

Urban Welfare: Tourism in Barcelona

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New Wave of Urban Research

A. New generation of **urban spatial equilibrium models** (Ahlfeldt *et al.* , 2015; Allen & Arkolakis, 2016)

- Structural counterfactuals at a high resolution
- ... but restrictive parametric assumptions and/or structural estimation

B. New generation of **urban data**

- Urban economic activity can be observed in unprecedented detail
 - Mobility, expenditure, income networks (cellphone, banks, apps)
 - ... but hard to implement tractable and informative empirical analysis
-
- Welfare effects of an urban shock...

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- Welfare effects of an urban shock...
 - ... in a tractable way without parametric assumptions or structural estimation?

This Paper: A method to estimate welfare effects of urban shocks

1. Both simple and general:

- Simple: Regression based framework
- General: No parametric assumptions necessary

2. Based on two insights:

- Envelope results from residents' optimal (spatial) cons & commuting patterns
⇒ Intuitive **analytical expression for intra-city welfare**
- Perturbation of market clearing identifies **heterogeneous effects** & **GE spillovers**

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3. Apply methodology to estimate welfare effect of tourism in Barcelona:

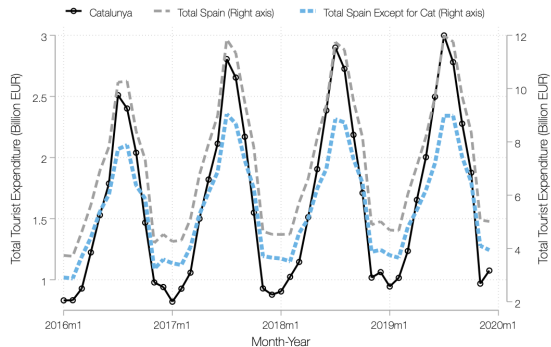
- Rich new data on expenditure and income spatial patterns
- Causal (shift-share) identification from variation in vacation timing in RoW

Tourism as an Urban Shock

- Large part of the economy
 - 7% of world exports
 - 330 million jobs
 - Spain: 11% of GDP

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 - BCN: 200% seasonal \uparrow within year



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- Growing, especially in cities
 - BCN: 25% secular \uparrow in past 5 yrs
 - BCN: 200% seasonal \uparrow within year
- Unequal welfare gains



Key Findings

1. Methodological

- Simple reduced form approach has problems (Aggr. bias + SUTVA violation)
- Incorporating theory-predicted heterogeneity and spillovers identifies het effects
- Predictions close to those from full structural model

2. Impact of tourism

- Median resident not substantially affected by (seasonal changes in) tourism...
- ...but there is substantial heterogeneity with winners and losers

Literature

Urban Quantitative Spatial Economics

- Ahlfeldt *et al.* (2015), Monte *et al.* (2018), Allen & Arkolakis (2016), Heblich *et al.* (2020)

Big Data Spatial Economics

- Athey *et al.* (2020), Couture (2016), Couture *et al.* (2020), Davis *et al.* (2019), Agarwal *et al.* (2017), Miyauchi *et al.* (2021), Kreindler & Miyauchi (2021)

Impact of Tourism

- Almagro & Domínguez-lino (2019), García-López *et al.* (2019), Faber & Gaubert (2019)

First-Order Impact of Price Shocks

- Deaton (1989), Kim & Vogel (2020), Atkin *et al.* (2018), Baqaee & Burstein (2021)

Small shocks in general equilibrium

- Allen *et al.* (2020), Baqaee & Farhi (2019), Kleinman *et al.* (2020), Porto (2006)

Outline of Talk

A General Methodology for (small) Urban Shocks

Intra-city Patterns of Consumption & Income

Empirical Strategy and Identification

Welfare Effects Across the City

Comparison with a Quantitative Model

Conclusion

An Envelope Result for the Welfare effects of Small Shocks

- Arbitrary discrete urban geography: N blocks, each with resident(s) and firm(s).
- Resident of block $n = 1, \dots, N$ chooses goods $i = 1, \dots, N$ to (spatially) consume.

$$u_n = \frac{v_n}{G(\mathbf{p}_n)}$$

- homothetic preferences
- v_n is disposable income of representative agent in block n
- $G(\cdot)$ is a price aggregator
- \mathbf{p}_n refers to the set of transport-cost and amenity adjusted prices

An Envelope Result for the Welfare effects of Small Shocks

- Supplies labor (spatially) to maximize income.

$$v_n = \max_{\{\ell_i\}} \sum_{i=1}^N w_i \ell_i \quad \text{s.t.} \quad H_n(\ell_n) = T_n$$

- T_n is the time endowment in location n scaled by population size
- $H_n(\cdot)$ is a convex function that reflects congestion costs in commuting
- ℓ_n is the vector of commuting cost adjusted labor supply

Roys Identity for Labor Supply

Intuitive analytical expression for intra-city welfare analysis

Theorem (Welfare Effect of a (small) Shock)

Consider a representative local residing in block n . Applying envelope theorem to consumption, production optimization problems yields:

$$d \ln u_n = \underbrace{\sum_i c_{ni} \times \partial \ln w_i}_{\Delta \text{Spatial Income}} - \underbrace{\sum_i s_{ni} \times \partial \ln p_i}_{\Delta \text{Spatial Price Index}}.$$

- Evaluating the welfare effects of an urban shock requires:
 - Income share data $\{c_{ni}\}_{n=1,i=1}^{N,N}$
 - Spatial expenditure data $\{s_{ni}\}_{n=1,i=1}^{N,N}$
 - Estimates of key elasticities: $\{\partial \ln p_i, \partial \ln w_i\}_{i=1}^N$

Heterogeneous Effects & GE Spillovers

Consider an external **expenditure shock** E^T to a city

- Goods market clearing in location i :

$$y_i = \sum_{n=1}^N s_{ni} v_n + s_i^T E^T$$

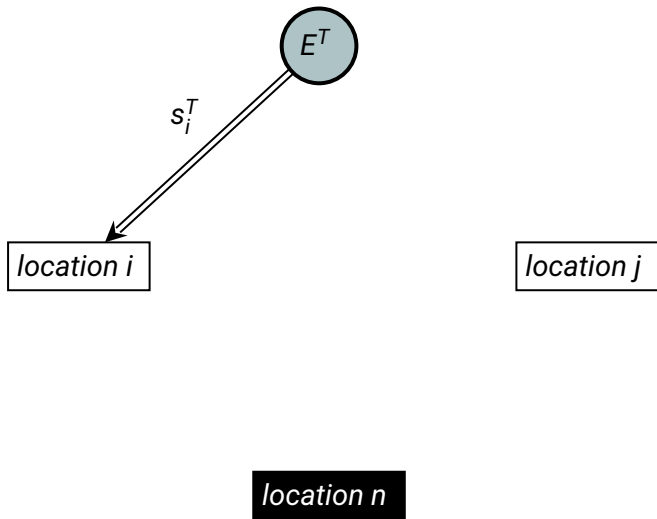
- Labor market clearing in location i :

$$\frac{w_i l_i}{\theta_i^\ell} = \sum_{n=1}^N s_{ni} v_n + s_i^T E^T$$

- where θ_i^ℓ is the output elasticity to labor

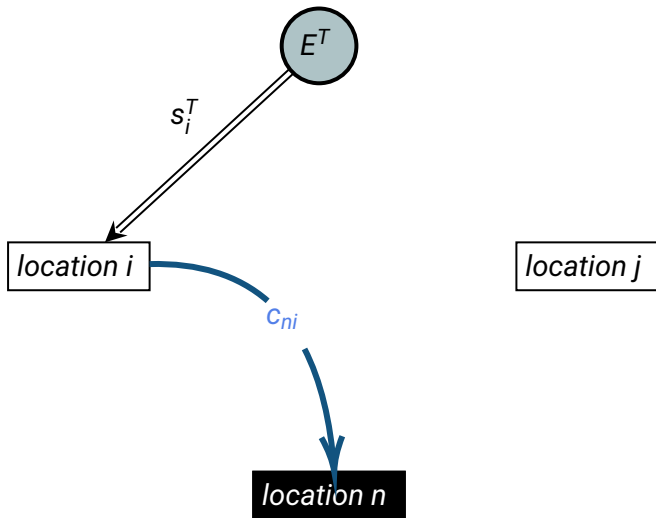
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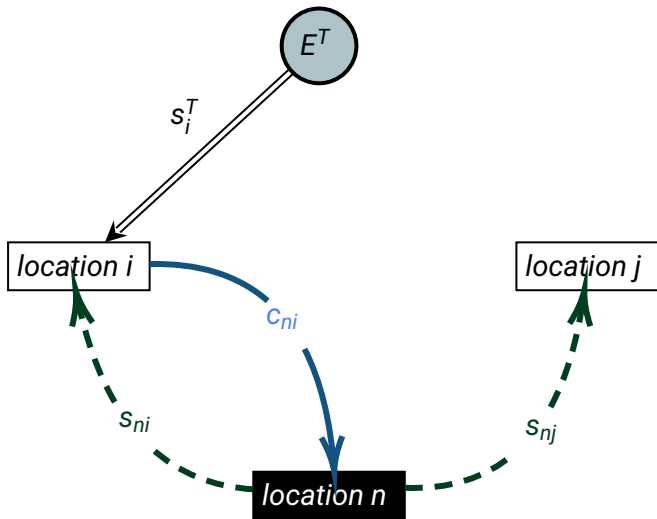
Heterogeneous Effects & GE Spillovers

