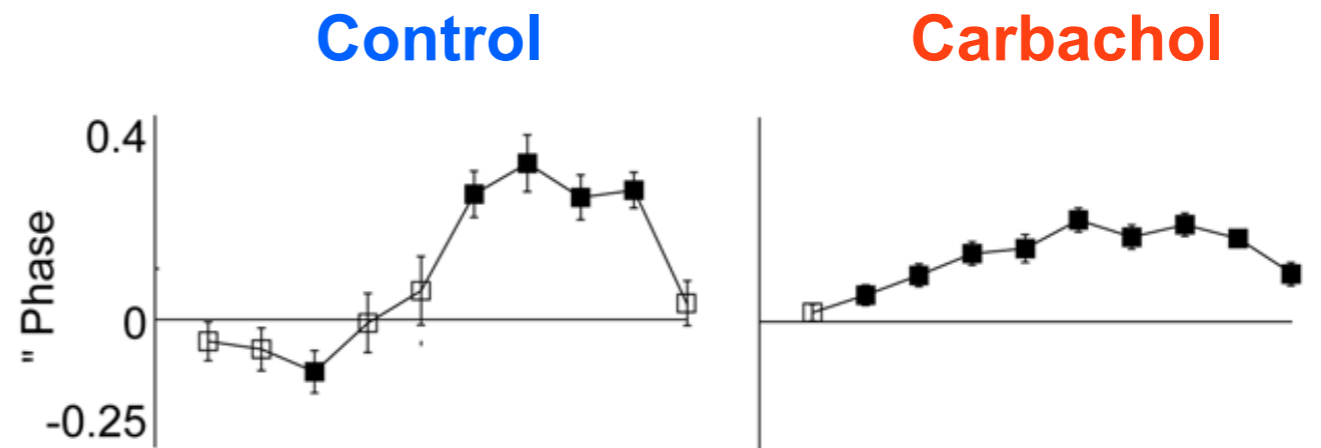
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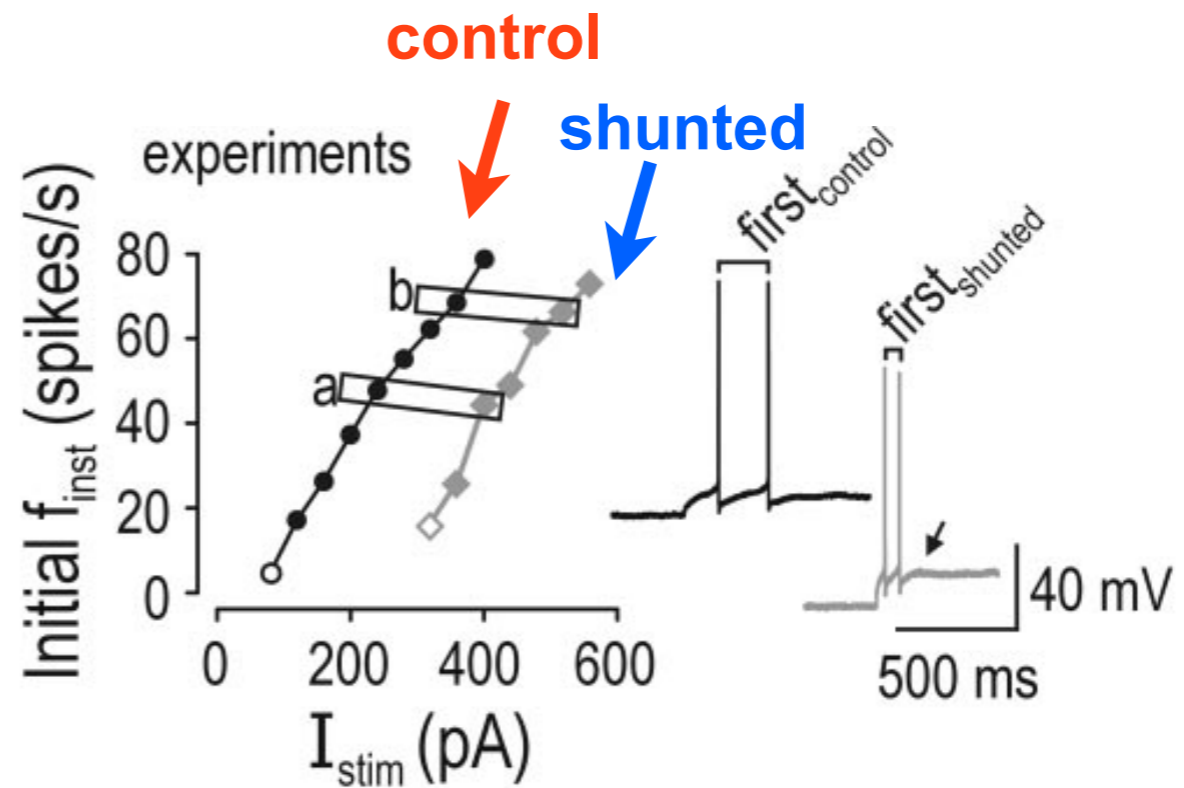


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**Type II  
excitability**



Stiefel et al., PLoS One, 2008



Prescott et al, J Neurophys, 2008

# Analytical calculations in phase models

$$T \gg 1 \rightarrow \rho_T \approx c \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} = cS$$

but

$$T \ll 1, \rho \approx cT \left( 1 - \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} \right) = cT(1 - S)$$

**Marella and Ermentrout, PRE, 2008**

**Barreiro et al., PRE, 2010**

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**Type I** cells are more efficient at transferring correlated input at **long** time scales, **Type II** at **short** time scales.

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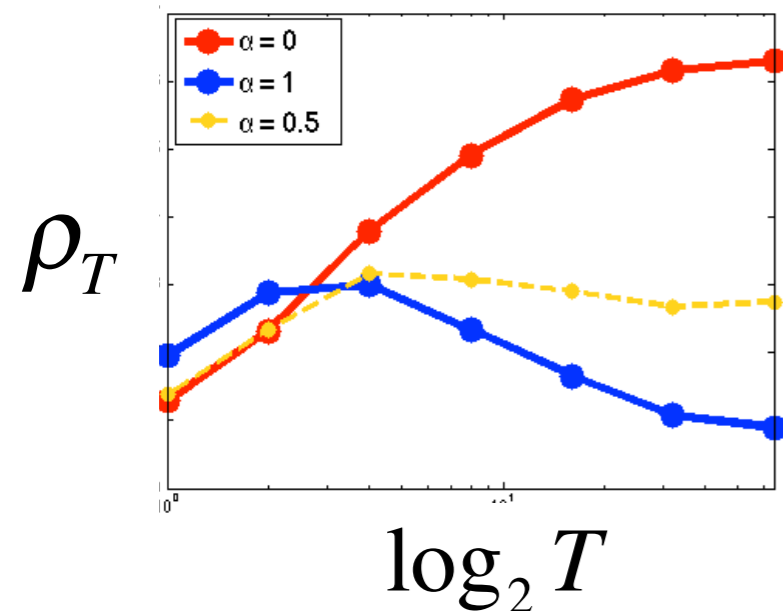
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**In sinusoidal phase oscillators:**



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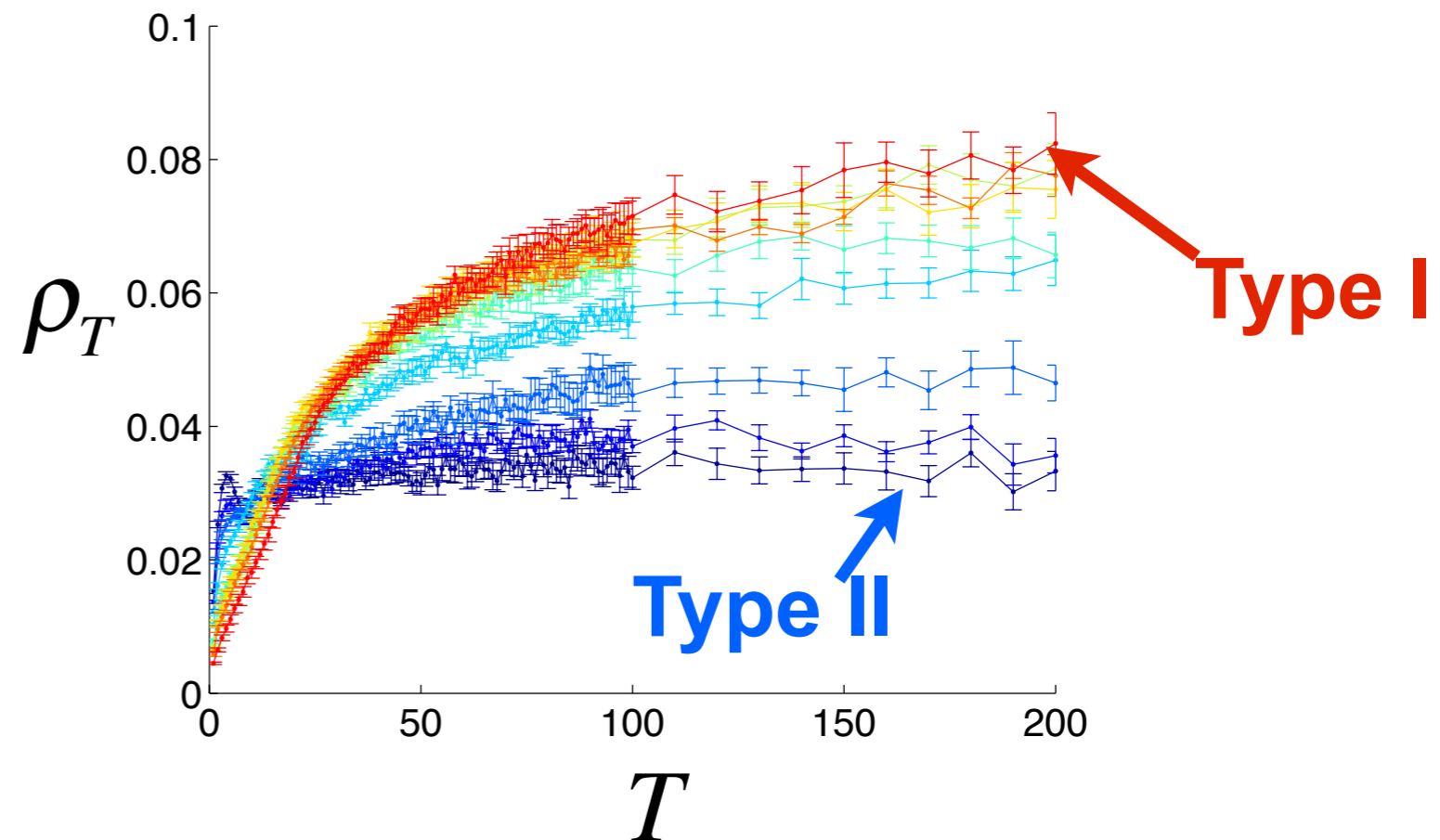
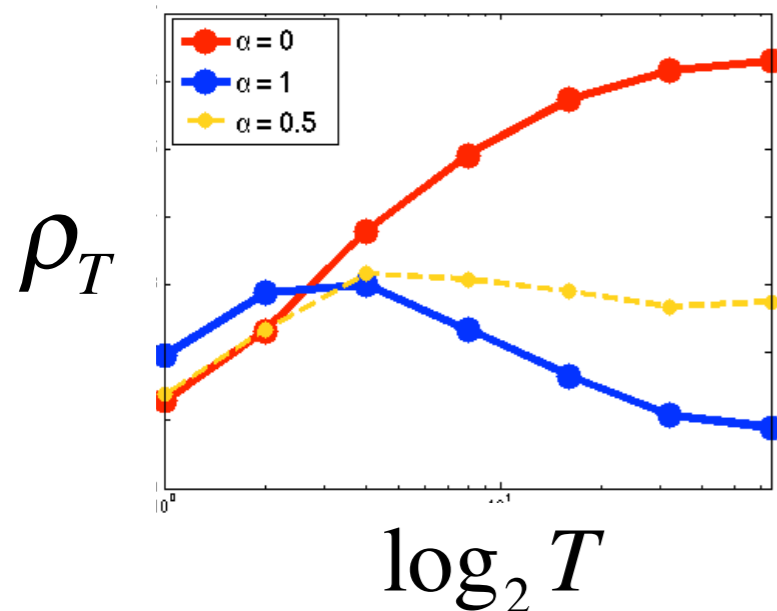
but

$$T \ll 1, \rho \approx cT \left( 1 - \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} \right) = cT(1 - S)$$



**Type I** cells are more efficient at transferring correlated input at **long** time scales, **Type II** at **short** time scales.

