# INCOME DYNAMICS OF COUPLES: Correlated Risks and Heterogeneous Within-Household Insurance

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#### Motivation

- ▶ Individuals face labor market risk → household earnings risk?
- ► HH earnings risk matters for
  - Fiscal Policy: private vs. public insurance (e.g., Wu & Krueger)
  - Monetary Policy: MPCs (e.g., Bardóczy '20)
  - Macro models w/ micro data: bachelor household (e.g., HSV '10)

HSV '10: Wages and hours worked are characteristics recorded at the individual level, while consumption and welfare are typically measured at the level of the household. This presents an obvious challenge for the bachelor model as a lens for interpreting micro data.

# Motivation (cont.)

- Traditional focus:
  - HH-insurance: out-of-LF female reacting to male income shock
  - Measurement: individuals (males) or stably married HHs

But...

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#### Traditional focus:

- HH-insurance: out-of-LF female reacting to male income shock
- Measurement: individuals (males) or stably married HHs

#### But...

- - Especially married women (e.g., Olsson '20)
- Same time: divorce and formation of new couples
  - on avg. 2.5 spouses / individual in our sample

## This Paper

Characterize earnings dynamics:

- ► in two-earner households
- with family formation and dissolution over the life-cycle
- ▶ in Denmark: high female LF participation throughout

Key role of

- Correlation of spouses' incomes (risk)
  - Sorted by: education, occupation, industry, firm, ...

Implications for

#### Heterogeneity of intra-household insurance

1. Analyze **co-movement** of earnings changes

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- 2. Heterogeneity by labor market characteristics of couples
  - ► More **similar** partners → **worse** earnings stabilization
  - Matters within different groups: age, wealth

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  - Household income & consumption

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- 3. Pass-through to household-level
  - Household income & consumption
- 4. Ongoing: Role of heterogeneity for life-cycle dynamics
  - ► Joint income process with singles/couples & marriage/divorce

#### Outline

#### Intro

Data

Joint Income Changes

Pass-Through to Household

A Joint Earnings Process

Amplification: Sorting Patterns

Summary and Outlook

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# Data: Danish tax register & social security

- Whole Danish population panel 1991–2018
- Links individuals (couples)
- Info on:
  - Age, education, occupation, sector, firm
  - Earnings: total annual labor earnings
  - Taxes, transfers, assets

Benchmark analysis: 5.3 million couple-year observations

#### Data: Some Details

- Main data: IDA (Integrated Database for Labour Market Research)
  - BEF (Demographic characteristics and family linkages)
  - UDDA (Education)
  - AKM (Employment)
- Sample: age 18-59 with employment info
- Classifications
  - 2 Education groups: College and non-college (High and Low)
  - ▶ DISCO Classification: 2-digit level → 26 occupations
  - ▶ NACE Classification: Level 1→21 industries

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Consider log earnings changes of head and spouse:

$$\Delta y_t^{sp} = f(\Delta y_t^{hd}) \tag{1}$$

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Specify f(·) flexibly:

1. Non-linear in  $\Delta y_t^{hd}$ 

2. Heterogeneity by similarity of labor market characteristics

- Education, Occupation, Industry, Firm
- 3. Other sources of heterogeneity
  - Age, Wealth
  - #Children

## Measures of Spousal Earnings Comovement

Implied spousal earnings changes for each group

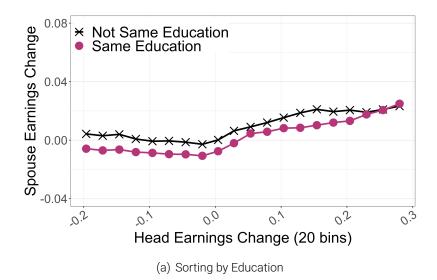
$$\hat{\Delta y}_t^{sp} = f(\Delta y_t^{hd}; \hat{\beta}) \tag{2}$$



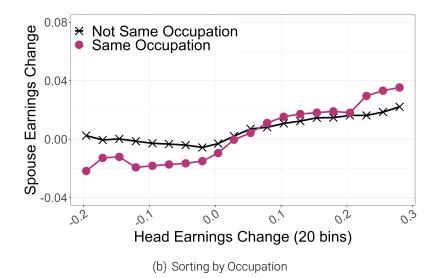
$$\hat{\epsilon}^{sp} = \frac{\hat{\Delta y}_t^{sp}}{\Delta y_t^{hd}}$$