Consider an external **expenditure shock** E^T to a city \rightarrow **Income Shock**



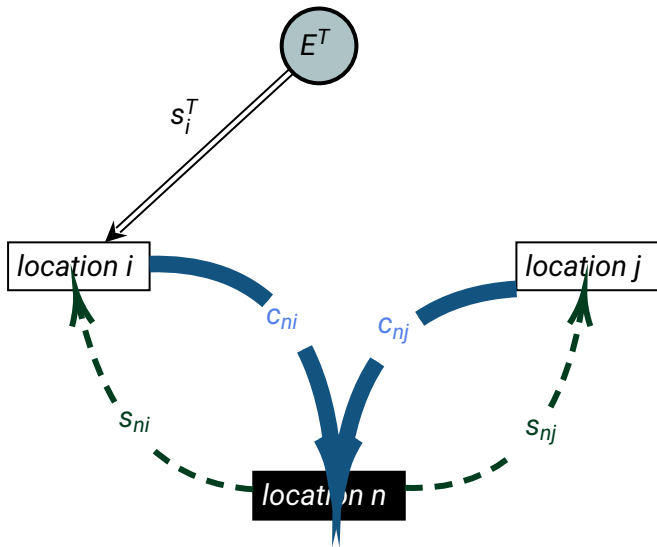
Heterogeneous Effects & GE Spillovers

Consider an external **expenditure shock** E^T to a city \rightarrow **Income Shock** \rightarrow **Demand**



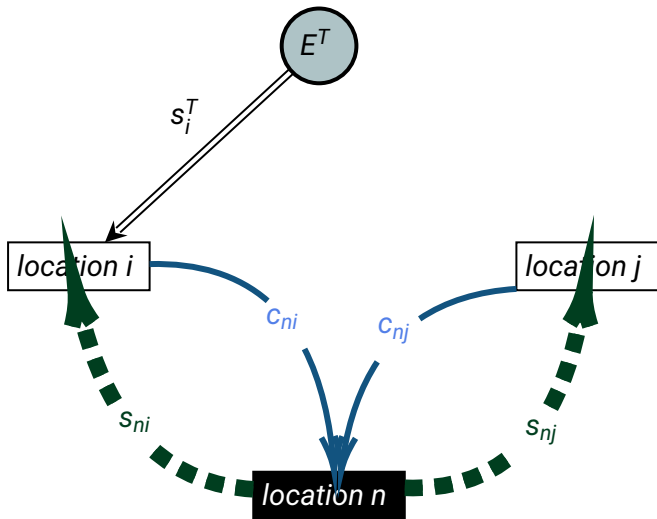
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Consider an external **expenditure shock** E^T to a city \rightarrow **Income Shock** \rightarrow **Demand** \rightarrow **Income Shock**



Heterogeneous Effects & GE Spillovers

Consider an external **expenditure shock** E^T to a city \rightarrow **Income Shock** \rightarrow **Demand** \rightarrow **Income Shock** \rightarrow **Demand**



Heterogeneous Effects & GE Spillovers

- **Direct Effect:**

- Expenditure shock increases prices/wages \propto to its expenditure share in that location

- **Indirect Effect:**

- Increases prices/wages by increasing residential income elsewhere (spatial multiplier)

Heterogeneous Effects & GE Spillovers

Elasticities: Theory Insights

Theorem ('Short Run' Elasticities for Prices and Wages)

Consider an external expenditure shock E^T to a city. Imposing market clearing, keeping expenditure shares and labor allocation constant, we obtain,

$$\frac{\partial \ln p_i}{\partial \ln E^T} = \underbrace{\frac{E_i^T}{y_i}}_{\text{Direct Effect } (\eta_{itm}^{0,T})} + \underbrace{\frac{1}{y_i} \sum_n s_{ni} \times v_n \times \sum_j c_{nj}}_{\text{GE Spillover via Spatial Exp Patterns}} \times \frac{\partial \ln w_j}{\partial \ln E^T}$$

$$\frac{\partial \ln w_i}{\partial \ln E^T} = \underbrace{\frac{E_i^T}{y_i}}_{\text{Direct Effect } (\eta_{itm}^{0,T})} + \underbrace{\frac{1}{y_i} \sum_n s_{ni} \times v_n \times \sum_j c_{nj}}_{\text{GE Spillover via Spatial Exp Patterns}} \times \left(\frac{E_j^T}{y_j} \right) + \dots$$

Heterogeneous Effects & GE Spillovers

- A General Methodology for (small) Urban Shocks
 - Intuitive analytical formula to trace out welfare effects
 - Predictions for heterogeneous and GE effects

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New Generation of High Resolution Urban Datasets

- Working closely with Caixabank, a large Spanish bank based in Barcelona
- First paper to combine:
 1. High resolution bilateral expenditure data.
 2. High resolution residential income data.
 3. High resolution commuting data.

New Generation of High Resolution Urban Datasets

- Expenditure Data:
- Income Data:
- Commuting data:

New Generation of High Resolution Urban Datasets

- Expenditure Data:
 - Source: Account & point-of-sale data covering 165M+ transactions pa
 - Locals: 1095 residential tiles x 1095 cons tiles x 20 sectors x 36 months
 - Tourists: country of origin x 1095 cons tiles x 20 sectors x 36 months
 - January 2017 - December 2019
 - Covers roughly 54.4 pc of total expenditure Comparison: HBS

- Income Data:

- Commuting data:

New Generation of High Resolution Urban Datasets

- Expenditure Data:
- Income Data:
 - Source: Payrolls and UB from over 400k accounts
 - Mean and median income per census tract [Comparison: INE](#) [Map: Income in Barcelona](#)
- Commuting data:

New Generation of High Resolution Urban Datasets

- Expenditure Data:
- Income Data:
- Commuting data: Two sources:
 1. Imputed from expenditures on weekday lunches (Caixa)
 2. Commuting patterns from cell phone locations (INE)

New Generation of High Resolution Urban Datasets

- Expenditure Data:
- Income Data:
- Commuting data:
- Housing prices:
 - Source: Idealista ("Spanish Zillow")
 - House prices and rental rates
 - Monthly frequency for neighborhoods (more aggregated than census blocks)

Three Stylized Facts

1. Tourism varies across space and time within the city
2. Locals' spending and income are spatially determined by residence
3. Tourist spending affects local's spending and incomes

Three Stylized Facts

$$d \ln u_n = \underbrace{\sum_i c_{ni} \times \partial \ln w_i}_{\Delta \text{Spatial Income}} - \underbrace{\sum_i s_{ni} \times \partial \ln p_i}_{\Delta \text{Spatial Price Index}} .$$

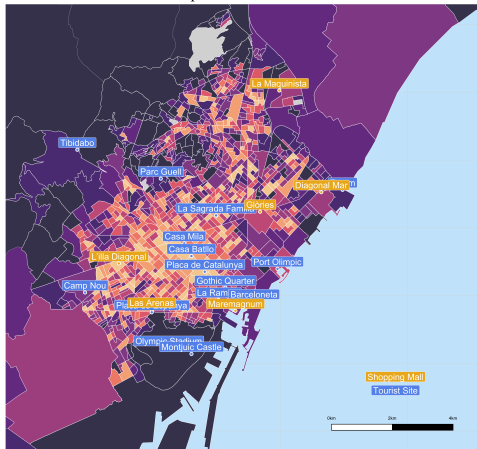
1. **Tourist spending** varies across space and time within the city
 - Provides variation for identification
2. Locals' **spending** and **income** are spatially determined by residence
 - Documents the heterogeneous incidence across space
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 - Prima-facie evidence of the effect of tourism

Three Stylized Facts

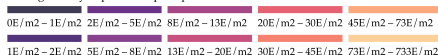
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Fact 1: Tourism varies across space and time within the city

Local Expenditures in Barcelona

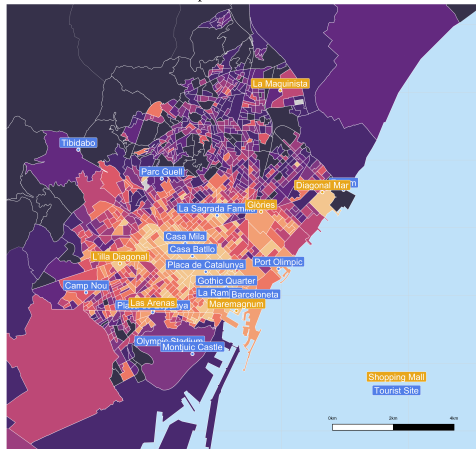


Average Yearly Expenditure per sqm in EUR

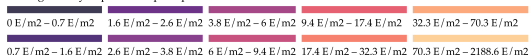


Source: CBRE Research & Analytics (2019)