**In sinusoidal phase oscillators:**



- Marella and Ermentrout, PRE, 2008
- Barreiro et al., PRE, 2010
- Abouzeid and Ermentrout, PRE, 2011
- Barreiro et al., *J Neurophys* 2012

# Analytical calculations in phase models

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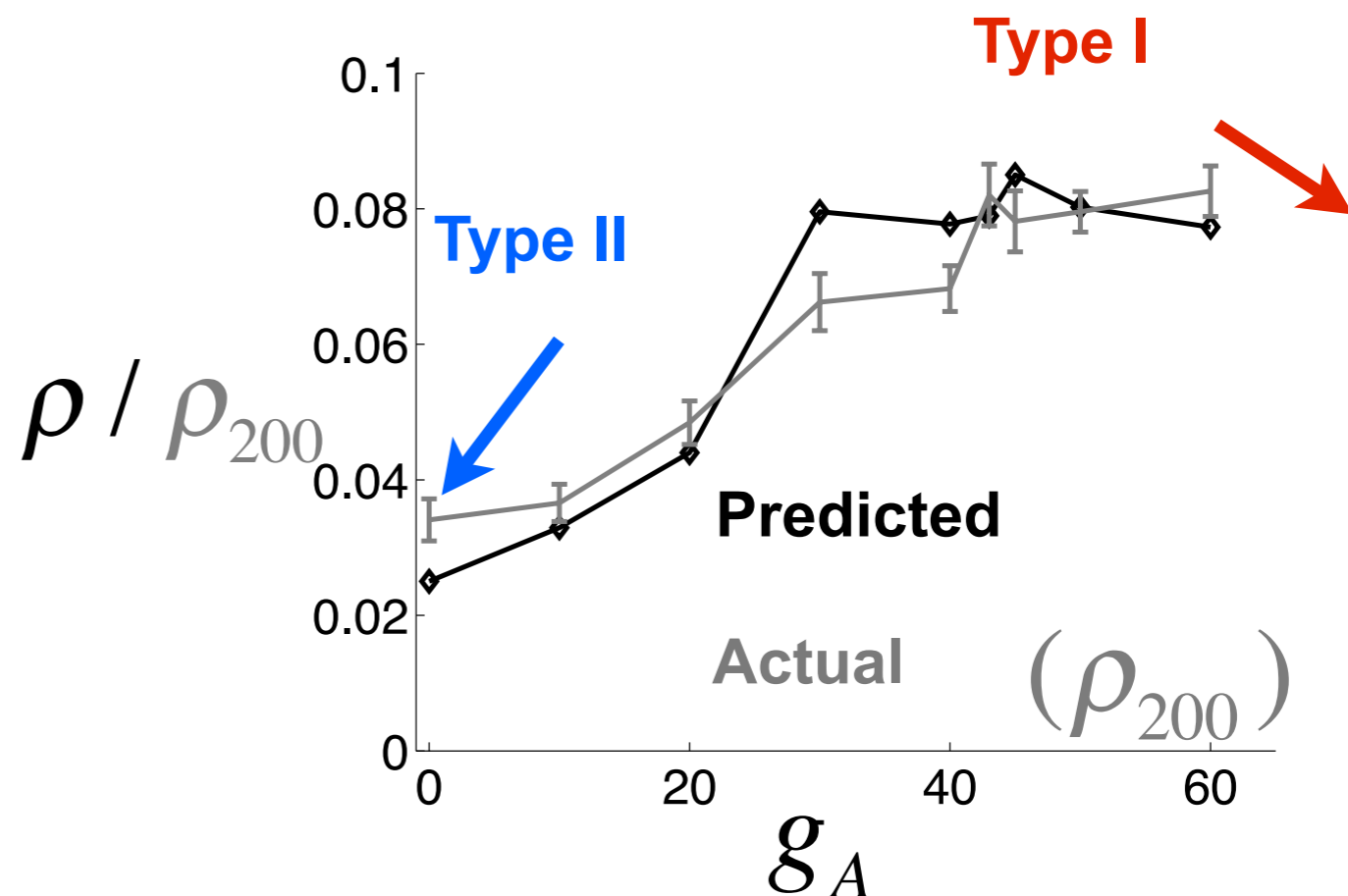
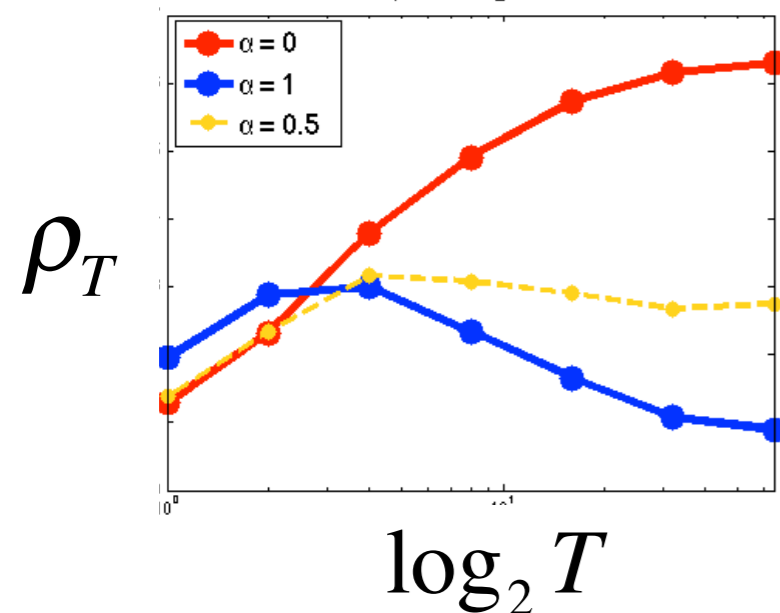
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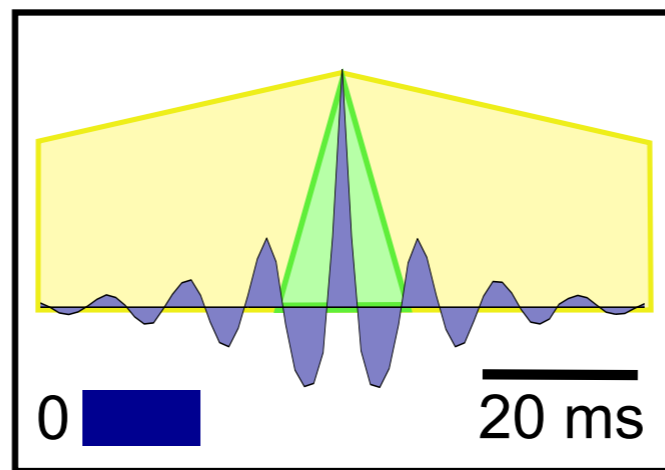
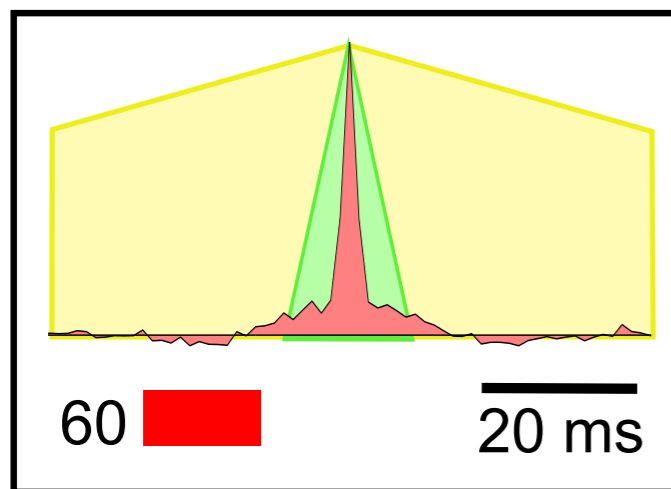
Barreiro et al., *J Neurophys* 2012

**Another prediction tool:  
Use common input *spike-triggered  
average (STA)***

$$Cov_T(n_1, n_2) = T \int_{-T}^T C_{12}(t) \left(1 - \frac{t}{T}\right) dt$$

$$C_{12}(t) \propto c(K * \tilde{K})(t); \quad K(t) = STA(t), \tilde{K} = STA(-t)$$

$$STA(t) = \frac{1}{N_{sp}} \sum_{k=1}^{N_{sp}} I_c(t_k - t)$$



10 ms  
128 ms

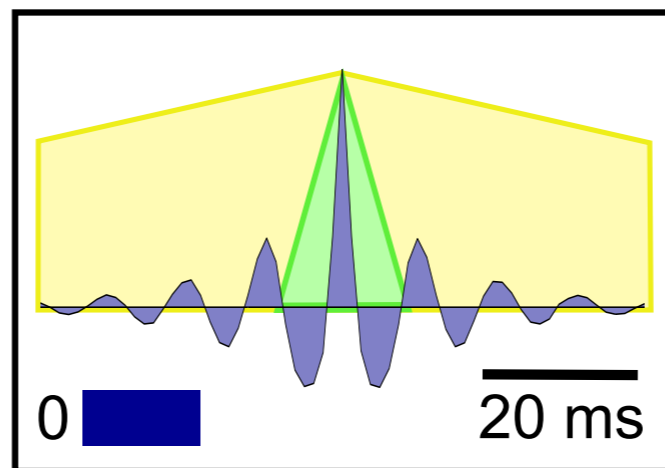
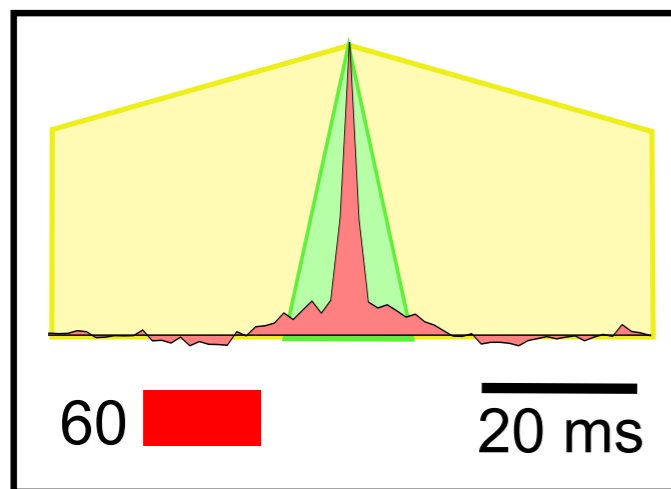
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Bair et al. 2001,  
Gabbiani and Koch 1998,  
Ostojic 2009;  
(but see Hong et al. 2012)



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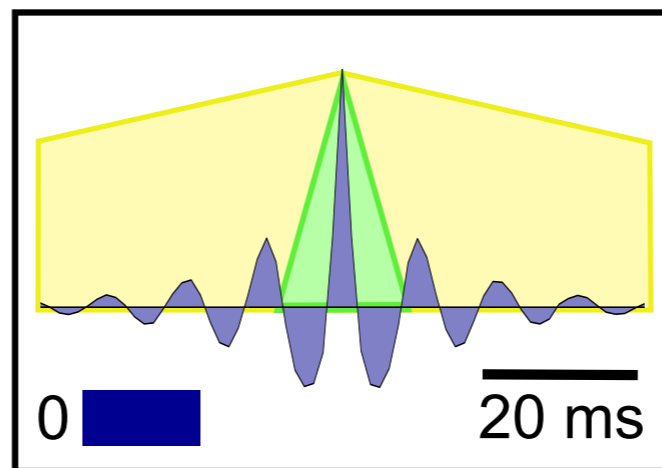
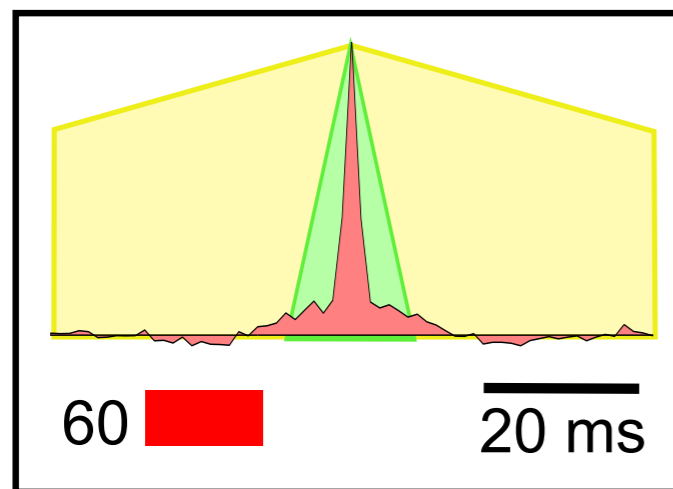
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Bair et al. 2001,  
Gabbiani and Koch 1998,  
Ostojic 2009;  
(but see Hong et al. 2012)

- Can be used in the subthreshold (excitable) regime
- Time window ( $T$ )-specific prediction



**10 ms**  
**128 ms**

# STA is very predictive of correlation transfer

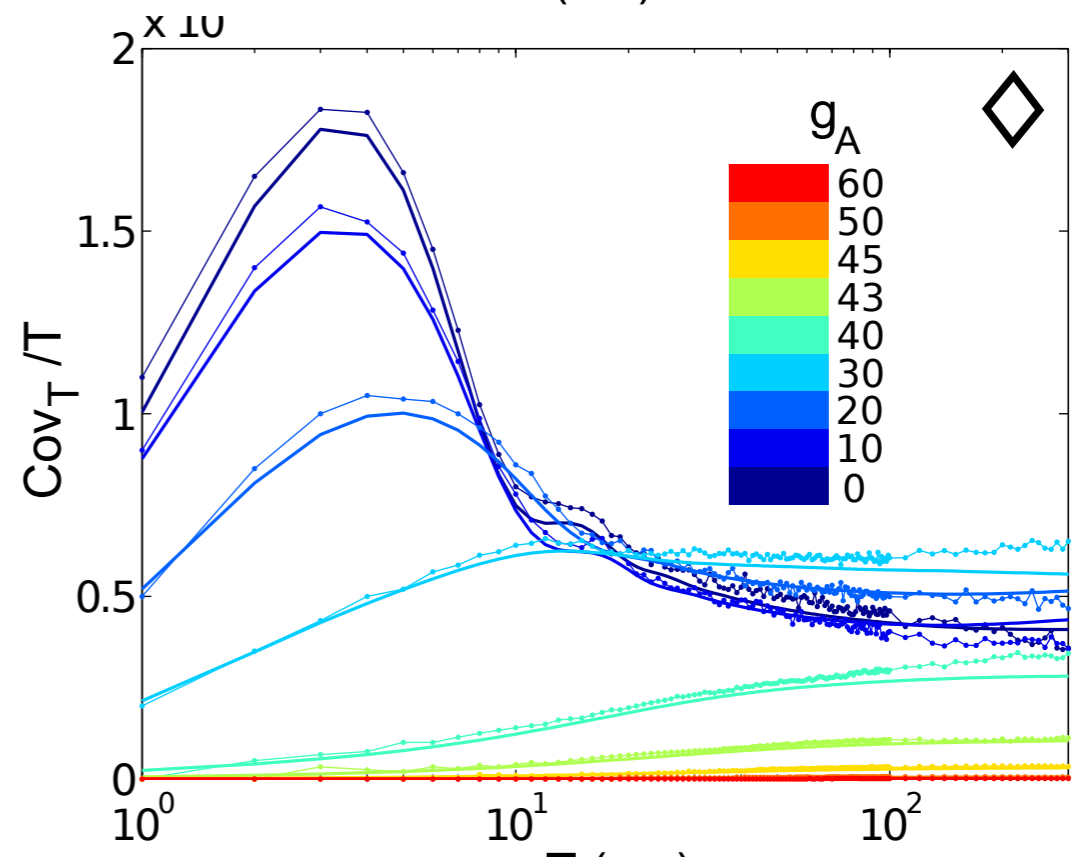
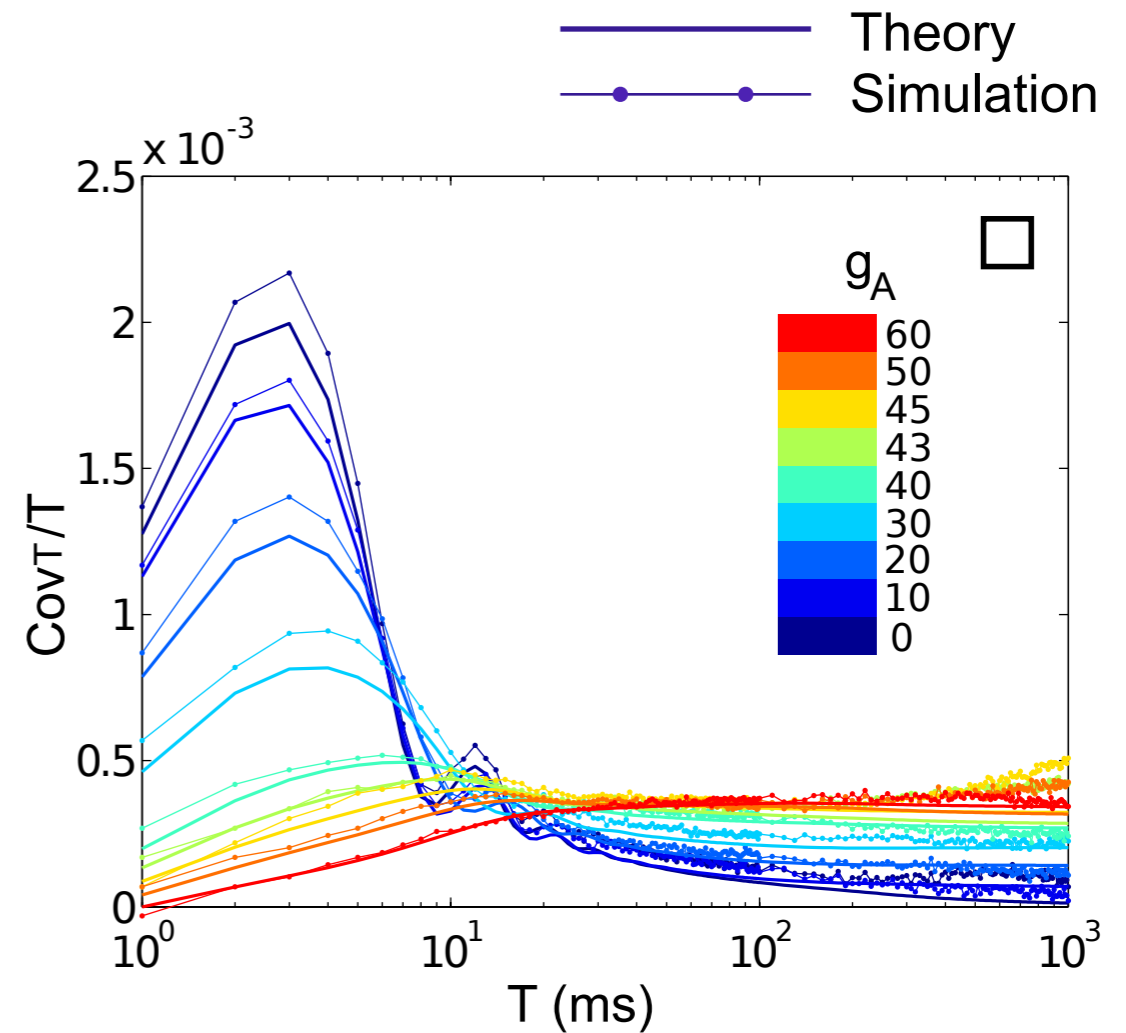
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$$K(t) = STA(t), \tilde{K} = STA(-t)$$