(3)

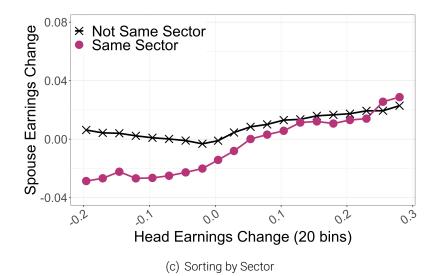
# Spousal Change–Education Groups



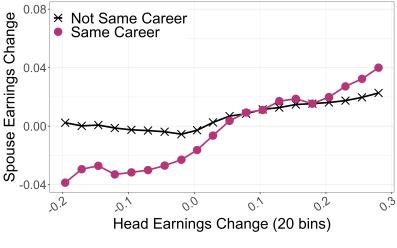
# Spousal Change–Occupation Groups



## Spousal Change–Sector Groups

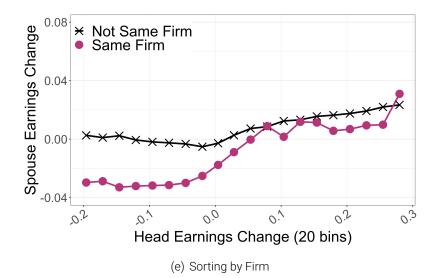


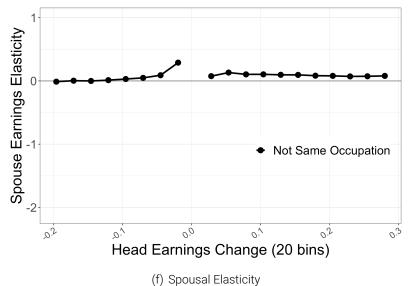
# Spousal Change–Sector×Occupation Groups

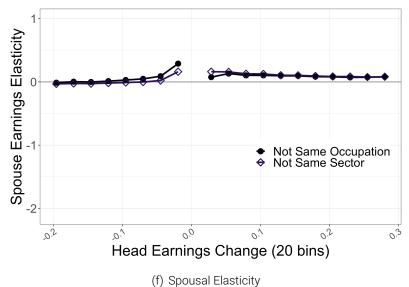


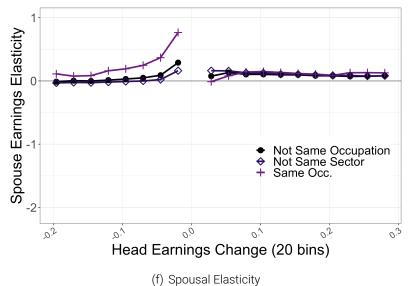
(d) Sorting by Sector×Occupation

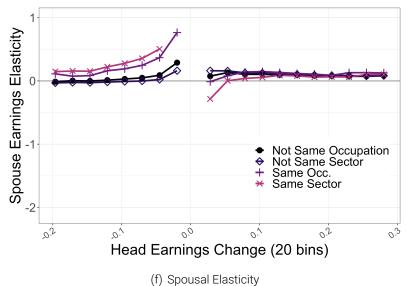
# Spousal Change–Firm Groups

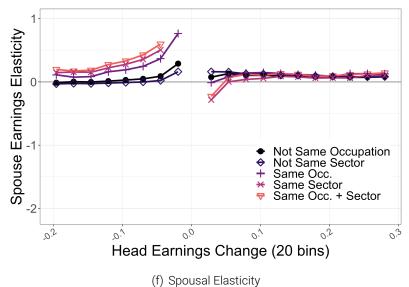


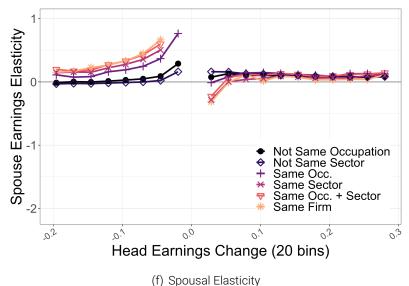




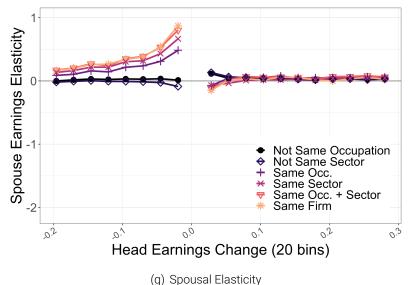








# Implied Spousal Earnings Elasticity-control age



#### Other Sources of Heterogeneity

- Spousal labor income (adjustments) one channel of insurance
- Other cannels: household savings; public transfers
  - Interaction?
  - Different relative importance for different groups?