Tourist Expenditures in Barcelona



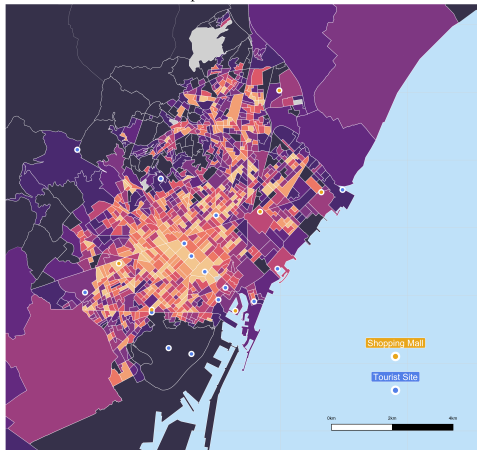
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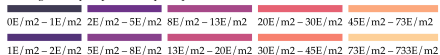
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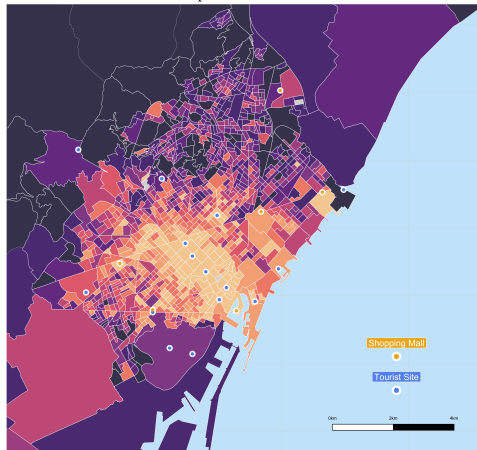


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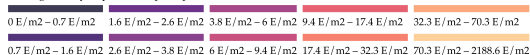


Source: CBRE Future Planning (2019)

Tourist Expenditures in Barcelona



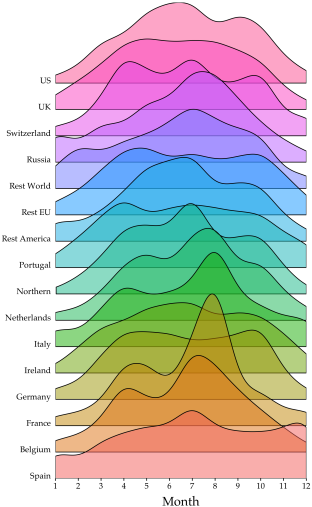
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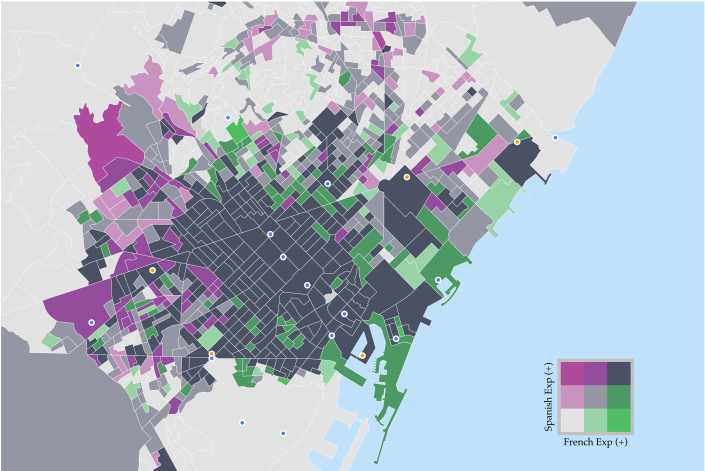
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Fact 1: Tourism varies across space and time within the city

Monthly Expenditure Shares



French vs Domestic Tourists Expenditure Shares

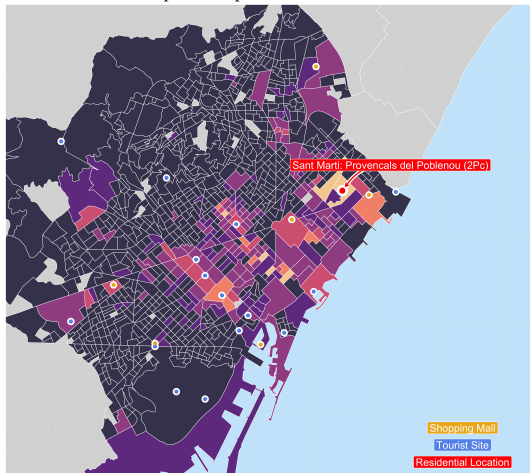


Three Stylized Facts

1. Tourism varies across space and time within the city
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Fact 2: Local Spending & Income is Spatial

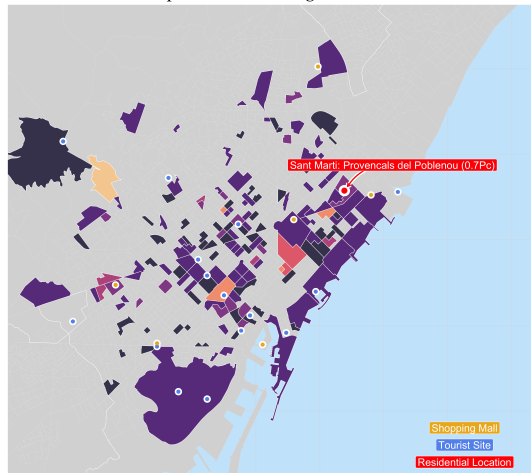
Spatial Expenditure Patterns



Expenditure Share



Spatial Commuting Patterns



Commuting Share

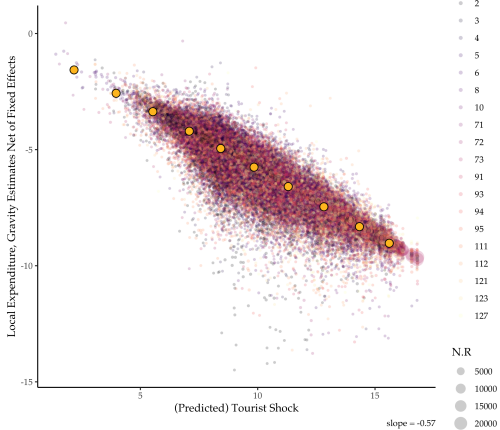
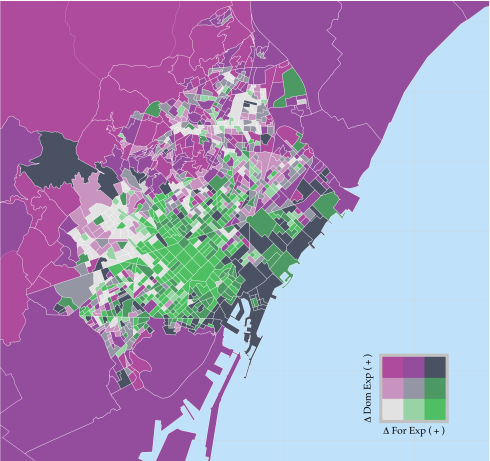


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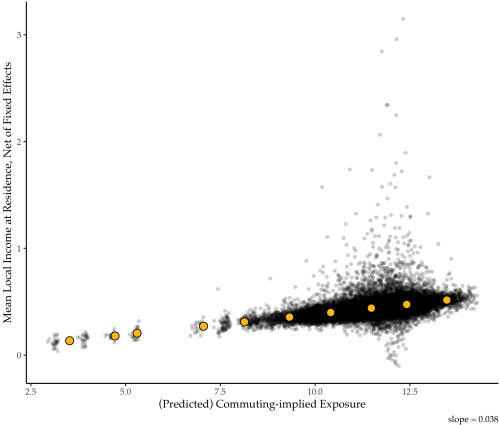
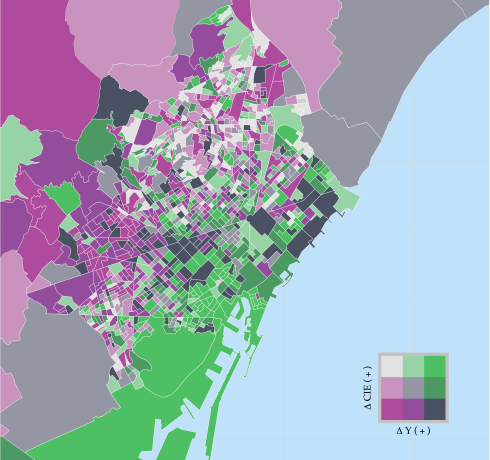
Fact 3: Tourist spending affects local's spending

Δ Local vs Δ Tourist Expenditure (Aug vs Jan)



Fact 3: Tourist spending affects local's incomes

Δ Income vs Δ Commuting Impl Exposure (Aug vs Jan)



Three Stylized Facts

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Empirics

- From Theory to Estimation
- Identification
- Results

From Theory to Estimation

- Welfare Formula

$$d \ln u_n = \underbrace{\sum_i c_{ni} \times \partial \ln w_i}_{\Delta \text{Spatial Income}} - \underbrace{\sum_i s_{ni} \times \partial \ln p_i}_{\Delta \text{Spatial Price Index}}.$$

- Estimates of key elasticities: $\left\{ \frac{\partial \ln p_i}{\partial \ln E_i^T}, \frac{\partial \ln w_j}{\partial \ln E_j^T} \right\}_{i=1}^N$

From Theory to Estimation

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- **Challenges**

- p_{it} includes non-pecuniary effects
- our data: income v_{nt} , not wages w_{it}
- $\ln E_{it}$ not exogenous (everyone likes the beach)

From Theory to Estimation: Step 1

- Recovering amenity-adjusted prices

- From CES preferences

- δ_{it} is the destination fixed effect of a gravity regression:

$$\ln X_{nit} = \ln \delta_{nt} + \ln \delta_{it} + \beta^{dist} \ln travel_time_{nit} + \varepsilon_{nit}$$