superthreshold  
(mean-driven)

subthreshold  
(fluctuation-driven)



# Correlation transfer modulates downstream firing rate

$$\tau \dot{V} = -V + I(t)$$

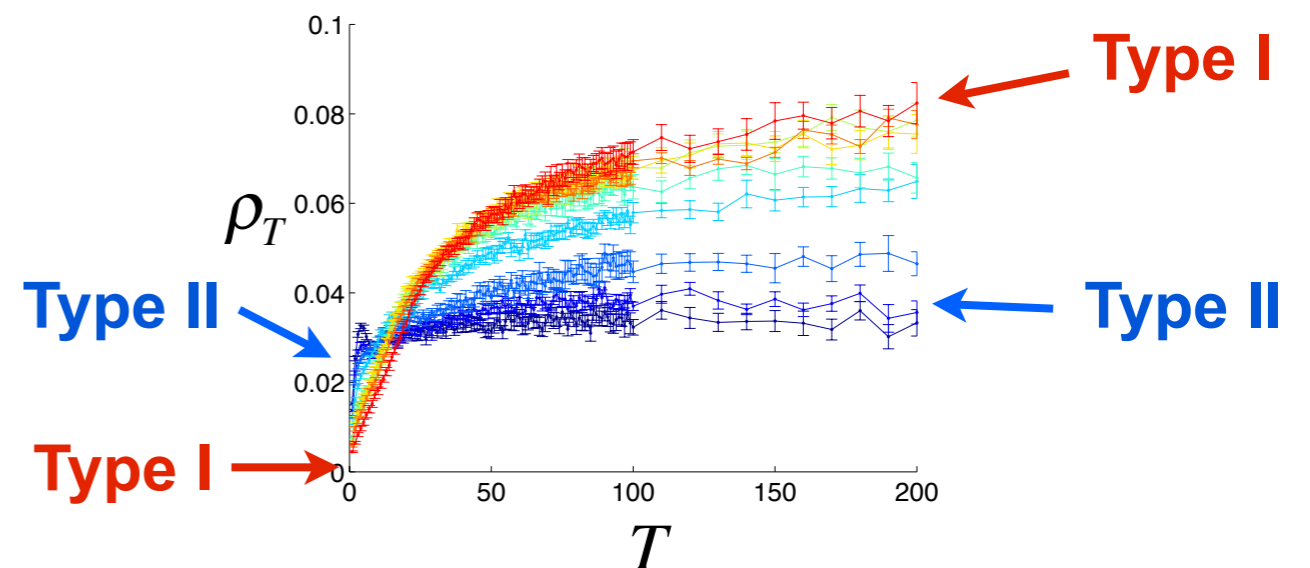
???

“Hears”  $\sum_i n_i^{(\tau)}$  ..... larger fluctuations in this sum trigger more frequent spikes

**Type II** cells will be more effective than **Type I cells** at driving *short time constant* neurons

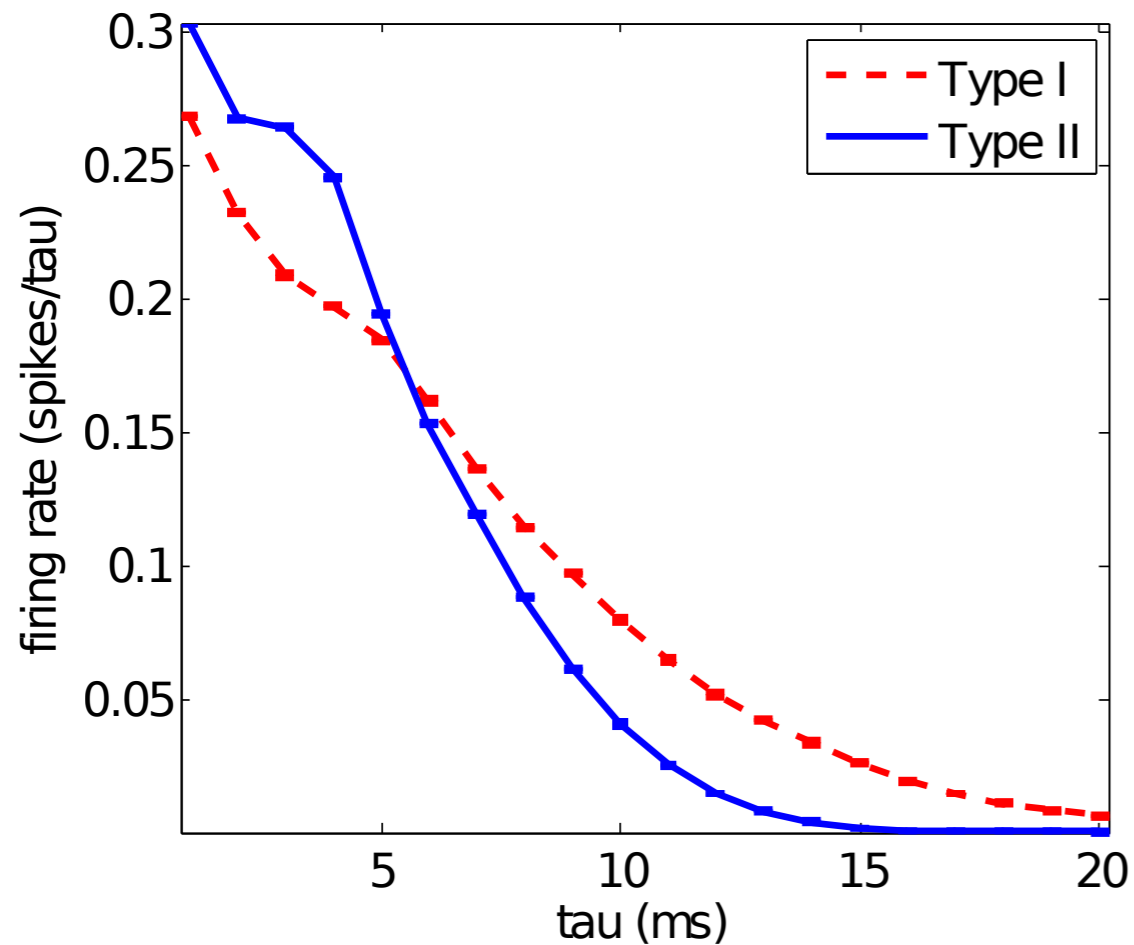
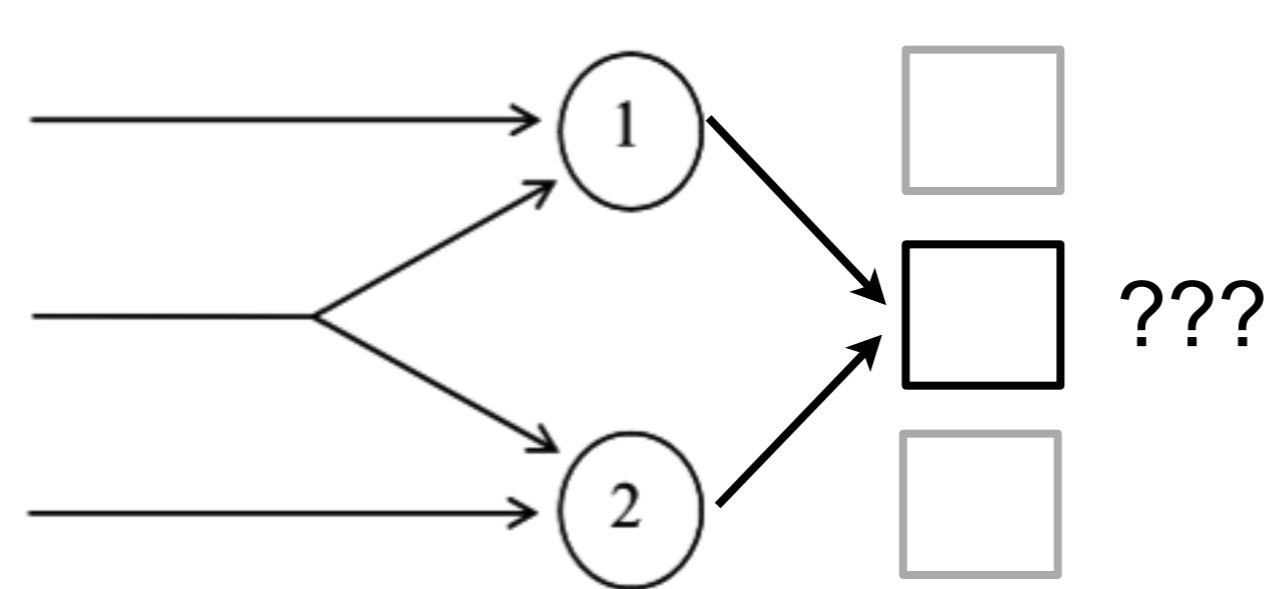
**Type I** cells will be more effective than **Type II** cells at driving *long time constant* neurons