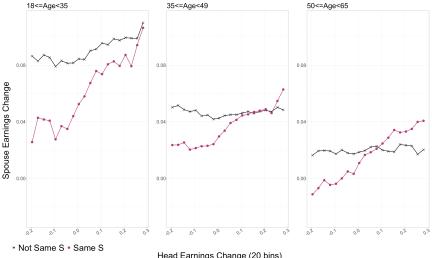
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- Spousal labor income (adjustments) one channel of insurance
- Other cannels: household savings; public transfers
  - Interaction?
  - Different relative importance for different groups?
- Role of labor market sorting by:
  - Age
  - Wealth (before change)

(cash+deposits+stocks+shares+property+cars-liabilities)

 $\Rightarrow$  Sorting matters within groups

# By Age Groups: Spousal Earnings





# By Wealth Groups: Spousal Earnings



Head Earnings Change (20 bins)



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### Measures of Pass-Through to Household Earnings

► Head earnings change  $\rightarrow$  Spouse earnings change

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- ▶ Head earnings change  $\rightarrow$  Household earnings change
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- Implied household earnings changes for each group

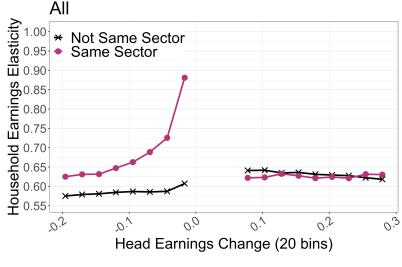
$$\hat{\Delta y}_t^{hh} = f(\Delta y_t^{hd}; \hat{\beta}) \tag{4}$$



$$\hat{\epsilon}^{hh} = \frac{\hat{\Delta y}_t^{hh}}{\Delta y_t^{hd}} \tag{5}$$

## Household Earnings Elasticity

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(i) Household Elasticity: Sector

► Household Change

### From Income To Consumption

$$\boldsymbol{C} = \boldsymbol{Y} - \boldsymbol{T} - \Delta \boldsymbol{A} \tag{6}$$

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### Components of budget in data:

- Y: Labor + capital income (+imputed cons. value housing)
- T: Tax payments transfer receipts

#### ΔA: Change asset value

(cash+deposits+stocks+shares+property+cars-liabilities)

### ⇒ Consumption

Lines up with Expenditure Survey

(De Giorgi, Frederiksen & Pistaferri, ReStud'20)

Measures of Pass-Through to Consumption

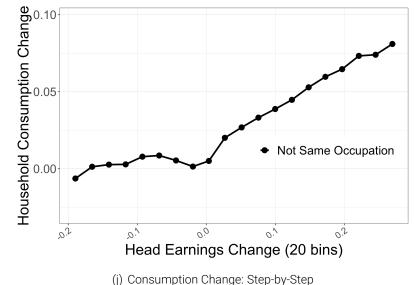
Implied household consumption changes for each group

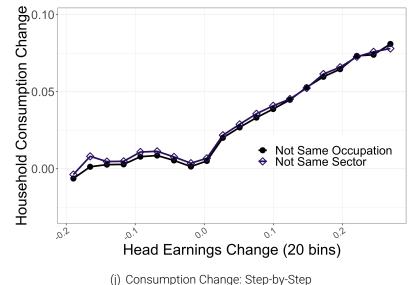
$$\hat{\Delta y}_t^c = f(\Delta y_t^{hd}; \hat{\beta}) \tag{7}$$