- PPML estimated

- Including both prices and non-pecuniary effects of tourism

From Theory to Estimation: Step 1

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- PPML estimated

- Including both prices and non-pecuniary effects of tourism

- Price Regressions (Average Treatment Effect)

$$\ln \delta_{it} = \alpha + \beta^P \times \ln E_{it}^T + \epsilon_{it}$$

From Theory to Estimation: Step 1

- Tourist shock at residential level:
 - **Commuting implied exposure** measures impact of tourism on income

$$\ln C_i E_{ntm}^T = \sum_i c_{ni} \times \ln E_{itm}^T$$

- Derived from income maximization problem [Derivations](#)

From Theory to Estimation: Step 1

- Tourist shock at residential level:
 - **Commuting implied exposure** measures impact of tourism on income

$$\ln \text{CiE}_{ntm}^T = \sum_i c_{ni} \times \ln E_{itm}^T$$

- Derived from income maximization problem [Derivations](#)
- Income Regressions (Average Treatment Effect)

$$\ln v_{nt} = \alpha + \beta^w \times \ln \text{CiE}_{ntm}^T + \epsilon_{it}$$

From Theory to Estimation: Step 1

- Income & Price Regressions (Average Treatment Effect)

$$\ln v_{nt} = \alpha + \beta^w \times \ln C_i E_{ntm}^T + \epsilon_{it}$$

$$\ln \delta_{it} = \alpha + \beta^p \times \ln E_{it}^T + \epsilon_{it}$$

From Theory to Estimation: Step 1

- Income & Price Regressions (Average Treatment Effect)

$$\ln v_{nt} = \alpha + \beta^w \times \ln C_i E_{ntm}^T + \epsilon_{it}$$

$$\ln \delta_{it} = \alpha + \beta^p \times \ln E_{it}^T + \epsilon_{it}$$

- **Challenge**

- Does not take heterog. into account when calculating welfare (Aggregation bias)

From Theory to Estimation: Step 2

- Income & Price Regressions (Heterogeneous Treatment Effect)

$$\ln v_{nt} = \alpha + \beta^w \times \ln \text{Ci}E_{ntm}^T + \beta^{w,het} \times \ln \text{Ci}E_{ntm}^T \left(\eta_{itm}^0 \right) + \epsilon_{it}$$

$$\ln \delta_{it} = \alpha + \beta^p \times \ln E_{it}^T + \beta^{p,het} \times \eta_{itm}^0 \times \ln E_{it}^T + \epsilon_{it}$$

- Variables
 - $\eta_{itm}^0 = E_i^T / y_i$ is the direct effect

From Theory to Estimation: Step 2

- Income & Price Regressions (Heterogeneous Treatment Effect)

$$\ln v_{nt} = \alpha + \beta^w \times \ln \text{CiE}_{ntm}^T + \beta^{w,het} \times \ln \text{CiE}_{ntm}^T \left(\eta_{itm}^0 \right) + \epsilon_{it}$$

$$\ln \delta_{it} = \alpha + \beta^p \times \ln E_{it}^T + \beta^{p,het} \times \eta_{itm}^0 \times \ln E_{it}^T + \epsilon_{it}$$

- **Challenge**

- Abstracts from GE spillover effects (SUTVA violation)

From Theory to Estimation: Step 3

- Income & Price Regressions (HTE and Controlling for GE Spillovers)

$$\ln v_{nt} = \alpha + \beta^w \times \ln \text{Ci}E_{ntm}^T + \beta^{w,het} \times \ln \text{Ci}E_{ntm}^T \left(\eta_{itm}^0 \right) + \epsilon_{it}$$

$$\ln \delta_{it} = \alpha + \beta^p \times \ln E_{it}^T + \beta^{p,het} \times \eta_{itm}^0 \times \ln E_{it}^T + \beta^{p,GE} \times \eta_{itm}^{0,Res} \times \log E_{itm}^{T,GE} + \epsilon_{it}$$

- Variables

- $\ln E_{ntm}^{T,GE} \left(\eta_{itm}^0 \right) = \sum_n \mathbf{s}_{ni} \times \widehat{\ln \text{Ci}E_{ntm}^T \left(\eta_{itm}^0 \right)}$ captures (first-degree) GE spillovers

Identification: Shift-Share IV from Het Tourist Pref

- **Challenge:** Unobserved changes in attractiveness/productivity of a location
 - Induces comovement between residential expenditure and tourist expenditure
 - ...or residential income and tourist expenditure
 - ...or measurement error in independent variable (income proxy)

Identification: Shift-Share IV from Het Tourist Pref

- **Our Strategy:** Shift-share IV from Heterogeneous Tourist Preferences
 - Total tourist expenditure is given by:

$$B_{it}^T = \sum_{g \in T} s_{git}^0 \times E_{gt}^T$$

- Shares s_{git}^0 capture spatial preferences for group g in **baseline**
- Shifts from changes in group-specific expenditures (E_{gt}^T)
 - Leave-own-location-out
- Can be derived from non-parametric tourist demand [Derivations](#)
- With FE identification comes from unanticipated changes in Tourist expenditures

First Stage

Estimation Results

Income Regressions: Average and Heterogeneous Effects

- Recover **average treatment effects**

$$\ln v_{nmt} = \gamma_i + \gamma_m + \gamma_t + \beta^w \times \ln \text{CiE}_{ntm}^T + \epsilon_{imt},$$

- Recover **heterogeneous treatment effects**

$$\ln v_{nmt} = \gamma_i + \gamma_m + \gamma_t + \beta^w \times \ln \text{CiE}_{ntm}^T + \beta^{w,het} \times \ln \text{CiE}_{ntm}^T \left(\eta_{itm}^0 \right) + \epsilon_{imt},$$

- Variables

- $\ln v_{nmt}$ is income at residential tile and is regressed on:

$$\ln \text{CiE}_{ntm}^T = \sum_i c_{ni} \times \ln E_{itm}^T$$

Income Regressions: Average and Heterogeneous Effects

Dependent Variable:		ln Income (Mean)					
		Cell	Lunch	Cell Phone		Lunchtime	
Model:		OLS		IV - 2017 Low Season		IV - 2017 Low Season	
		(1)	(2)	(3)	(4)	(5)	(6)
<i>Variables</i>							
ln CiE _{nt}		0.012 (0.012)	0.006 (0.004)	0.035 (0.025)	0.008 (0.037)	0.040** (0.018)	-0.009 (0.025)
$\eta_{it}^0 \times \ln \widehat{CiE}_{nt}(\eta_{it}^0)$					0.046 (0.033)		0.092*** (0.027)
<i>Fixed-effects</i>							
Location		✓	✓	✓	✓	✓	✓
Month		✓	✓	✓	✓	✓	✓
Year		✓	✓	✓	✓	✓	✓
<i>Fit statistics</i>							
Observations		1,776	26,472	1,776	1,776	26,472	26,472
Adjusted R ²		0.93	0.888	0.93	0.93	0.888	0.888
F-test = t ² (1st Stage)				142.8	142.8	927.0	927.0

Heteroskedasticity-robust standard-errors in parentheses

Signif. Codes: ***: 0.01, **: 0.05, *: 0.1

[ATE Results \(Details\)](#)

[HTE Results \(Details\)](#)

Price Regressions: Step 1

- Recover **average treatment effects**

$$\ln \delta_{ismt} = \gamma_{tms} + \gamma_{is} + \gamma_{ist} + \gamma_{ism} + \beta^p \times \log E_{itm}^T + \epsilon_{ismt},$$

- Variables
 - δ_{ismt} is destination FE from PPML specification on travel time
 - [Binscatter Plot](#) [Gravity Results](#)

Price Regressions: Step 1

Dependent Variable:	Residents Expenditure (Gravity): δ_{ist}^R								
	OLS			IV - Ref: 2017 Average			IV - Ref: 2017 Low Season		
Model:	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
<i>Variables</i>									
Tourists Expenditure: $\ln E_{it}^T$	0.159*** (0.011)	0.152*** (0.014)	0.091*** (0.010)	-0.437*** (0.096)	-0.477*** (0.108)	-0.576*** (0.189)	-0.469*** (0.100)	-0.512*** (0.111)	-0.668*** (0.223)
<i>Fixed-effects</i>									
Month-Year \times Sector (480)	✓	✓	✓	✓	✓	✓	✓	✓	✓
Location \times Sector (21,920)	✓	✓	✓	✓	✓	✓	✓	✓	✓
Location \times Sector \times Year (43,840)		✓	✓		✓	✓		✓	✓
Location \times Sector \times Month (263,040)			✓			✓			✓
<i>Fit statistics</i>									
Observations	526,080	526,080	526,080	526,080	526,080	526,080	526,080	526,080	526,080
Adjusted R^2	0.992	0.993	0.994	0.99	0.991	0.993	0.99	0.991	0.992
F-test = t^2 (1st Stage)				145.4	138.2	38.4	153.3	148.7	30.7

Heteroskedasticity-robust standard-errors in parentheses

Signif. Codes: ***: 0.01, **: 0.05, *: 0.1

Binscatter Plots

Price Regressions: Step 2 and 3

- Recover heterogeneous treatment effects

$$\ln \delta_{ismt} = \gamma_{tms} + \gamma_{is} + \gamma_{ist} + \gamma_{ism} + \beta^{p,het} \times \eta_{itm}^0 \times \log E_{itm}^T + \beta^{p,GE} \times \eta_{itm}^{0,Res} \times \log E_{itm}^{T,GE} + \epsilon_{ismt}$$

- Variables
 - $\eta_{itm}^{0,Res} = E_i^R / y_i$ is the importance of residential expenditures in a tile
 - (first-order) GE spillover effect is approximated by:

$$\ln E_{ntm}^{T,GE}(\eta_{itm}^0) = \sum_n s_{ni} \times \ln \widehat{CiE}_{ntm}^T(\eta_{itm}^0)$$