$$\text{Var} \left( \sum_i n_i^{(\tau)} \right) \propto N^2 \rho_\tau$$

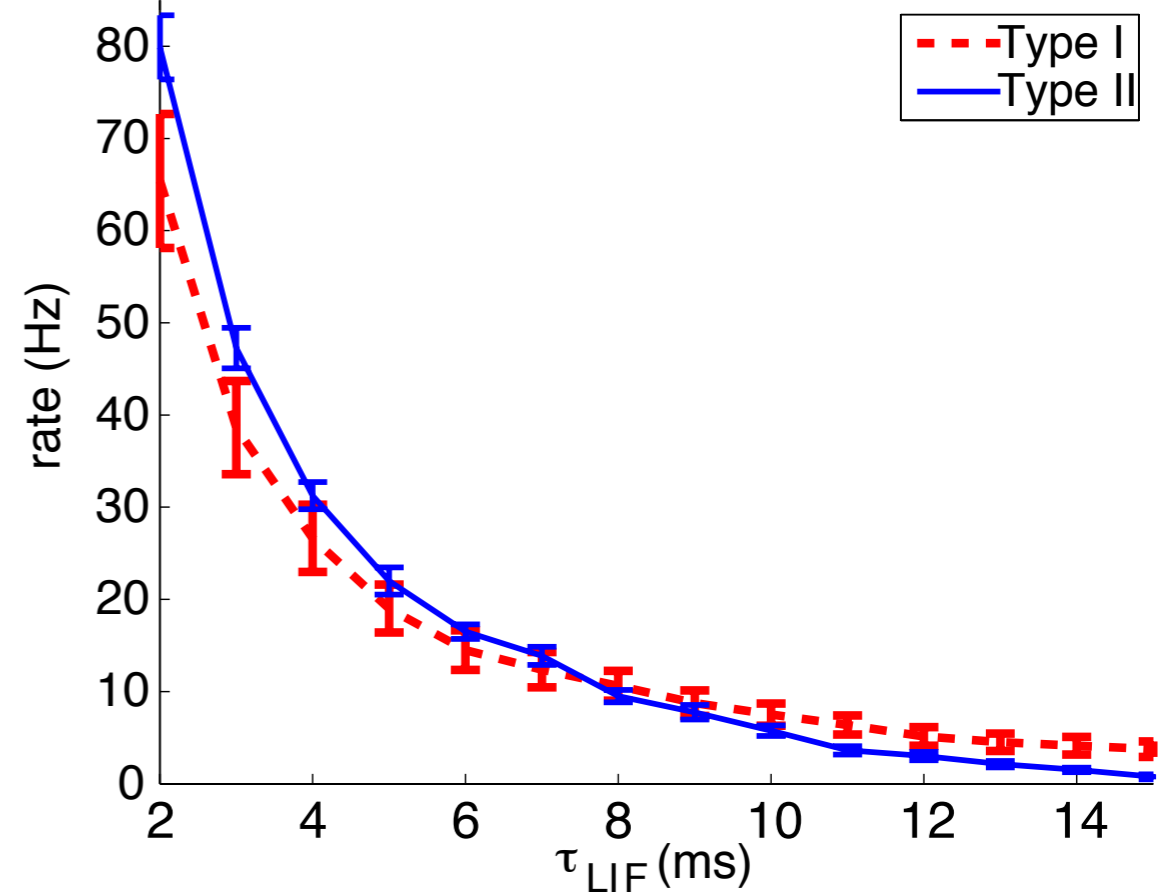




# Modulatory effect seen across upstream operating regimes

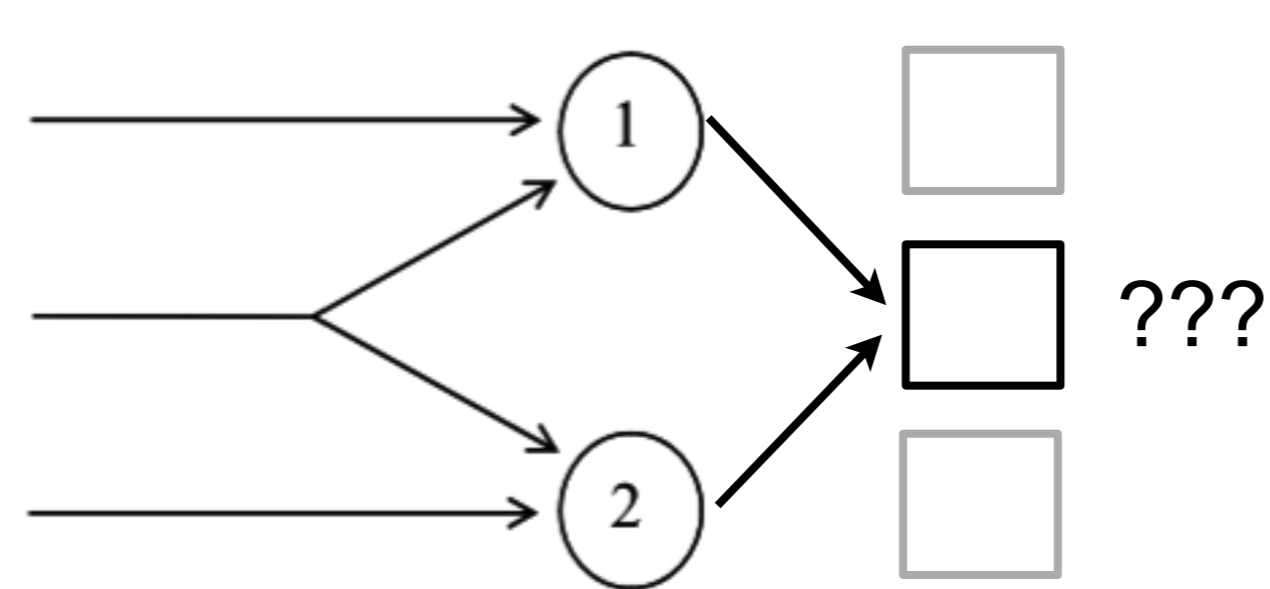


mean-driven upstream layer



fluctuation-driven upstream layer

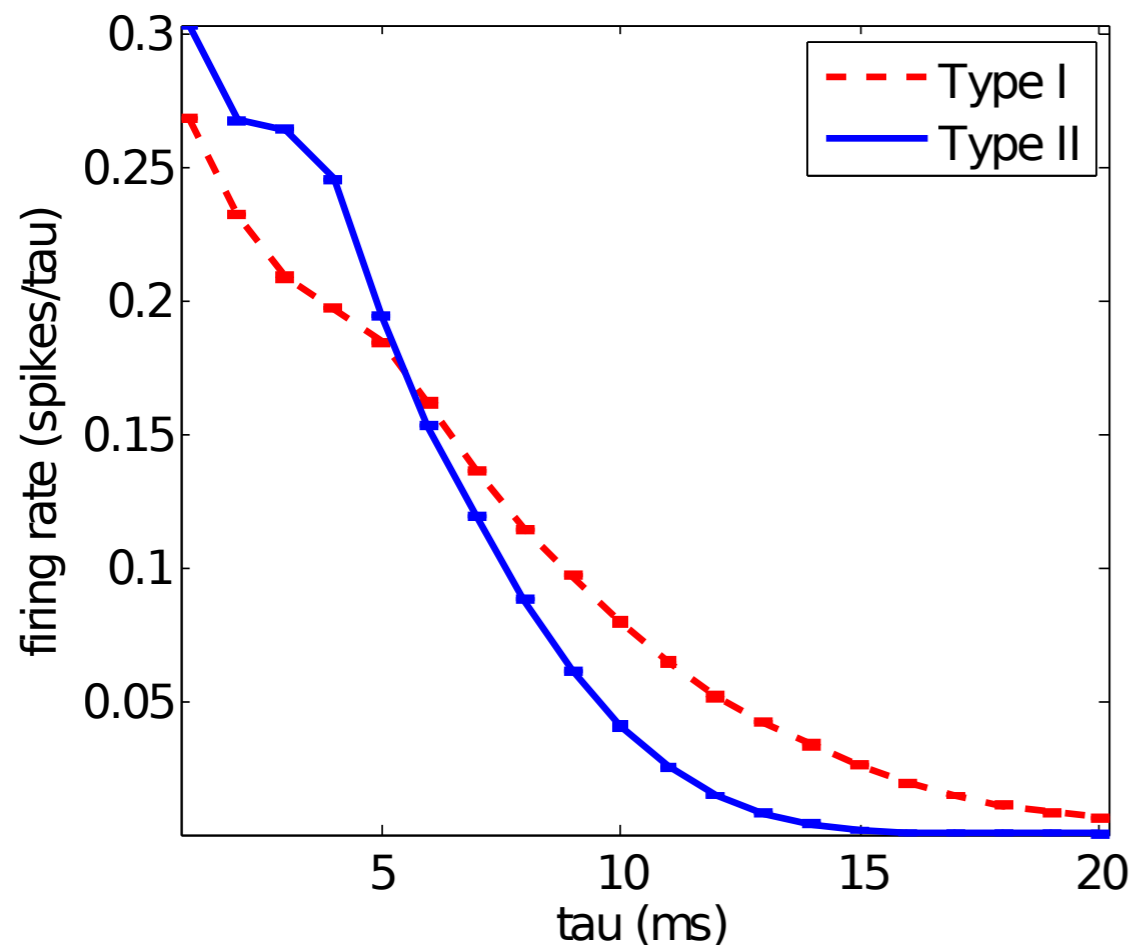
# Modulatory effect seen across upstream operating regimes



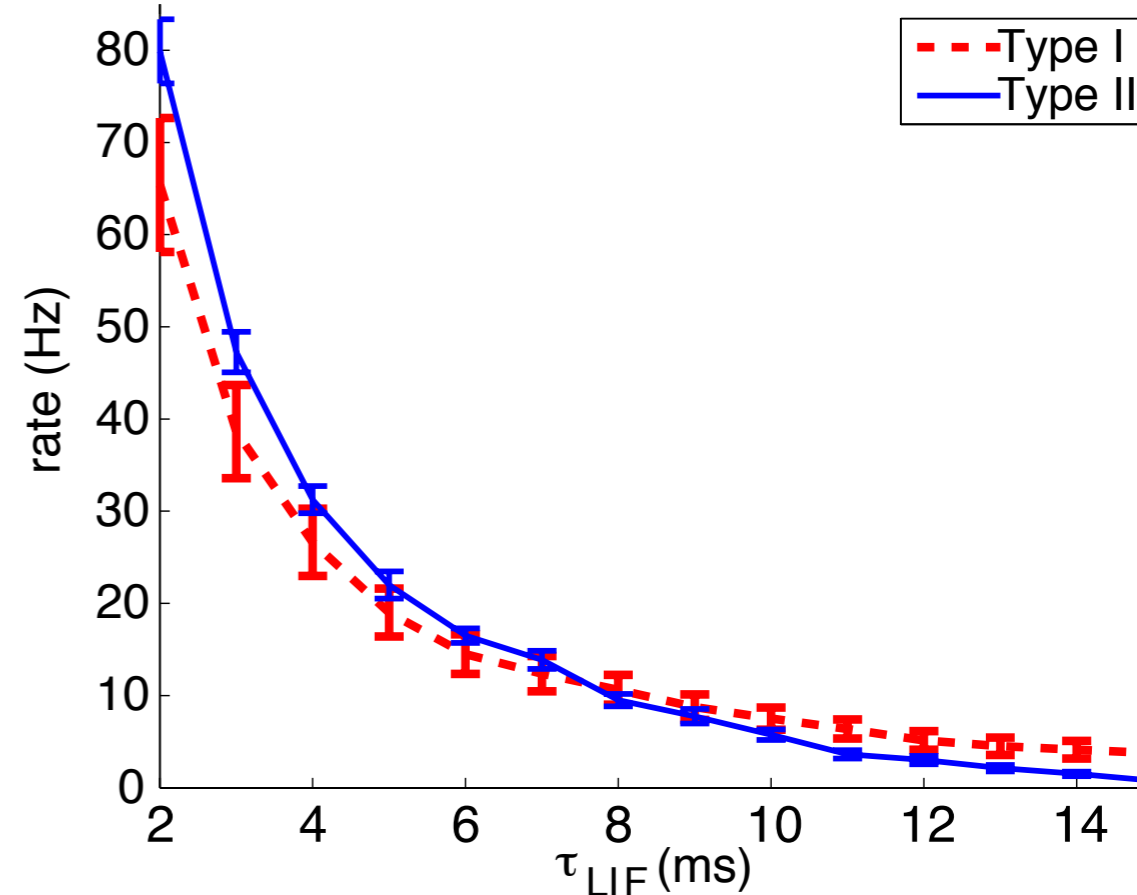
$$\tau \dot{V} = -V + I(t)$$

**Type I/Type II switch occurs at biophysically meaningful timescale:  $\tau \sim 5 - 10$  ms**

Destexhe et al. 2003; Prescott and De Koninck 2009



mean-driven upstream layer



fluctuation-driven upstream layer

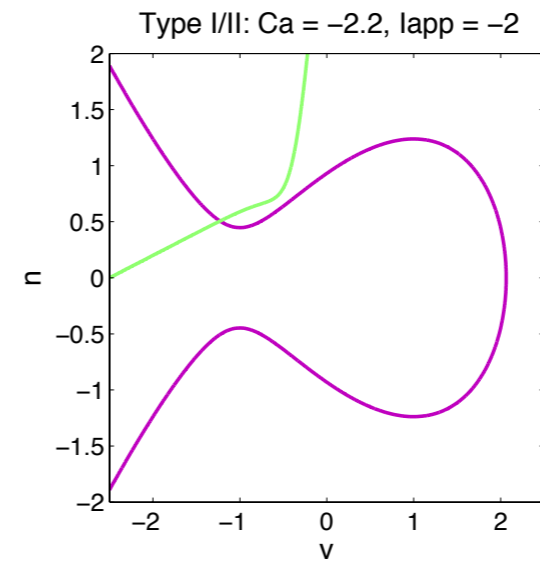
# On-going work: a novel excitability mechanism: “Type IV”

$$\dot{V} = \frac{1}{\epsilon_V} \left( V - V^3/3 + 2/3 - n^2 - z + I_{app} \right)$$

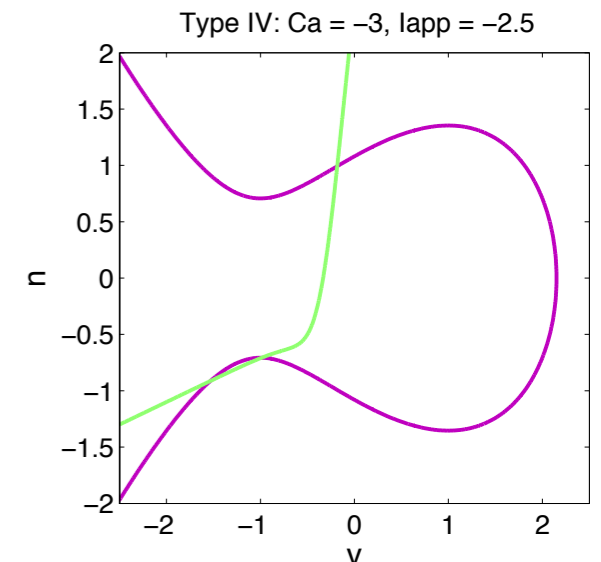
$$\dot{n} = \epsilon_n \left( k_m (V - V_0) \left( 1 + \frac{a}{1 + e^{(4k/a)(V_0 - V + 0.2)}} \right) + n_0 - n \right)$$

$$\dot{z} = \epsilon_{Ca} \left( \frac{k}{1 + e^{-5(V - a_{Ca})}} - 3 - z \right); \quad \epsilon_{Ca} \ll \epsilon_n$$