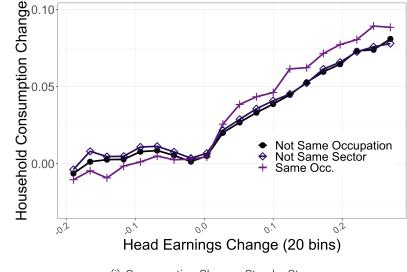


$$\hat{\epsilon}^{c} = \frac{\hat{\Delta c}_{t}^{hh}}{\Delta y_{t}^{hd}}$$

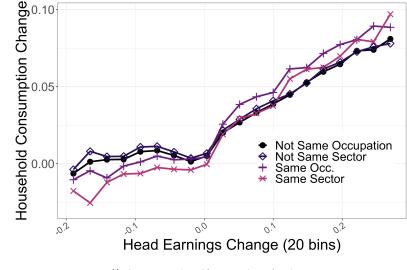
(8)



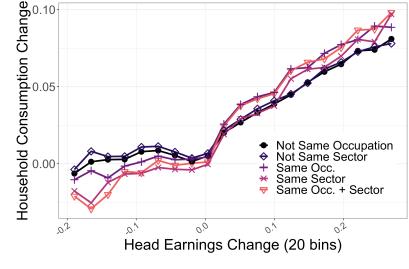




(j) Consumption Change: Step-by-Step



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### Income Dynamics: Adding Some Structure

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- Household earnings:
  - Two earnings (processes)
  - Correlated innovations
  - Transitory-permanent decomposition

(e.g., Blundell, Pistaferri & Saporta-Eksten, AER'16)

### Used in quantitative models

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Allow for heterogeneity by couple-type!

# A Simple (Joint) Income Process

## A Simple (Joint) Income Process

$$y_t^i = z_t^i + \varepsilon_t^i$$

$$z_t^i = z_{t-1}^i + \eta_t^i$$
(9)

- ▶ If in couple in t,  $\varepsilon_t^i \& \eta_t^i$  correlated
- Covariances  $\sigma_{\eta\eta}(s_t) \& \sigma_{\varepsilon\varepsilon}(s_t)$  depend on sorting group  $s_t$

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- Covariances  $\sigma_{\eta\eta}(s_t) \& \sigma_{\varepsilon\varepsilon}(s_t)$  depend on sorting group  $s_t$
- $\rightarrow$  Estimate on (co-)moments of *differences*:

$$\begin{aligned} \mathsf{var}(\Delta y_t^i) = \sigma_\eta^2 + 2\sigma_\varepsilon^2 \\ \mathsf{cov}(\Delta y_t^i, \Delta y_{t+1}^i) = -\sigma_\varepsilon^2 \\ \mathsf{cov}(\Delta y_t^m, \Delta y_t^f | \mathbf{s}_t = \mathbf{s}; \mathbf{s}_{t+1} = \mathbf{s}') = \sigma_{\eta\eta}(\mathbf{s}') + \sigma_{\varepsilon\varepsilon}(\mathbf{s}) + \sigma_{\varepsilon\varepsilon}(\mathbf{s}') \\ \mathsf{cov}(\Delta y_t^m, \Delta y_{t+1}^f | \mathbf{s}_t = \mathbf{s}; \mathbf{s}_{t+1} = \mathbf{s}') = -\sigma_{\varepsilon\varepsilon}(\mathbf{s}') \end{aligned}$$

### Estimates

- Consider different versions for *s*:
  - 1. none
  - 2. Education sorting:  $s \in \{same \ educ, not \ same \ educ\}$
  - 3. Occupation sorting: same occ vs. not same occ
  - 4. Sector, Career, Firm

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- $\rightarrow$  Correlations (old version):  $\rho_{\varepsilon} = -2.69\%$  and  $\rho_{\eta} = 3.74\%$
- With educ sorting:

$$ho_{arepsilon}(\text{same}) = -4.42\%, 
ho_{arepsilon}(\text{not}) = -2.86\%, 
ho_{\eta}(\text{same}) = 5.14\%, 
ho_{\eta}(\text{not}) = 2.28\%$$

► With occup sorting:

$$\rho_{\varepsilon}(\text{same}) = -3.73\%, \rho_{\varepsilon}(\text{not}) = -7.03\%, \\
\rho_{\eta}(\text{same}) = 10.45\%, \rho_{\eta}(\text{not}) = 3.21\%$$

### **Richer Income Process**

Process estimated on 'stable couples' not representative

- $\rightarrow~$  Estimate individual male and female processes
- $\rightarrow$  ...using male and females data
- $\rightarrow\ ...$ together with process of 'marriage' and 'divorce'
- Resulting income dynamics:
  - Correlated shocks while in couple
  - Additional conditional income shock upon divorce

$$y_t^i = z_t^i + \varepsilon_t^i + \delta_t^{\varepsilon_i} \cdot \mathbf{1} \{ div_t = \mathbf{1} \}$$
  

$$z_t^i = z_{t-1}^i + \eta_t^i + \delta_t^{\eta_i} \cdot \mathbf{1} \{ div_t = \mathbf{1} \}$$
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- Marriage and divorce shocks orthogonal to income shocks
- → Separately identified!