Price Regressions: Step 2 and 3

Dependent Variable:	δ_{ist}^R					
	IV - Ref: 2017 Average			IV - Ref: 2017 Low Season		
Model:	(1)	(2)	(3)	(4)	(5)	(6)
<i>Variables</i>						
$\widehat{\ln E_{it}^T}$	0.019 (0.059)	-0.029 (0.059)	-0.059 (0.060)	0.011 (0.064)	-0.037 (0.064)	-0.062 (0.065)
$\widehat{\ln E_{it}^T} \times \eta_{it}^0$	-0.523*** (0.087)	-0.467*** (0.087)	-0.357*** (0.096)	-0.628*** (0.091)	-0.555*** (0.091)	-0.448*** (0.102)
$\widehat{\ln E_{it}^{GE}}(\eta_i^0)$		-0.004*** (0.0005)	-0.009*** (0.002)		-0.005*** (0.0005)	-0.009*** (0.002)
$\widehat{\ln E_{it}^{GE}}(\eta_i^0) \times \eta_i^{0,Res}$			0.007*** (0.003)			0.006** (0.003)
<i>Fixed-effects</i>						
Month-Year \times Sector (480)	✓	✓	✓	✓	✓	✓
Location \times Sector (21,840)	✓	✓	✓	✓	✓	✓
Location \times Sector \times Year (43,680)	✓	✓	✓	✓	✓	✓
Location \times Sector \times Month (262,080)	✓	✓	✓	✓	✓	✓
<i>Fit statistics</i>						
Observations	524,160	524,160	524,160	524,160	524,160	524,160
Adjusted R^2	0.975	0.975	0.975	0.975	0.975	0.975

Normal standard-errors in parentheses

Signif. Codes: ***: 0.01, **: 0.05, *: 0.1

Group Estimates

Rental Rate Estimates

Outline of Talk

A General Methodology for (small) Urban Shocks

Intra-city Patterns of Consumption & Income

Empirical Strategy and Identification

Welfare Effects Across the City

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Conclusion

Is tourism good for the locals (on average)?

- Can aggregate to welfare using a simplified version of welfare results

$$\frac{d \ln \bar{u}}{\partial \ln E^T} = \frac{\partial \ln \bar{v}}{\partial \ln E_i^T} - \frac{\partial \ln \bar{p}}{\partial \ln E_i^T}$$

- Average Welfare effects (Low/High Season)
 - Implies net welfare deterioration of 5pc
- Caveats
 - Aggregation Bias
 - SUTVA violation

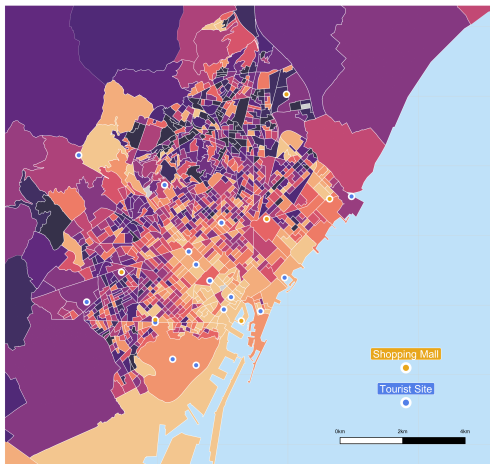
Is tourism good for the locals?

- Welfare Formula

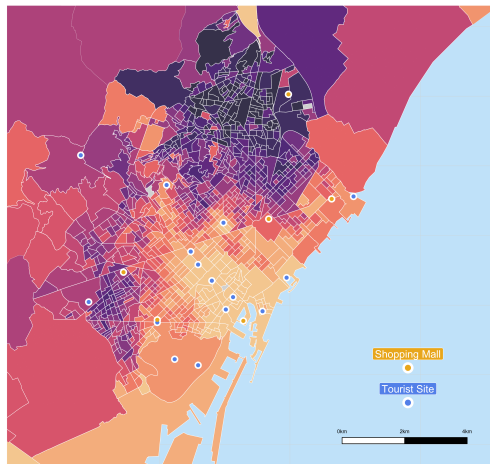
$$d \ln u_n = \frac{\partial \ln v_n}{\partial \ln E_i^T} \times d \ln E_i^T - \sum_i s_{ni} \times \frac{\partial \ln p_i}{\partial \ln E_i^T} \times d \ln E_i^T$$

- s_{ni} use baseline averages in 2017
- c_{ni} only one cross-section available
- Predict income and price changes from January to August

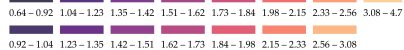
Income (Panel A) and Price Effects (Panel B)



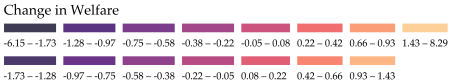
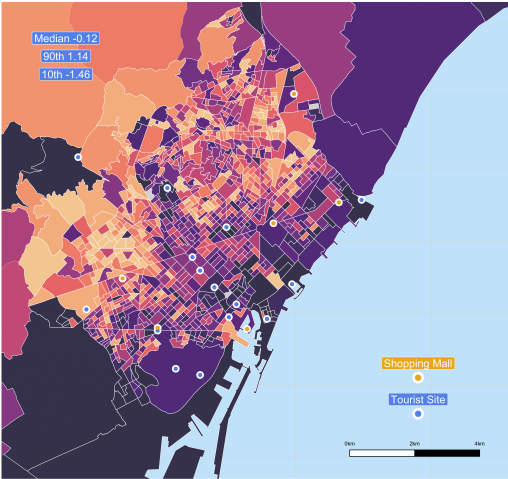
Change in Income



Change in Price Index



Welfare Effects



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Comparison to Quantitative Model

- Demand

$$G(\mathbf{p}_n) = \left(\sum_{s=0}^S \alpha_s \left(\left(\sum_{i=1}^N \tilde{p}_{nis}^{1-\sigma_s} \right)^{\frac{1}{1-\sigma_s}} \right)^{1-\eta} \right)^{\frac{1}{1-\eta}}$$

- Wage Aggregator ($\epsilon < 0$)

$$J(\mathbf{w}_n) = \left(\sum_i (w_{ni})^{1-\epsilon} \right)^{\frac{1}{1-\epsilon}}$$

- Production with Specific Factors

$$Q_{is} = F_{is}(l_{is}, m_{is}) = z_{is} l_{is}^{\beta_s} m_{is}^{1-\beta_s}$$

Equilibrium

- Market Clearing Condition

$$y_{is} = \sum_{n=1}^N s_{nis} v_n + \sum_{g=1}^G s_{gis} E_g^T$$

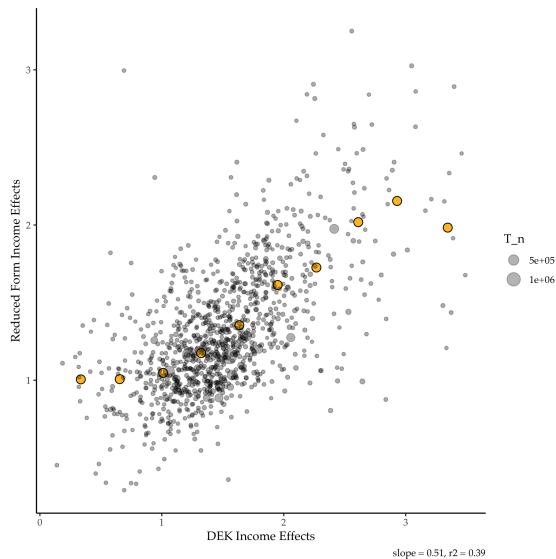
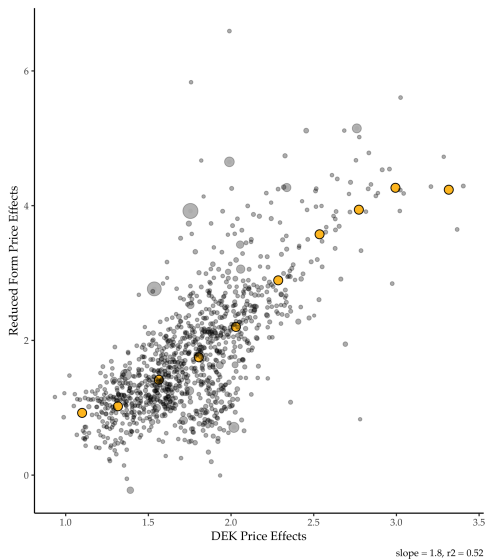
- Labor Market Clearing

$$w_i \ell_i = \sum_{s=0}^S \theta_s^\ell \sum_{n=1}^N s_{nis} v_n + \sum_{s=0}^S \theta_s^\ell \sum_{g=1}^G s_{gis} E_g^T$$

- Disposable Income

$$v_n = \left(\sum_i (w_{ni})^{1-\epsilon} \right)^{\frac{1}{1-\epsilon}} \times T_n$$