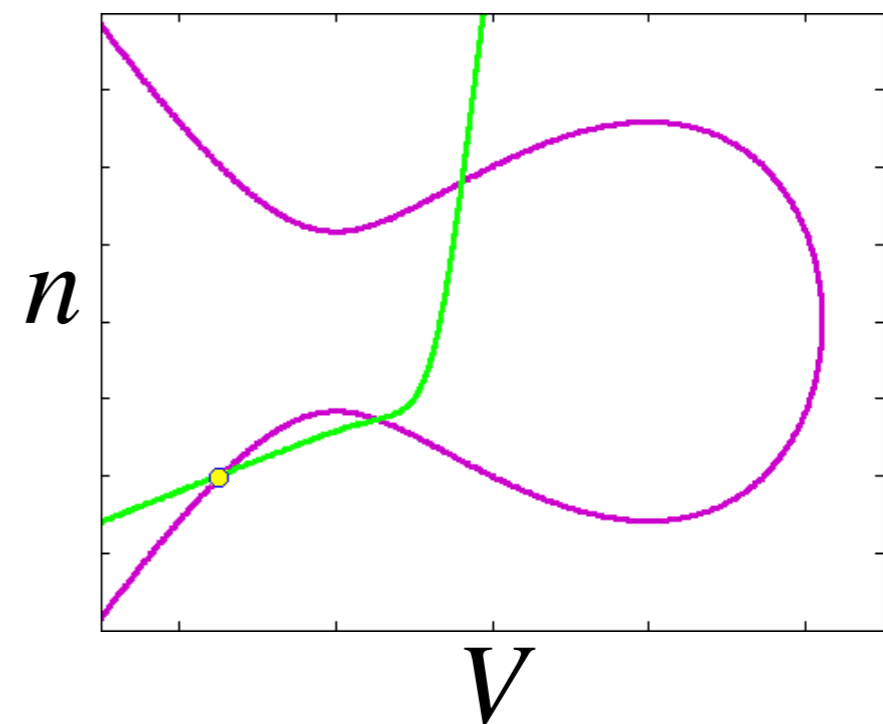
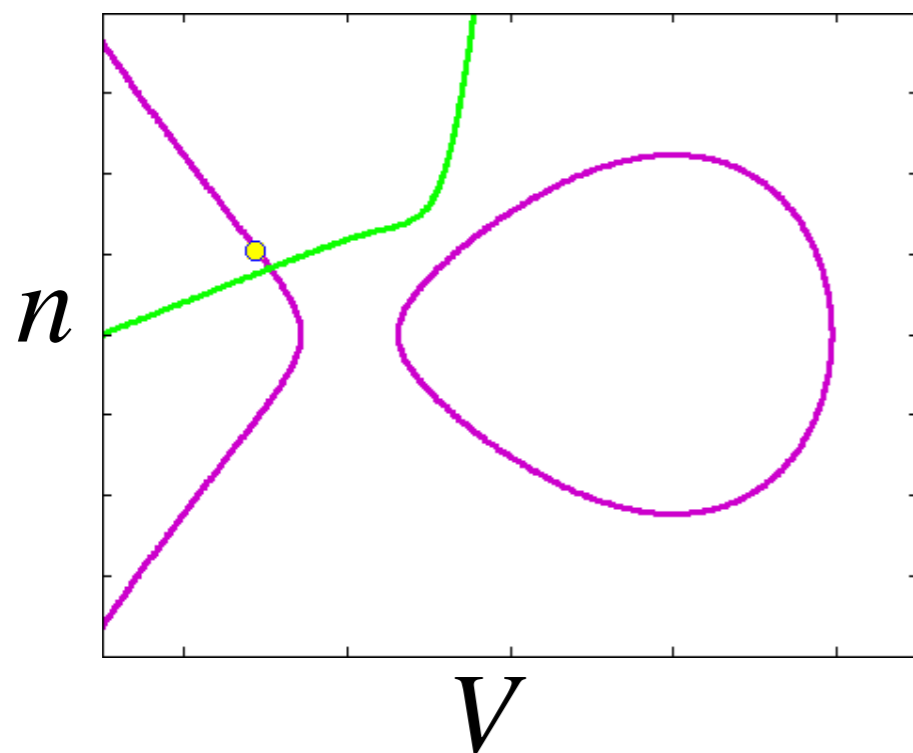
Similar to models in:  
 Franci et al. *PLoS One* 2012;  
 Drion et al. *PLoS Comp Bio* 2012



**Type I/II**  
 ( $n_0 = 0.8$ )



**Type IV**  
 ( $n_0 = -0.5$ )



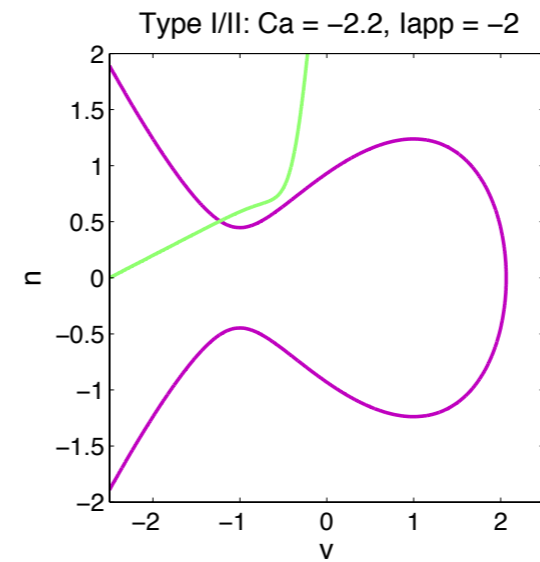
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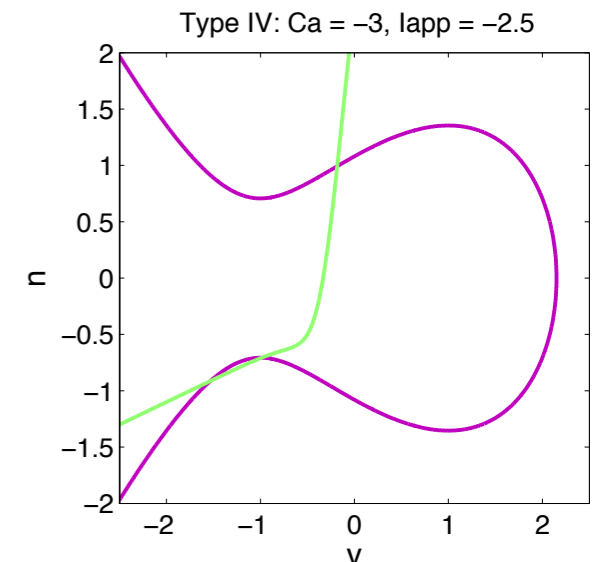
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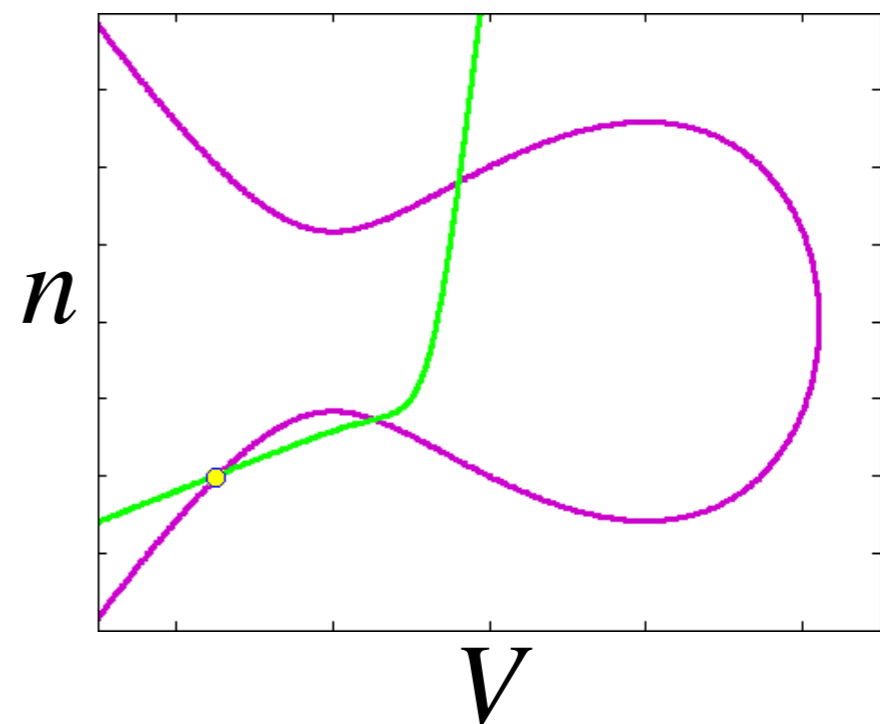
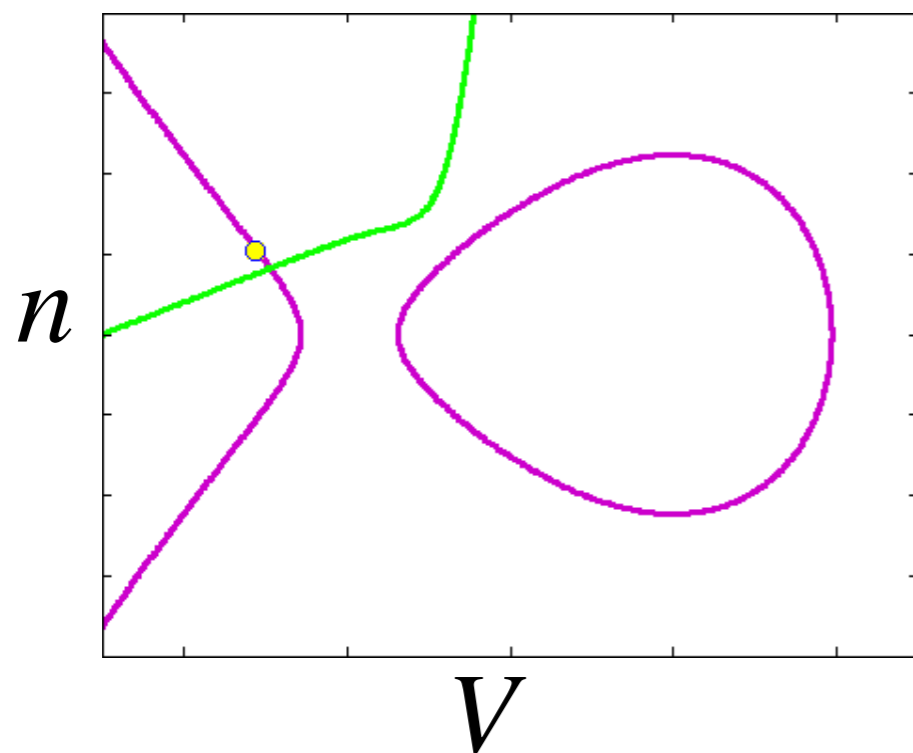
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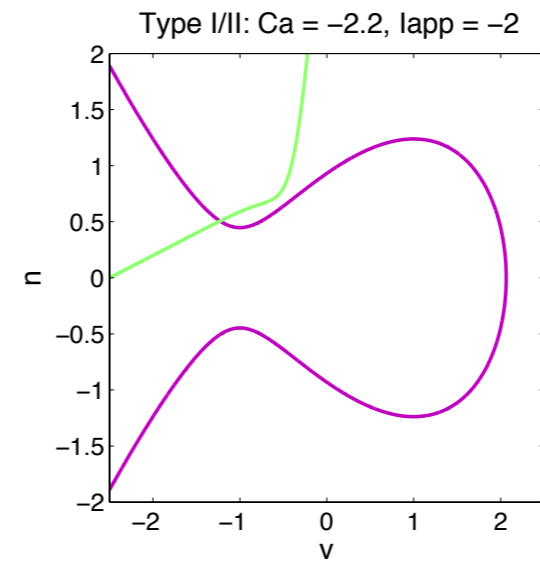
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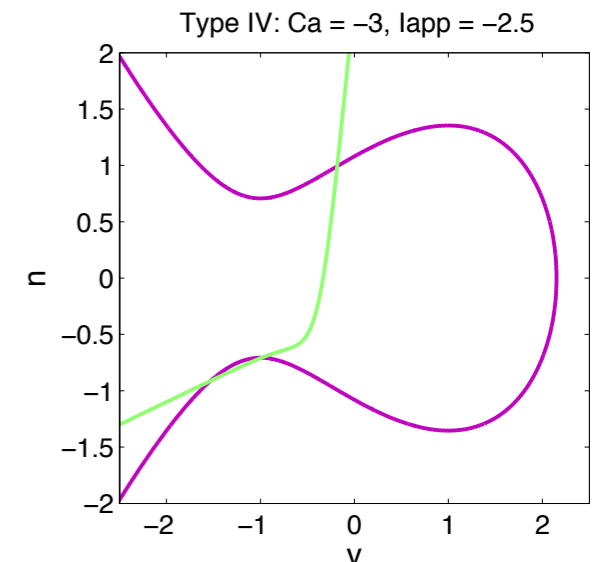
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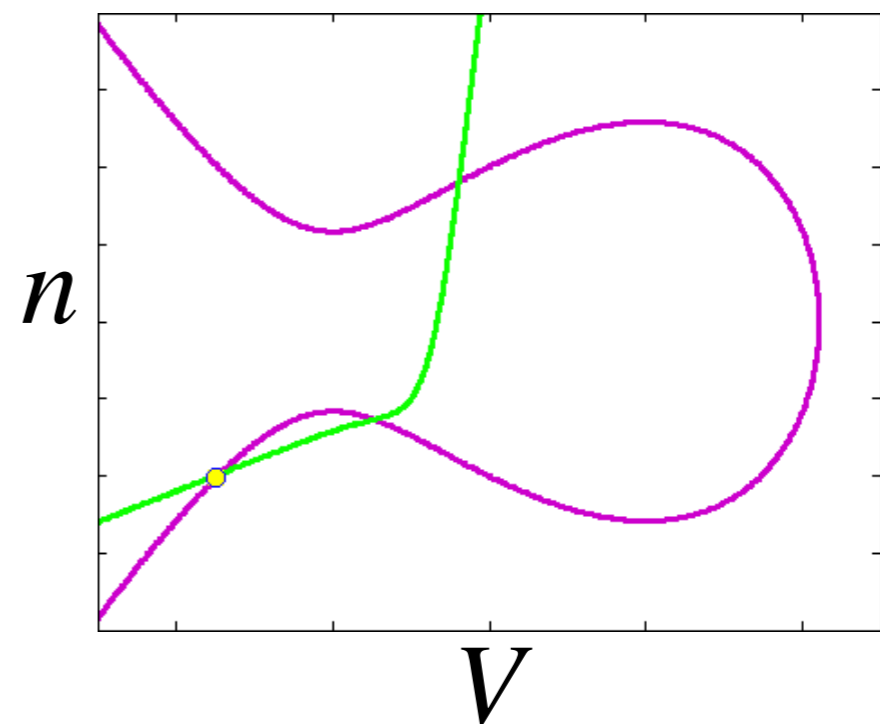
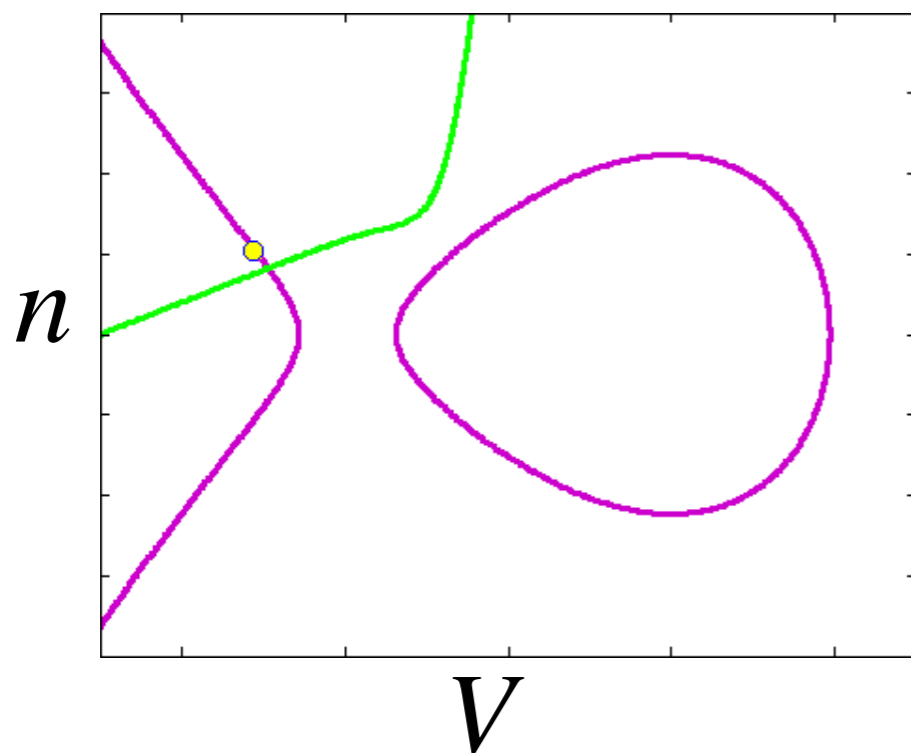
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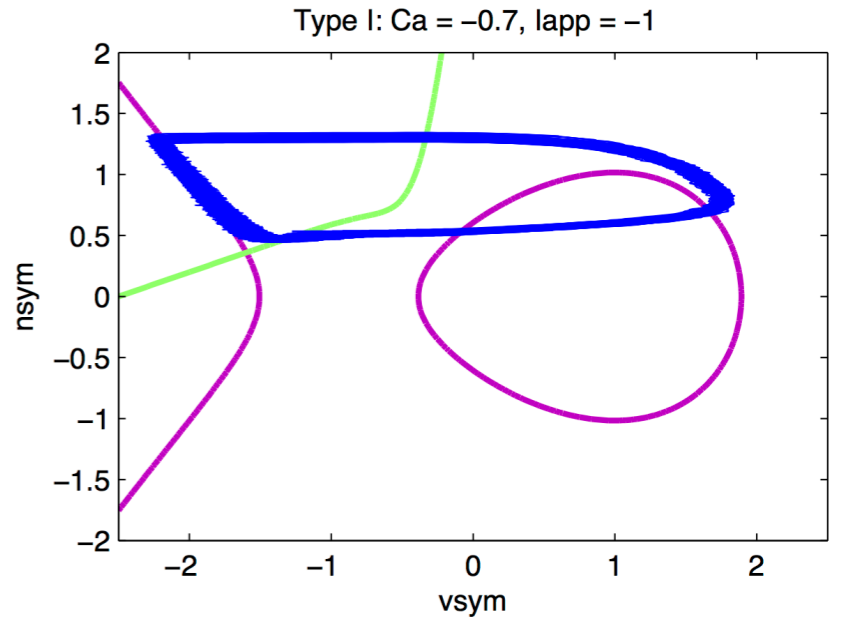
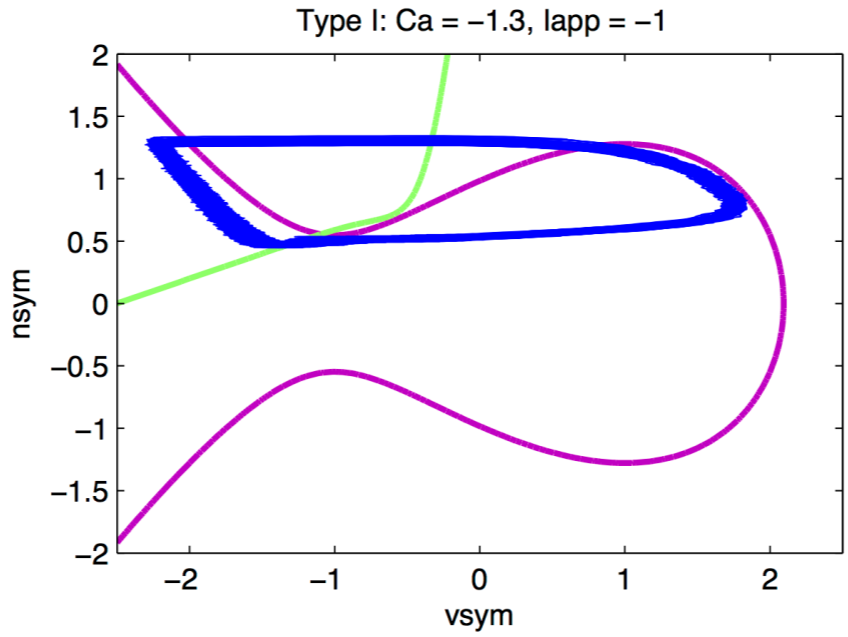
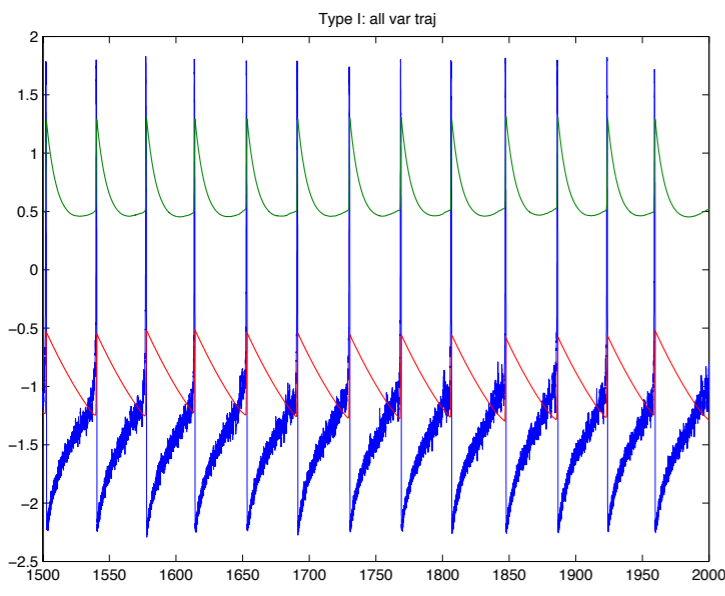