# Earnings dynamics and family changes

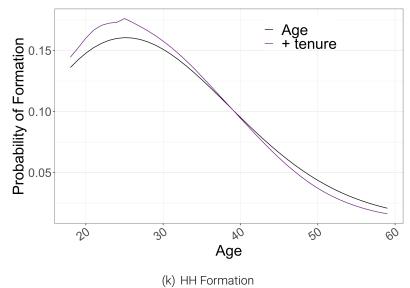
At every age, each single male and female can:

- form a couple with probability p<sup>form</sup>: receive ε, η, correlated with her spouse's ε, η in the next period
- stay single: receive  $\varepsilon, \eta$

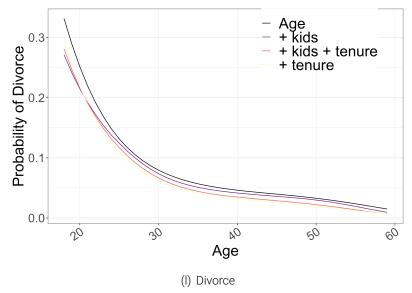
At every age, each male and female in couples can:

- divorce with probability *p<sup>div</sup>*: receive ε, η, correlated with her (outgoing) spouse's ε, η AND δ<sup>η</sup>, δ<sup>ε</sup>
- ▶ stay in the couple: receive  $\varepsilon$ ,  $\eta$ , correlated with her spouse's  $\varepsilon$ ,  $\eta$

# Couple formation Process (p<sup>form</sup>)



# Divorce Process (*p<sup>div</sup>*)



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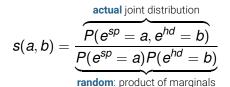
A Joint Earnings Process

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### Sorting Patterns

One simple measure (Eika, Mogstad, Zafar, JPE'19):



(11)

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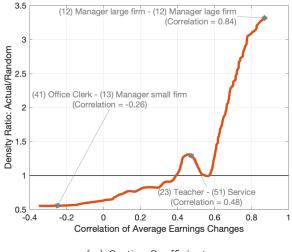
$$s(a,b) = \underbrace{\frac{P(e^{sp} = a, e^{hd} = b)}{P(e^{sp} = a)P(e^{hd} = b)}}_{random: \text{ product of marginals}}$$

(11)

Couples positively sorted by characteristics

- Education Sorting:  $s(H, H) \approx 2$  and  $s(L, L) \approx 1.2$
- ► Occupation and Sector: ≈ 2.2
- ⇒ Amplifies aggregate importance of above channels

# Sorting Coefficient Across Occupation-Pairs



(m) Sorting Coefficient

🕨 3d heatmap

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  - $\rightarrow$  Translates to household outcomes: **consumption**
- Couples sort:
  - Education, sector, occupation
  - Amplifies role of similarity for aggregate

## Outlook: Current & Future Steps

- Life-cycle dynamics for different sorting groups
  - Use panel dimension of data
  - Divorce risk, marriage risk
- Decompose spousal labor supply vs. savings vs. transfers
- Extensive margin of adjustment
  - Subsample: spell data
- Source of heterogeneous reaction to policy



#### Next: Quantitative Model

- Sorting/distribution of couples matters for
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  - Within-household insurance ("added worker effect")
  - Evaluation of public insurance
- Model featuring:
  - Incomplete markets
  - Distribution of couples over pairs of occupation
  - Head earnings process; Spouse wage process
    - $\longrightarrow$  Endogenous labor supply of spouse
  - Tax & transfer function

Joint Dynamics: Average by Group

Spousal income changes:

$$\Delta y_t^{sp} = \beta_0 + \tilde{f}(\Delta y_t^{hd}) + \mathbf{X}_t^{sp} \gamma + \mathbf{Y}\delta + u_{st}$$
(12)