Price and Income Predictions highly correlated with DEK Results



Price Regressions Redux

Dependent Variable:	δ_{1st}^R			
	IV - Ref: 2017 Average			
Model:	(1)	(2)	(3)	(4)
<i>Variables</i>				
$\widehat{\ln E_{it}^T}$	0.011 (0.064)	2.63 (4.61)	-0.062 (0.065)	4.49 (4.61)
$\widehat{\ln E_{it}^T} \times \eta_{it}^0$	-0.628*** (0.091)	-0.541*** (0.179)	-0.448*** (0.102)	-0.294 (0.186)
$\widehat{\ln E_{it}^T} \times \widehat{p}_i^{DEK}$		-2.58 (4.54)		-4.49 (4.55)
$\widehat{\ln E_{it}^{GE}}(\widehat{\eta}_i^0)$			-0.009*** (0.002)	-0.009*** (0.002)
$\widehat{\ln E_{it}^{GE}}(\widehat{\eta}_i^0) \times \widehat{\eta}_i^{0,Res}$			0.006** (0.003)	0.006** (0.003)
<i>Fixed-effects</i>				
Month-Year \times Sector (480)	✓	✓	✓	✓
Location \times Sector (21,840)	✓	✓	✓	✓
Location \times Sector \times Year (43,680)	✓	✓	✓	✓
Location \times Sector \times Month (262,080)	✓	✓	✓	✓
<i>Fit statistics</i>				
Observations	524,160	524,160	524,160	524,160
Adjusted R^2	0.975	0.975	0.975	0.975

Normal standard-errors in parentheses

Signif. Codes: ***: 0.01, **: 0.05, *: 0.1

Outline of Talk

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Conclusion

Conclusion: Estimating the welfare impacts of an urban shock

- Option A: Quantitative model
 - (+) Incorporates full GE structure of the city
 - (-) Relies on strong parameterizations
- Option B: Average treatment effects
 - (+) Robust to model mis-specification
 - (-) Ignores heterogeneity, GE spillovers (SUTVA likely violated).
- Option C: A hybrid approach.
 - (+) Incorporates heterogeneity, (short-run) GE spillovers
 - (+) With a minimal set of model assumptions.

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Commuting Implied Exposure Derivation

- Disposable income is given by

$$v_n = \sum_{i=1}^N w_i l_{ni}$$

- Totally differentiating and applying the envelope result from above, we obtain,

$$d \ln v_n = \sum_{i=1}^N c_{ni} d \ln w_i$$

- Impact of tourist expenditure shock,

$$d \ln v_n = \sum_{i=1}^N c_{ni} \frac{d \ln w_i}{d \ln E^T} d \ln E^T \quad \ln C_i E_{ntm}^T = \sum_i c_{ni} \times \ln E_{itm}^T$$

Shift-Share Instrument: Derivations

- Representative tourist for group g has preferences,

$$u_g = \frac{E_g^T}{G(\tilde{\mathbf{p}})}$$

- Roy's identity gives expenditure shares
- Changes in tourist expenditure are:

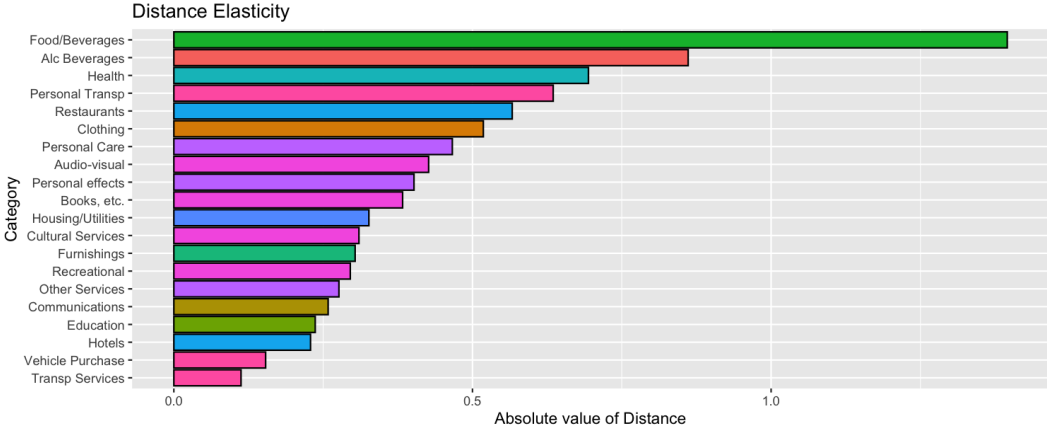
$$dX_i^T = \sum_g s_{gi} dE_g^T + \sum_g s_{gi} db_{gi} + \sum_g s_{gi} dp_i$$

- Taking it to the data,

$$\Delta E_{imt}^T = \underbrace{\sum_g s_{gi} \times \Delta E_{gt}^T}_{\text{Group Composition}} + \epsilon_{imt}^T$$

- where $\epsilon_{imt}^T = \sum_g s_{gi} db_{gi} + \sum_g s_{gi} dp_i$

Distance Coefficient for Gravity by Sector



Source: CXBK Payment Processing (2019)

Commuting Gravity Estimates

Dependent Variables:	commuters	log(commuters+1)	log(commuters)	transactions	log(transactions+1)	log(transactions)
	Cell Phone			Lunchtime		
Model:	(1) Poisson	(2) OLS	(3) OLS	(4) Poisson	(5) OLS	(6) OLS
<i>Variables</i>						
ldist	-4.48*** (0.107)	-1.51*** (0.037)	-1.17*** (0.054)	-1.53*** (0.028)	-0.134*** (0.002)	-0.411*** (0.012)
<i>Fixed-effects</i>						
Origin	✓	✓	✓			
Destination	✓	✓	✓			
Origin (CT)				✓	✓	✓
Destination (CT)				✓	✓	✓
<i>Fit statistics</i>						
Observations	24,025	24,025	2,162	1,051,159	1,216,609	42,086
Pseudo R ²	0.798	0.117	0.193	0.598	0.343	0.091

Heteroskedasticity-robust standard-errors in parentheses

*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

back

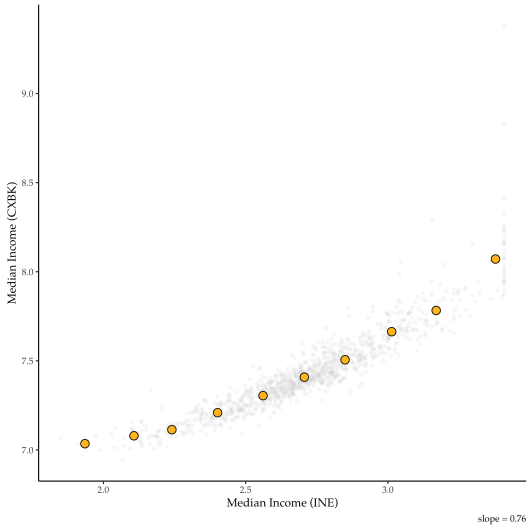
Housing Price Regressions

Dependent Variables:	HPRICE				RENT			
	IV - Ref: 2017 Average		IV - Ref: 2017 Low Season		IV - Ref: 2017 Average		IV - Ref: 2017 Low Season	
Model	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
<i>Variables</i>								
$\widehat{\log E_{it}^T}$	0.059*** (0.016)	0.028*** (0.005)	0.059*** (0.016)	0.028*** (0.005)	0.043*** (0.013)	0.008* (0.005)	0.044*** (0.013)	0.009* (0.005)
<i>Fixed-effects</i>								
i (108)	✓	✓	✓	✓	✓	✓	✓	✓
i×month (1,296)	✓		✓		✓		✓	
i×year (216)		✓		✓		✓		✓
<i>Fit statistics</i>								
Observations	2,592	2,592	2,592	2,592	2,592	2,592	2,592	2,592
Adjusted R^2	0.983	0.993	0.983	0.993	0.933	0.952	0.933	0.952

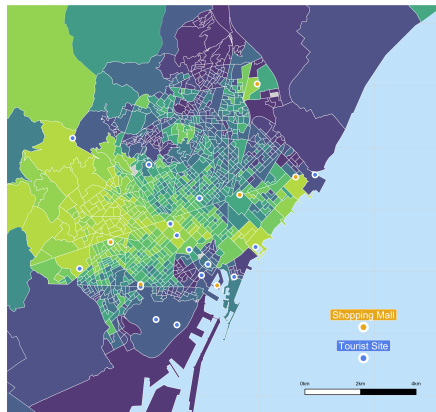
Heteroskedasticity-robust standard-errors in parentheses

*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

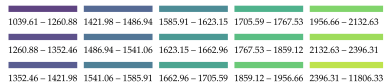
Income Data: Comparison with Administrative Data