**Type IV**  
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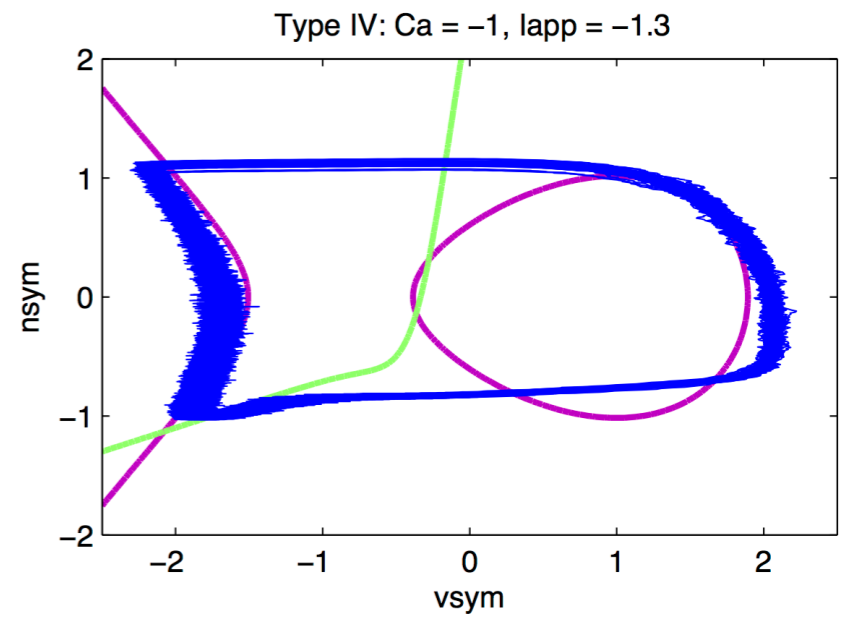
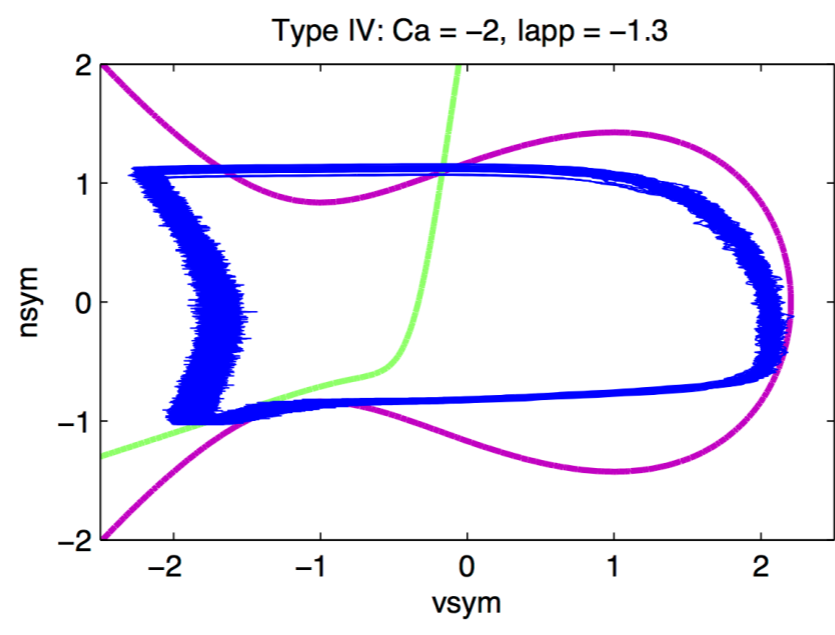
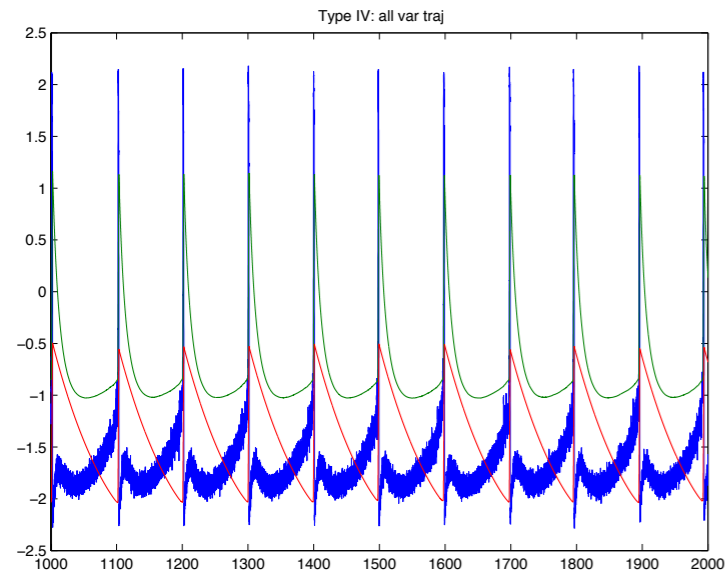


# Effect of lower nullcline branch on spike shape: after-depolarization potentials (ADP)

## Type I/II



## Type IV



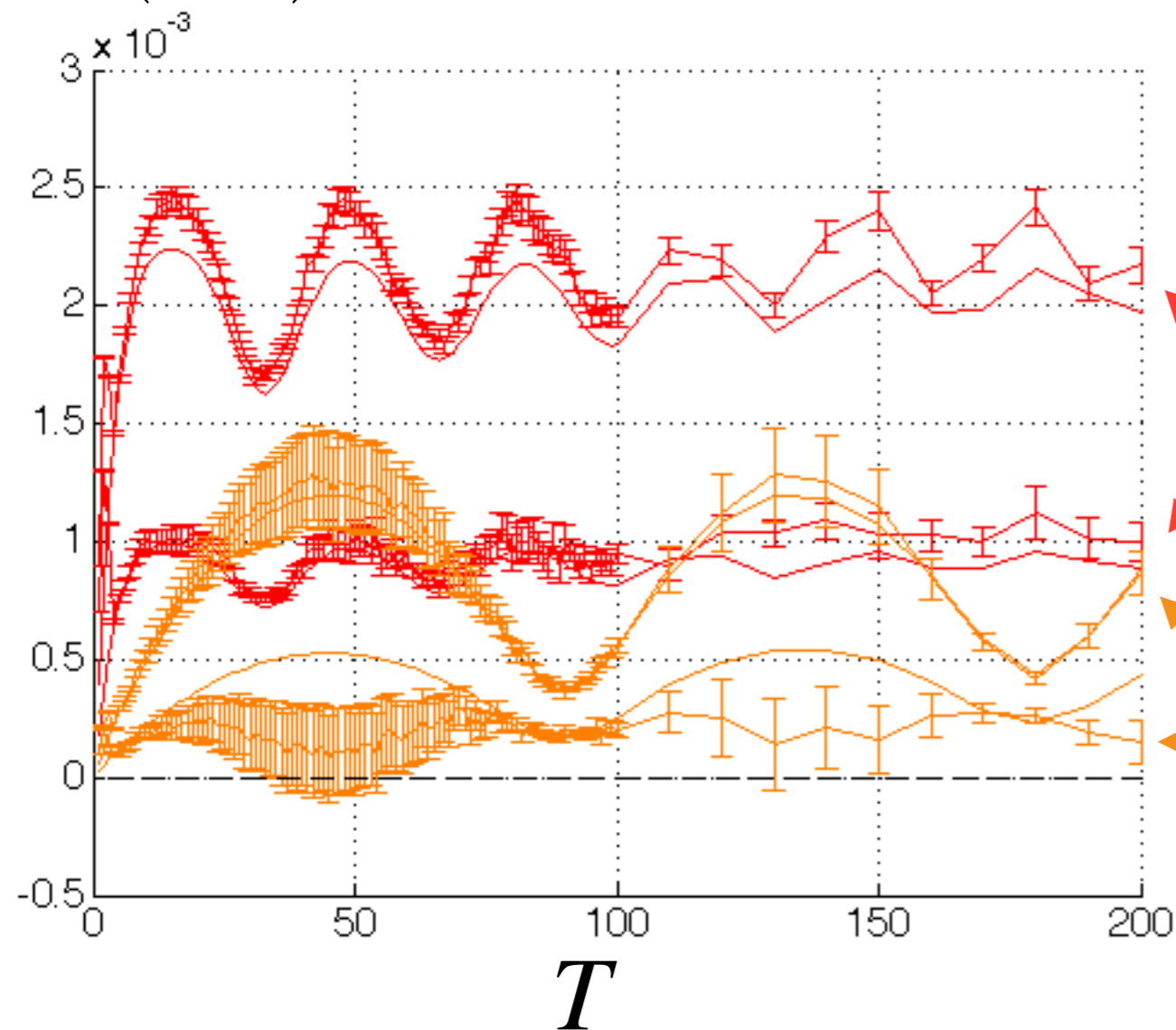
In some cases, the STA effectively predicts covariance