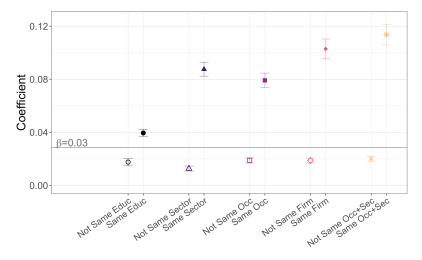
with

$$\tilde{f}(\Delta y_t^{hd}) = \left(I_{o_t^{hd} \neq o_t^{sp}} \beta^{\text{not same } x} + I_{o_t^{hd} = o_t^{sp}} \beta^{\text{same } x}\right) \Delta y_t^{hd}$$
(13)

>  $X_t^{sp}$ : age quadratic, education dummies, occupation dummies

• 
$$\Delta y_t^i$$
: 1-year income change

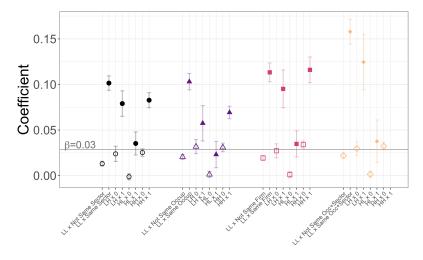
## Group-Specific Coefficients



(n) Elasticities for Different Sorting Vars

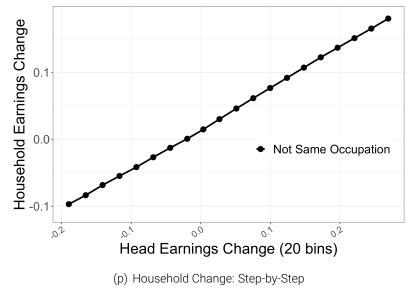
Back 🚺 🕨 Interacted 🕽

## Group-Specific Coefficients: By Education Pairs

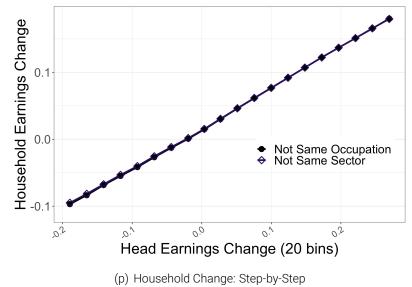


(o) Elasticities-Educ⊗Sorting Var

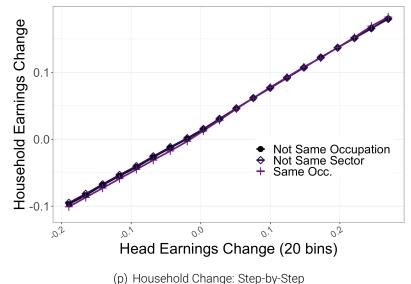
Back to Average



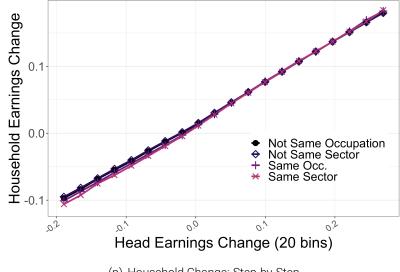
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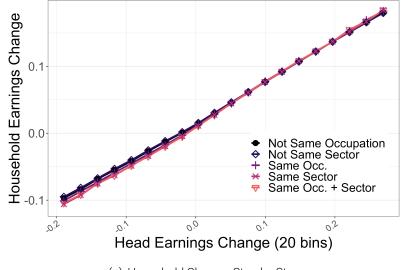


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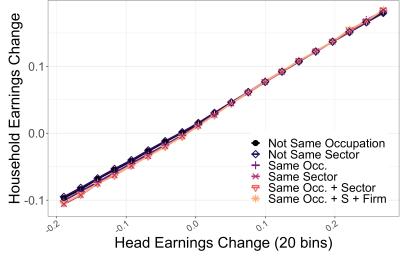
(p) Household Change: Step-by-Step