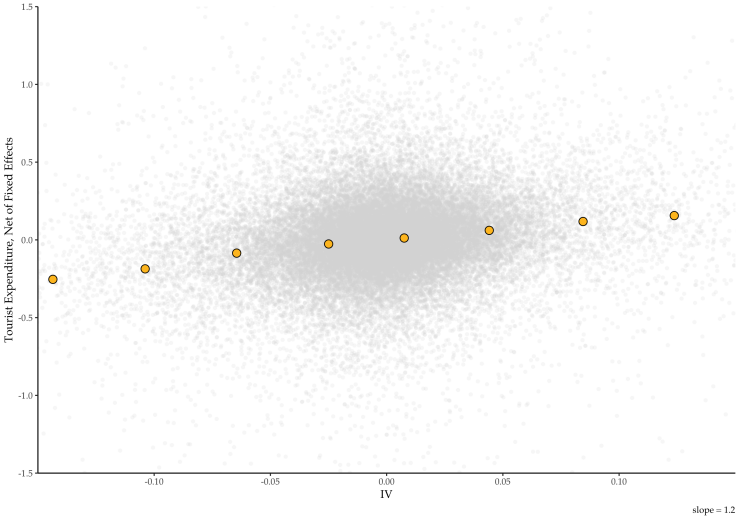
Income Distribution across Barcelona



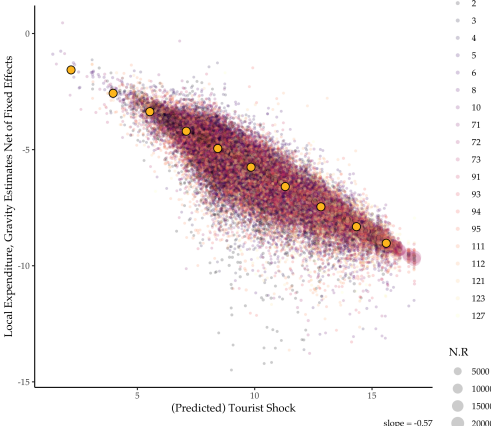
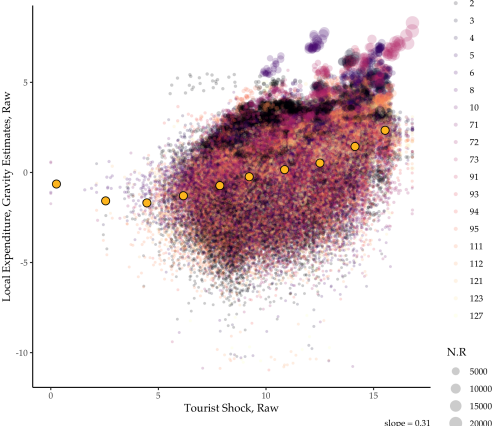
Mean Income



Shift Share: First Stage

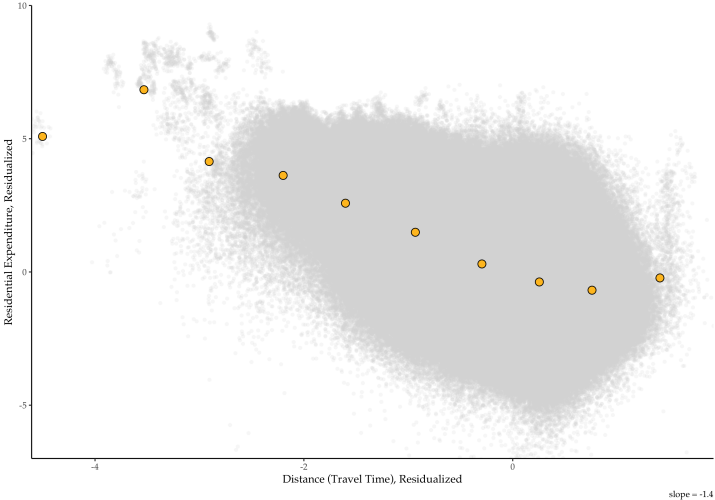


Price Regressions: Raw vs 2SLS



Back

Fit of Gravity Specification



Expenditure Gravity Regressions

Dependent Variables:	Bilateral Spending		log(Bilateral Spending+1)		log(Bilateral Spending)	
Model:	(1) Poisson	(2) Poisson	(3) OLS	(4) OLS	(5) OLS	(6) OLS
<i>Variables</i>						
log(travel time)	-2.17*** (0.003)	-2.17*** (0.003)	-1.37*** (0.0009)	-1.37*** (0.0009)	-1.36*** (0.001)	-1.36*** (0.001)
<i>Fixed-effects</i>						
Origin (CT)	✓		✓		✓	
Destination (CT)	✓		✓		✓	
Origin (CT)×YEARMONTH		✓		✓		✓
Destination (CT)×YEARMONTH		✓		✓		✓
<i>Fit statistics</i>						
Observations	43,204,320	43,125,480	43,204,320	43,204,320	6,566,622	6,566,622
Pseudo R ²	0.781	0.788	0.127	0.130	0.120	0.126

Heteroskedasticity-robust standard-errors in parentheses

*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

Is tourism good for the locals (on average)?

- Can aggregate to welfare using a simplified version of welfare results

$$\frac{d \ln \bar{u}}{\partial \ln E^T} = \frac{\partial \ln \bar{v}}{\partial \ln E_i^T} - \frac{\partial \ln \bar{p}_s}{\partial \ln E_i^T}$$

- Results
 - Income elasticity: .04
 - Consumption Price Index elasticity: [.1,.175]
 - House Price elasticity: .06
 - Welfare elasticity: [-.1,-.04]
 - Average increase between February and July \approx 50pc
 - Implies net welfare deterioration of 5pc

Income Regressions: Step 1

Dependent Variable:		ln Income (Mean)					
	Lunch	Cell	Cell Phone		Lunchtime		
Model:	OLS (1)	(2)	IV - 2017 Average (3)	IV - 2017 Low Season (4)	IV - 2017 Average (5)	IV - 2017 Low Season (6)	
<i>Variables</i>							
ln MA _{nt}	0.006 (0.004)	0.012 (0.012)	0.032 (0.021)	0.035 (0.025)	0.038*** (0.015)	0.040** (0.018)	
<i>Fixed-effects</i>							
Location	✓	✓	✓	✓	✓	✓	
Month	✓	✓	✓	✓	✓	✓	
Year	✓	✓	✓	✓	✓	✓	
<i>Fit statistics</i>							
Observations	26,472	1,776	1,776	1,776	26,472	26,472	
Adjusted R ²	0.888	0.93	0.93	0.93	0.888	0.888	
F-test = t ² (1st Stage)			204.5	142.8	1,267.2	927.0	

Heteroskedasticity-robust standard-errors in parentheses

*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

Comparison with Household Budget Survey

COICOP (2D)	COICOP (2D)	Local	Spanish Tourists	Foreign Tourists	Total	Survey (INE)	Survey Adj (INE)
11	Food/Beverages	32.82 (24.72)	1.32 (5.04)	4.51 (5.10)	38.66	12.96	23.82
21	Alc Beverages	1.97 (1.48)	0.07 (0.28)	0.60 (0.68)	2.64	0.71	1.31
31	Clothing	11.58 (8.72)	1.94 (7.39)	12.00 (13.55)	25.51	3.39	6.23
41	Housing/Utilities	2.81 (2.12)	0.78 (3.00)	0.59 (0.67)	4.19	5.33	9.80
51	Furnishings	10.03 (7.55)	3.32 (12.67)	2.01 (2.27)	15.35	0.88	1.62
61	Health	10.76 (8.10)	1.94 (7.40)	1.82 (2.06)	14.52	2.24	4.12
71	Vehicle Purchase	3.14 (2.36)	0.18 (0.67)	0.32 (0.36)	3.63	3.78	6.95
72	Personal Transp	7.27 (5.47)	2.06 (7.89)	0.70 (0.79)	10.03	6.38	11.73
73	Transp Services	10.13 (7.63)	6.52 (24.90)	9.61 (10.85)	26.26	1.90	3.49
81	Communications	0.30 (0.23)	0.02 (0.09)	0.08 (0.09)	0.40	0.33	0.61
91	Audio-visual	5.06 (3.81)	0.57 (2.17)	1.78 (2.01)	7.40	0.58	1.07
93	Recreational	2.62 (1.97)	0.27 (1.03)	1.21 (1.37)	4.09	1.43	2.63
94	Cultural Services	4.29 (3.23)	0.62 (2.38)	2.79 (3.15)	7.70	0.57	1.05
95	Books, etc	1.64 (1.23)	0.22 (0.85)	0.53 (0.60)	2.39	1.30	2.39
101	Education	1.11 (0.84)	0.10 (0.39)	0.61 (0.69)	1.82	0.77	1.41
111	Restaurants	17.73(13.35)	3.79 (14.46)	19.04 (21.50)	40.56	7.83	14.39
112	Hotels	1.13 (0.85)	1.49 (5.69)	23.12 (26.11)	25.75	1.21	2.22
121	Personal Care	4.84 (3.64)	0.32 (1.23)	0.97 (1.10)	6.14	2.53	4.65
123	Other	2.49 (1.88)	0.36 (1.37)	5.69 (6.42)	8.54	0.32	0.59
Total		131.72 (100)	25.88 (100)	87.97 (100)	245.58	54.4	100

Income Regressions: Step 2

Dependent Variable:		ln Income (Mean)					
	Cell	Lunch	Cell Phone		Lunchtime		
Model:	OLS (1)	(2)	IV - 2017 Average (3)	IV - 2017 Low Season (4)	IV - 2017 Average (5)	IV - 2017 Low Season (6)	
<i>Variables</i>							
$\ln \widehat{CIE}_{nt}$	0.012 (0.012)	0.006 (0.004)	0.007 (0.029)	0.008 (0.037)	-0.005 (0.021)	-0.009 (0.025)	
$\ln \widehat{CIE}_{nt}(\eta_{it}^0)$			0.045 (0.030)	0.046 (0.033)	0.086*** (0.027)	0.092*** (0.027)	
<i>Fixed-effects</i>							
Location	✓	✓	✓	✓	✓	✓	
Month	✓	✓	✓	✓	✓	✓	
Year	✓	✓	✓	✓	✓	✓	
<i>Fit statistics</i>							
Observations	1,776	26,472	1,776	1,776	26,472	26,472	
Adjusted R^2	0.93	0.888	0.93	0.93	0.888	0.888	
F-test = t^2 (1st Stage)			204.5	142.8	1,267.2	927.0	