$$Cov_T(n_1, n_2) = T \int_{-T}^T C_{12}(t) \left(1 - \frac{|t|}{T}\right) dt$$

$$C_{12}(t) \propto c(K * \tilde{K})(t);$$

$$K(t) = STA(t), \tilde{K} = STA(-t)$$

$Cov_T(n_1, n_2)$



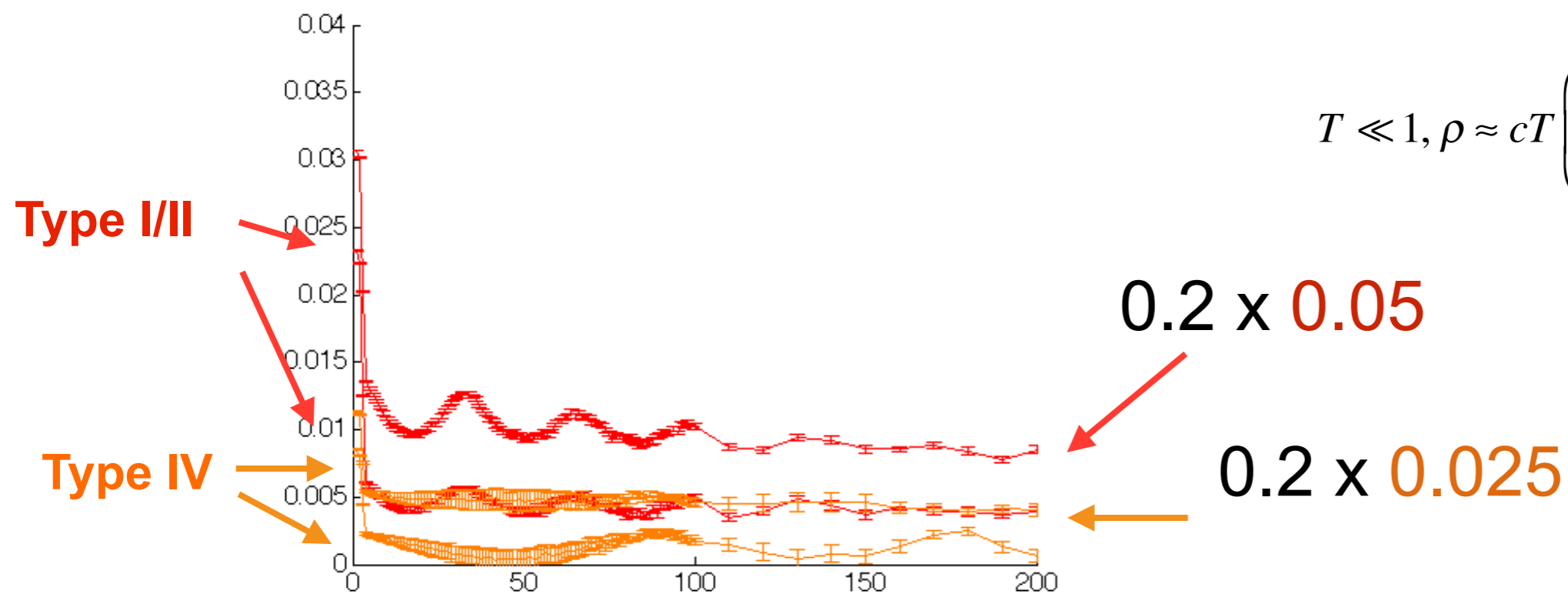
**Type I/II**

**Type IV**

What about  $\rho_T$ ?

$$T \gg 1 \rightarrow \rho_T \approx c \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} = cS$$

$$T \ll 1, \rho \approx cT \left( 1 - \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} \right) = cT(1-S)$$



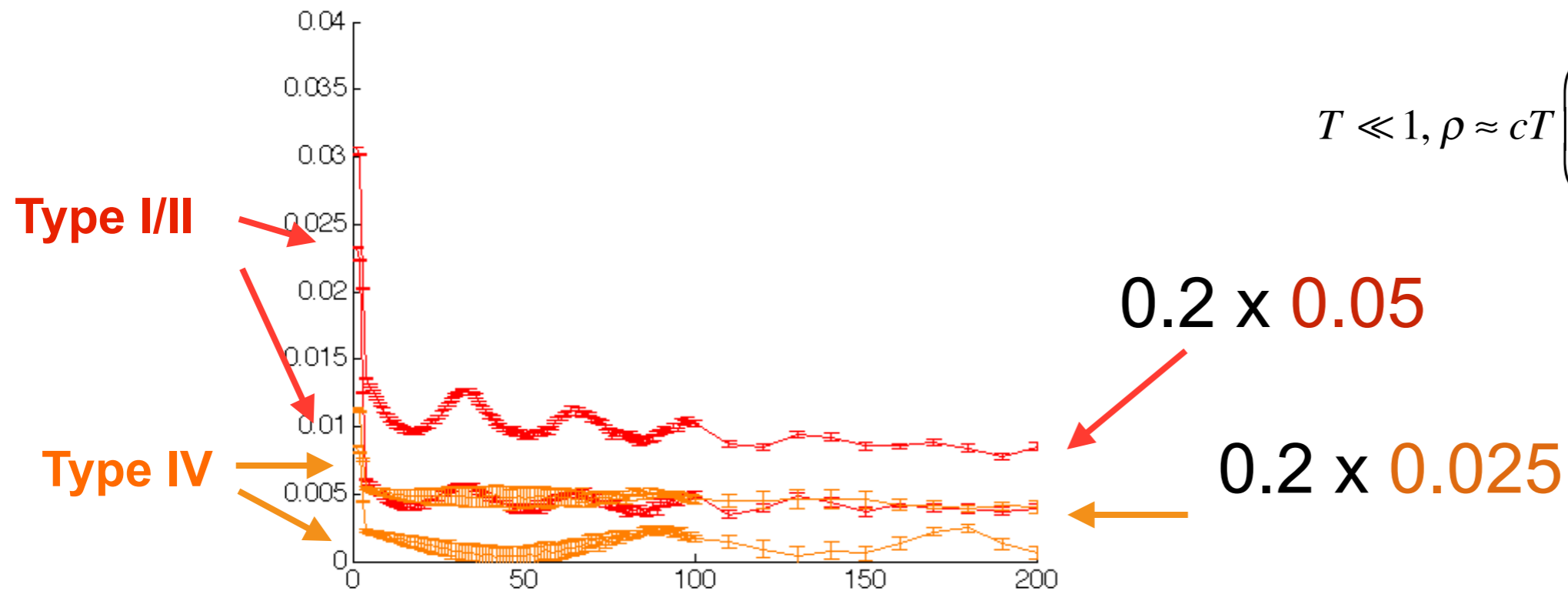
Very low correlation transfer (5%, 2.5% respectively)



What about  $\rho_T$ ?

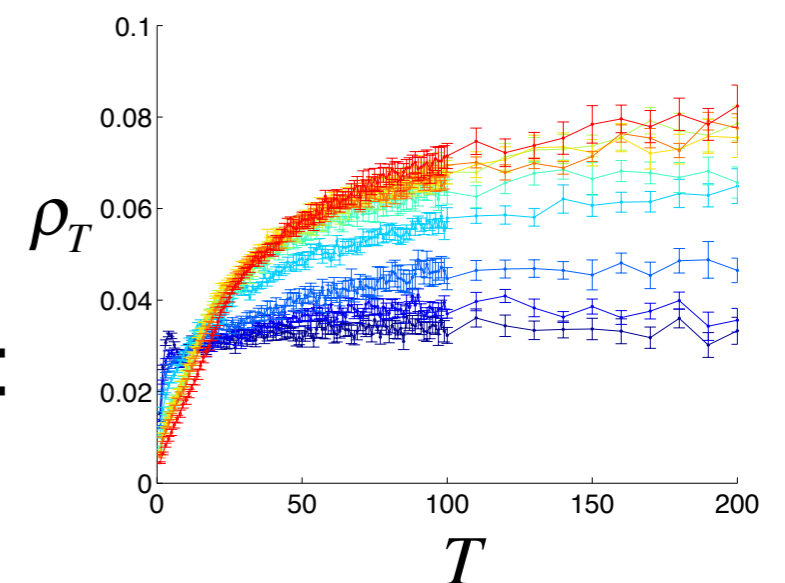
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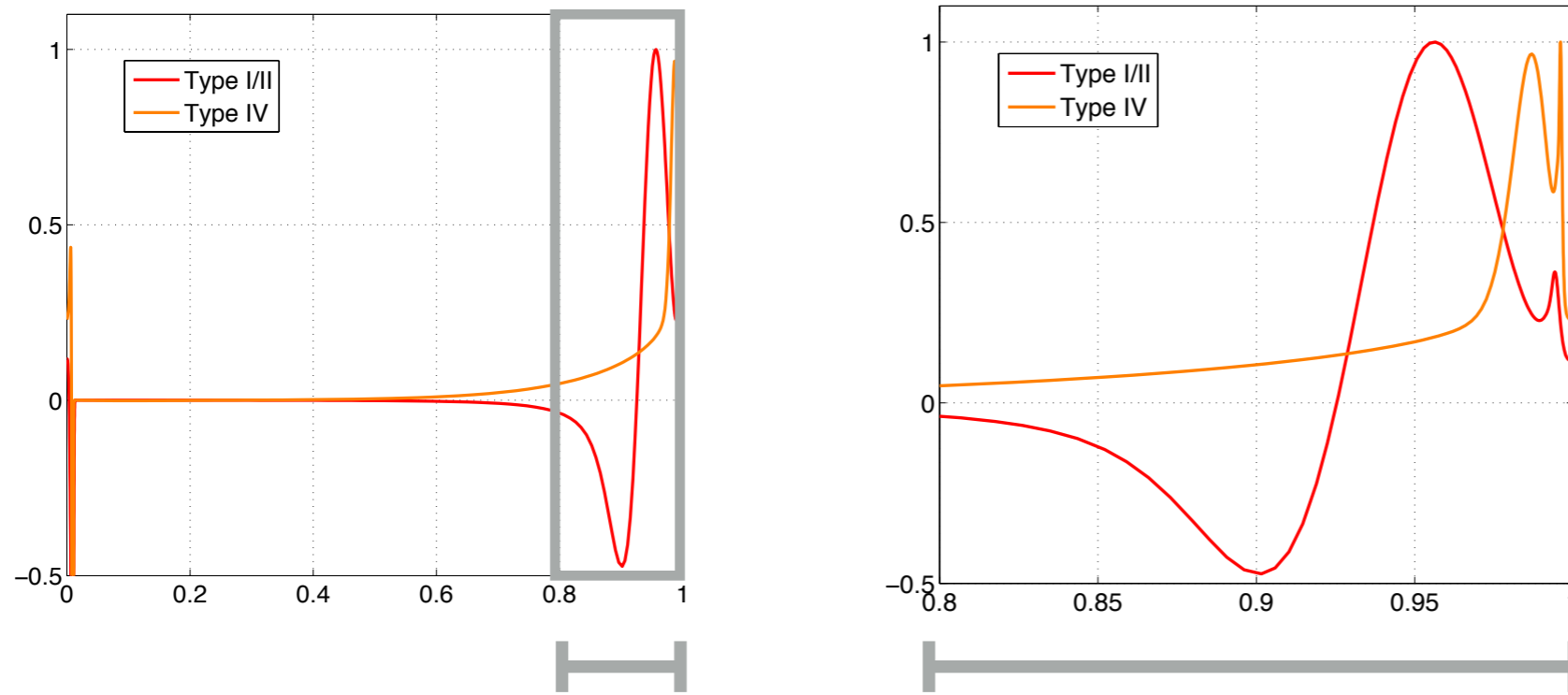


Very low correlation transfer (5%, 2.5% respectively)

(compare to CS:  
40-80%)



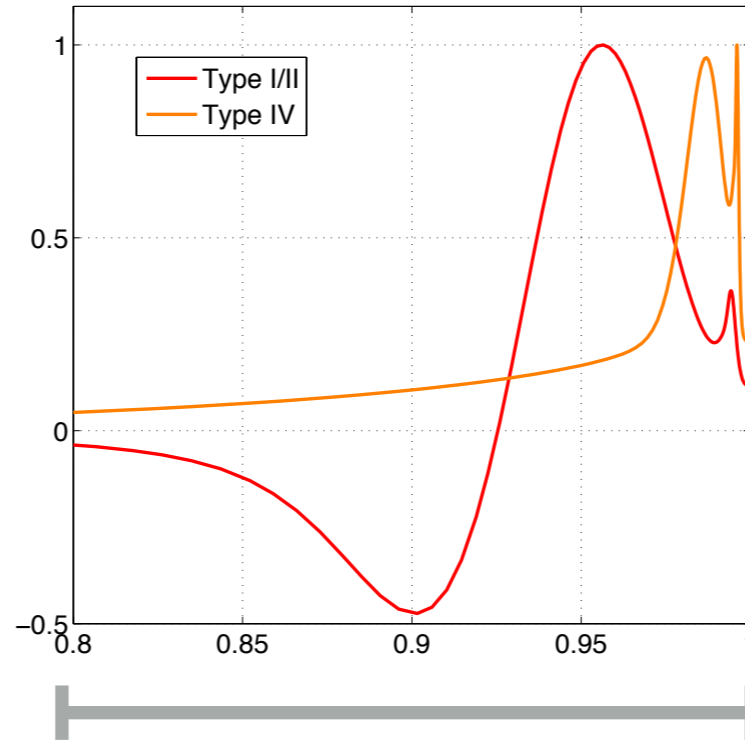
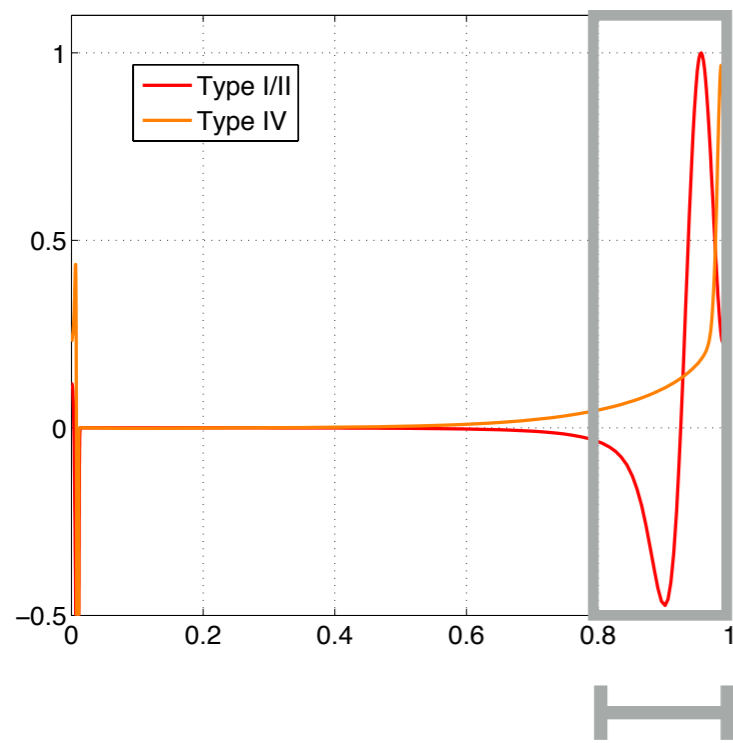
Hypothesis: for systems with strong time scale separation, limited-support PRC  $\Rightarrow$  low  $\rho_T$



$$Z(x) = \begin{cases} \hat{Z}\left(\frac{x}{\epsilon}\right), & 0 \leq x < \epsilon \\ 0, & \epsilon < x < 1 \end{cases}$$

$$\rho_Z = c \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} = c\epsilon \frac{\langle \hat{Z} \rangle^2}{\langle \hat{Z}^2 \rangle} = \epsilon \rho_{\hat{Z}}$$