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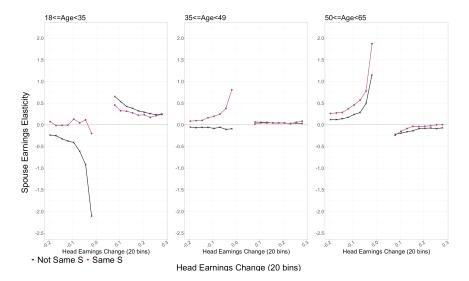
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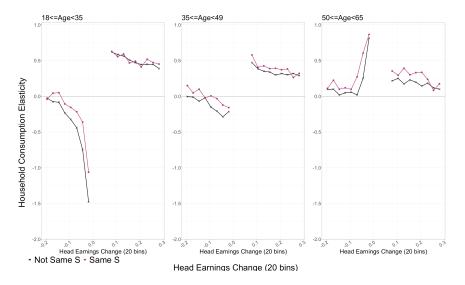
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# By Age Groups: Spousal Earnings



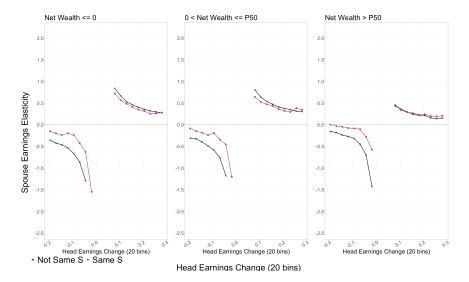


# By Age Groups: Household Consumption



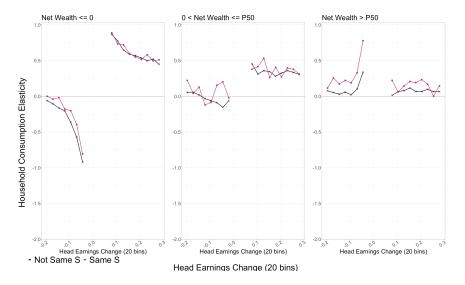
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# By Wealth Groups: Spousal Earnings



Busch, Madera & Groes (LMU, SMU & CBS): Correlated Risks

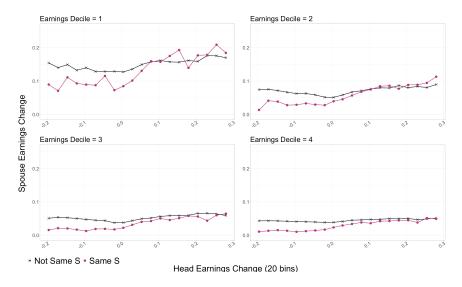
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► Change

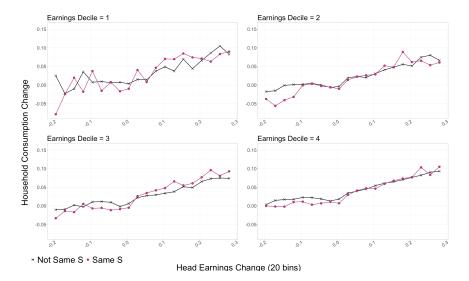
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## By Recent Income Groups: Spousal Earnings





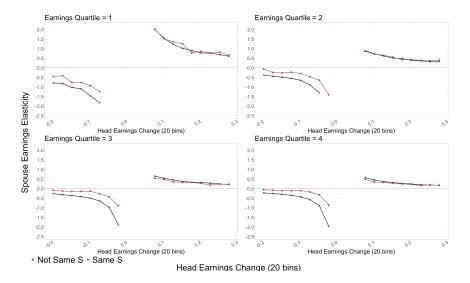
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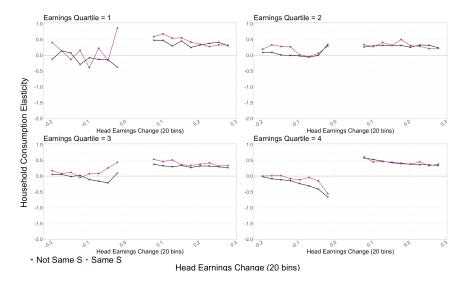
## By Recent Income Groups: Spousal Earnings





Busch, Madera & Groes (LMU, SMU & CBS): Correlated Risks

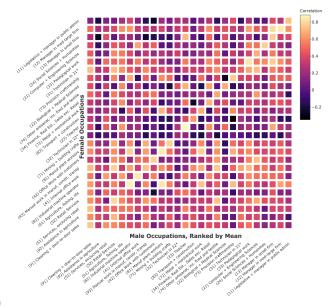
## By Recent Income Groups: Household Consumption





Busch, Madera & Groes (LMU, SMU & CBS): Correlated Risks

#### 676 Underlying Occupation Pairs



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