Heteroskedasticity-robust standard-errors in parentheses

*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

Hat Algebra

- Market Clearing Condition

$$\hat{y}_{is} = \pi_{is}^{local} \sum_{n=1}^N (\pi_{is}^n \hat{S}_{nis} \hat{V}_n) + \pi_{is}^{group} \sum_{g=1}^G (\pi_{is}^g \hat{S}_{gis} \hat{E}_g^T)$$

- Labor Market Clearing

$$\sum_s \frac{\beta_s y_{is}}{\sum_{s'} \beta_s y_{is'}} \hat{y}_{is} = \sum_{n=1}^N \frac{w_i l_{ni}}{\sum_{n'=1}^N w_i l_{n'i}} (\hat{W}_{ni})^\theta \hat{T}_n \hat{W}_n^{1-\theta}$$

- Disposable Income

$$\hat{v}_n = \sum_{i=1}^N \frac{l_{ni} w_i}{\sum_{i'=1}^N l_{ni'} w_{i'}} (\hat{W}_{ni})^\theta \hat{T}_n \hat{W}_n^{1-\theta}$$

Parameterization

Parameter	Value	Comment
β_s	0.65 $\forall s$	labor share of income
σ_s	4 $\forall s$	elasticity of substitution (within sectors)
η	1.5	elasticity of substitution (between sectors)
θ	1.5	labor dispersion ($1 - \epsilon$)
γ	[0, 0, 0, 0]	consumption spillovers

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Data Requirements

Data	Description	Comment
I_{ni}	Commuting Flows	Lunch Expenditures
x_{nis}	Base Local Expenditures	
x_{gis}	Base Tourist Expenditures	
\hat{E}_i^T	Change in Tourist Expenditures	Difference from Jan to July
v_n	Worker Incomes	

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Roy's Identity for Labor Supply

- Income maximization problem:

$$v_n = \max_{\{\ell_i\}} \sum_{i=1}^N w_i \ell_i \quad \text{s.t.} \quad H_n(\ell_n) = T_n$$

- Maximand is the income function $y(\mathbf{w}_n, T_n)$ and envelope theorem implies,

$$\frac{\partial y(\cdot)}{\partial w_i} = \ell_i$$

- Dual is cost minimization problem, where minimand is $h(\mathbf{w}_n, \bar{Y})$

- Differentiating we obtain,

$$\frac{\partial y(\cdot)}{\partial w_i} = - \frac{\frac{\partial h(\mathbf{w}_n, y(\mathbf{w}_n, T_n))}{\partial w_i}}{\frac{\partial h(\mathbf{w}_n, y(\mathbf{w}_n, T_n))}{\partial h(\mathbf{w}_n, y(\mathbf{w}_n, T_n))}} = \ell_i$$

Derivation of Welfare Formula

- Assuming both homothetic demand and a homothetic income maximization problem allows us to write the indirect utility function as,

$$u_n = \frac{T_n J(\mathbf{w}_n)}{G(\mathbf{p}_n)}$$

- Totally differentiating,

$$\frac{du_n}{u_n} = \sum_{i=1}^N \frac{1}{J(\mathbf{w}_n)} \frac{\partial (J(\mathbf{w}_n))}{\partial w_i} w_i \frac{dw_i}{w_i} + \sum_{i=1}^N G(\mathbf{p}_n) \frac{\partial (1/G(\mathbf{p}_n))}{\partial p_{ni}} p_{ni} \frac{dp_{ni}}{p_{ni}}$$

- Applying Roy's identity for the income maximization and consumption problem from above,

$$\frac{du_n}{u_n} = \sum_{i=1}^N \frac{\ell_i}{v_n} w_i \frac{dw_i}{w_i} - \sum_{i=1}^N \frac{q_{ni}}{v_n} p_{ni} \frac{dp_{ni}}{p_{ni}}$$

Price Regressions: Group Estimates

Dependent Variables:	δ_{ist}^R	$\delta_{ist}^{T.Dom}$	$\delta_{ist}^{T.For}$	δ_{ist}^R	$\delta_{ist}^{T.Dom}$	$\delta_{ist}^{T.For}$
	OLS			IV - Ref: 2017 Average		
Model:	(1)	(2)	(3)	(4)	(5)	(6)
<i>Variables</i>						
$\ln E_{it}^T$	0.091*** (0.003)	0.485*** (0.005)	0.454*** (0.004)	-0.576*** (0.034)	-0.277*** (0.077)	0.029 (0.056)
<i>Fixed-effects</i>						
Month-Year \times Sector (480)	✓	✓	✓	✓	✓	✓
Location \times Sector (21,920)	✓	✓	✓	✓	✓	✓
Location \times Sector \times Year (43,840)	✓	✓	✓	✓	✓	✓
Location \times Sector \times Month (263,040)	✓	✓	✓	✓	✓	✓
<i>Fit statistics</i>						
Observations	526,080	526,080	526,080	526,080	526,080	526,080
Adjusted R^2	0.994	0.991	0.994	0.993	0.99	0.993

Normal standard-errors in parentheses

Signif. Codes: ***: 0.01, **: 0.05, *: 0.1

CES Model Example of Simple Non-Parametric Model

- Preferences

$$u_n(\{q_{ni}\}_{i=1,\dots,N}) = \left(\sum_{i=1}^N \alpha_{ni}^{1/\sigma} q_{ni}^{(\sigma-1)/\sigma} \right)^{\sigma/(\sigma-1)}$$

- Constraint

$$\sum_{i=1}^N p_{ni} q_{ni} \leq v_n$$

- Utility max. gives lagrangian

$$\mathcal{L}(\{q_{ni}\}_{i=1,\dots,N}, \lambda) = \left(\sum_{i=1}^N \alpha_{ni}^{1/\sigma} q_{ni}^{(\sigma-1)/\sigma} \right)^{\sigma/(\sigma-1)} + \lambda \left(v_n - \sum_{i=1}^N p_{ni} q_{ni} \right)$$

CES Model Example of Simple Non-Parametric Model

- FOCs

$$\frac{\partial \mathcal{L}}{\partial q_{ni}} = 0 \iff \left(\sum_{i=1}^N \alpha_{ni}^{1/\sigma} q_{ni}^{(\sigma-1)/\sigma} \right)^{1/(\sigma-1)} \alpha_{ni}^{1/\sigma} q_{ni}^{-1/\sigma} = \lambda p_{ni} \quad \forall i = 1, \dots, N$$

$$\frac{\partial \mathcal{L}}{\partial \lambda} = 0 \iff \sum_{i=1}^N p_{ni} q_{ni} = v_n$$

- For two consumption locations i and j

$$\begin{aligned} \left(\frac{\alpha_{ni}}{\alpha_{nj}} \right)^{1/\sigma} \left(\frac{q_{ni}}{q_{nj}} \right)^{-1/\sigma} &= \frac{p_{ni}}{p_{nj}} \\ \frac{\alpha_{ni}}{\alpha_{nj}} &= \frac{p_{ni}^\sigma q_{ni}}{p_{nj}^\sigma q_{nj}} \end{aligned}$$

CES Model Example of Simple Non-Parametric Model

- For two consumption locations i and j

$$\frac{\alpha_{ni}}{\alpha_{nj}} = \frac{p_{ni}^{\sigma} q_{ni}}{p_{nj}^{\sigma} q_{nj}}$$
$$q_{nj} = \frac{\alpha_{nj} p_{ni}^{\sigma}}{\alpha_{ni} p_{nj}^{\sigma}} q_{ni}$$

- $\times p_{nj}$

$$q_{nj} p_{nj} = \frac{\alpha_{nj} p_{ni}^{\sigma}}{\alpha_{ni} p_{nj}^{\sigma}} q_{ni} p_{nj}$$
$$q_{nj} p_{nj} = \frac{1}{\alpha_{ni}} q_{ni} p_{ni}^{\sigma} \alpha_{nj} p_{nj}^{1-\sigma}$$

CES Model Example of Simple Non-Parametric Model

- \sum_j

$$\sum_j q_{nj} p_{nj} = \frac{1}{\alpha_{ni}} q_{ni} p_{ni}^\sigma \sum_j \alpha_{nj} p_{nj}^{1-\sigma}$$

- using FOC2 (BC)

$$v_n = \frac{1}{\alpha_{ni}} q_{ni} p_{ni}^\sigma P_n^{1-\sigma}$$

- and demand for good i

$$q_{ni} = \alpha_{ni} p_{ni}^{-\sigma} v_n P_n^{\sigma-1}$$

CES Model Example of Simple Non-Parametric Model

- We get indirect utility

$$U_n = \left(\sum_{i=1}^N \alpha_{ni}^{1/\sigma} \left[\alpha_{ni} p_{ni}^{-\sigma} v_n P_n^{\sigma-1} \right]^{(\sigma-1)/\sigma} \right)^{\sigma/(\sigma-1)}$$

$$U_n = P_n^{\sigma-1} v_n \left(\sum_{i=1}^N \alpha_{ni} p_{ni}^{1-\sigma} \right)^{\sigma/(\sigma-1)} = P_n^{\sigma-1} v_n P_n^{-\sigma}$$

$$U_n = \frac{v_n}{P_n} = \frac{v_n}{\left(\sum_{i=1}^N \alpha_{ni} p_{ni}^{1-\sigma} \right)^{1/(1-\sigma)}}$$

- We can also express demand as total spending

$$X_{ni} = p_{ni} q_{ni} = \alpha_{ni} \left(\frac{p_{ni}}{P_n} \right)^{1-\sigma} v_n$$