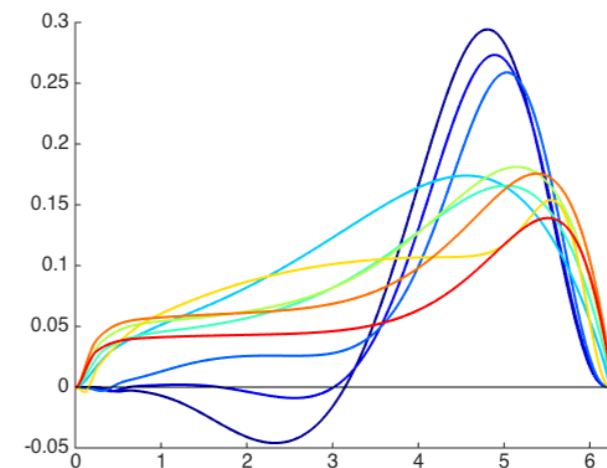
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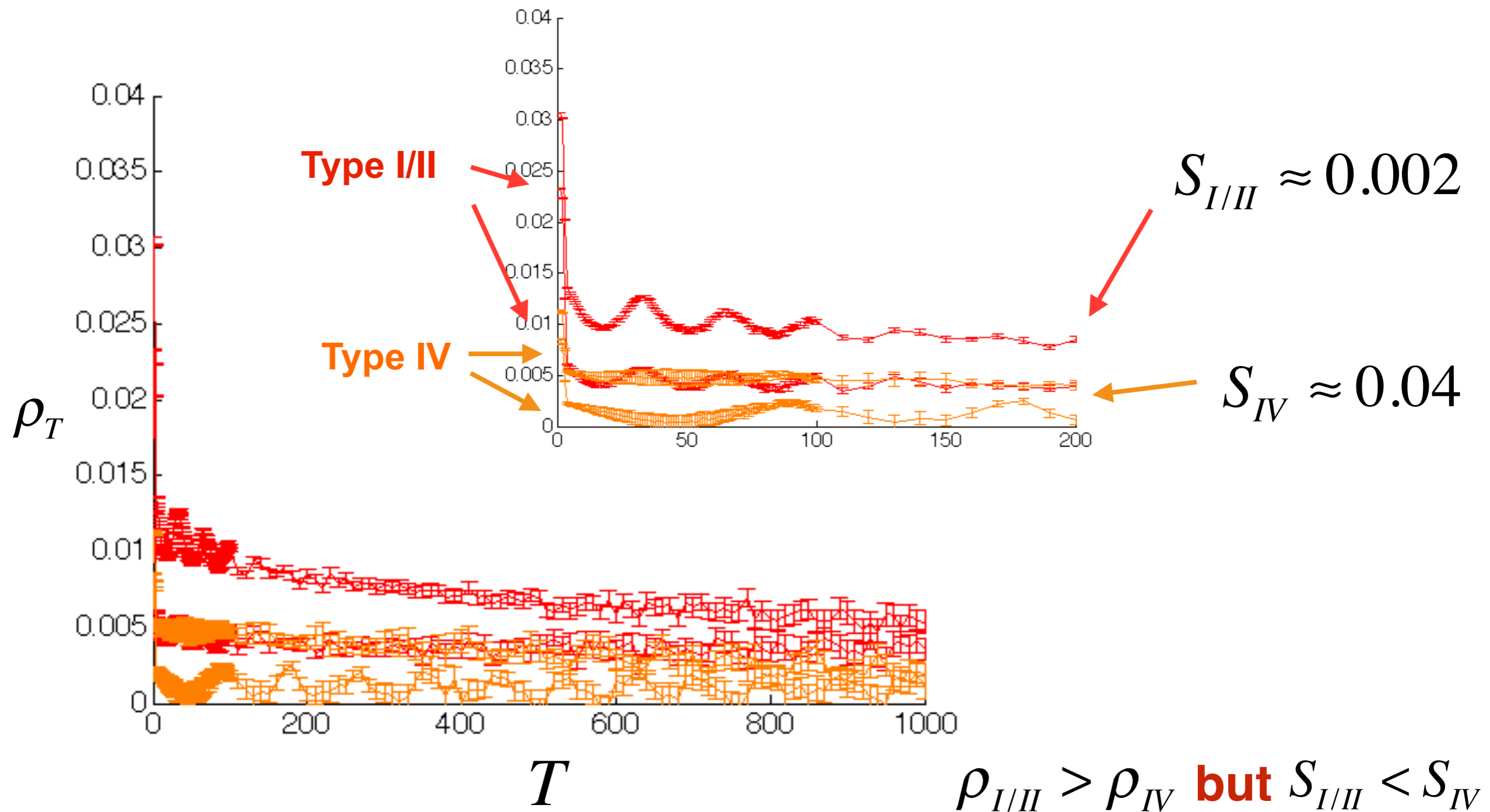
(compare w/ CS:)



# Is the PRC prediction accurate?

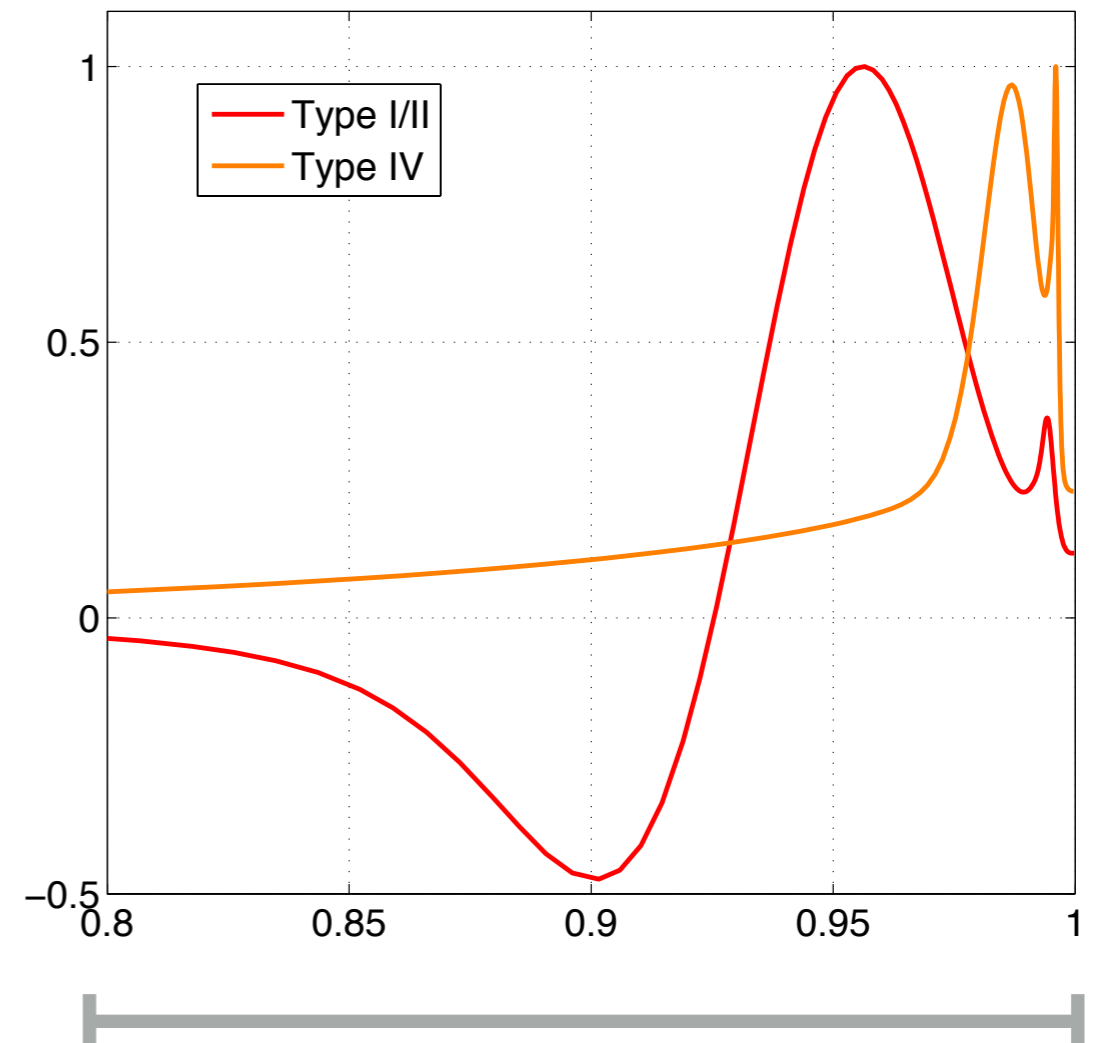
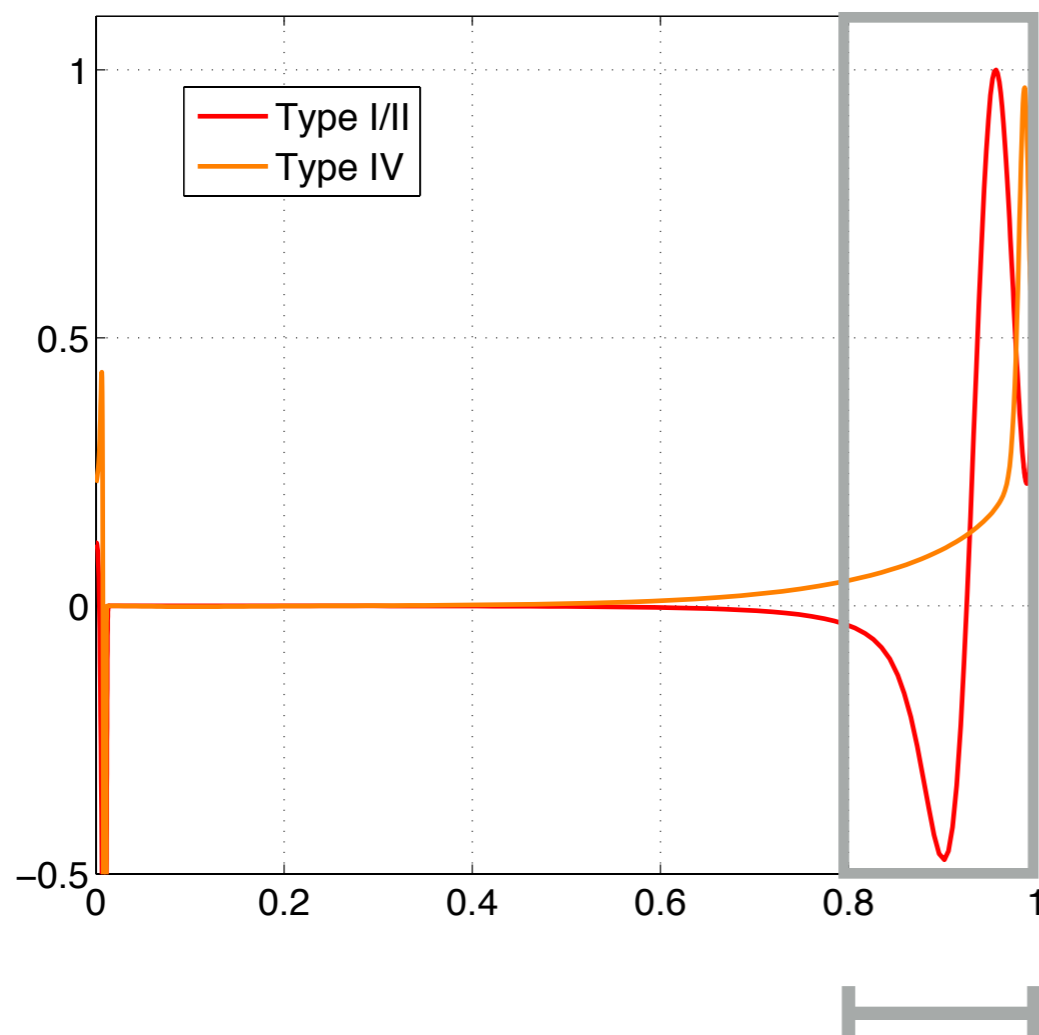
$$T \gg 1 \rightarrow \rho_T \approx c \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} = cS$$

$$T \ll 1, \rho \approx cT \left( 1 - \frac{\langle Z \rangle^2}{\langle Z^2 \rangle} \right) = cT(1-S)$$



## Possible issues:

- relaxation oscillator with strong time scale separation: insensitive to noisy current except at specific times in cycle
- very hard to get long  $T$  statistics
- very hard to get *joint* statistics
- How long is long enough (for  $T$ )?



# In Conclusion

- We study common input correlation transfer in both conductance-based (Connor-Stevens) and phase-oscillator models, focusing on the transition from Type I to Type II neural dynamics
- Type II neurons are more correlated at short time scales, but Type I neurons are more correlated at long time scales.
- The Type I/Type II transition can modulate downstream firing rate at biophysically relevant timescales
- Common input spike-triggered average methodology generalizes well to other excitability types (Type IV)
- PRC-based predictions less accurate: more study needed in relaxation oscillators

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- NSF Grant DMS-0817649, CAREER DMS-1056125
- Burroughs-Wellcome Fund
- NSF Teragrid allocation TG-IBN090004
- Mathematical Biosciences Institute (Early Career Award)