INCOME DYNAMICS OF COUPLES: CORRELATED RISKS AND HETEROGENEOUS WITHIN-HOUSEHOLD INSURANCE

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#### Motivation

- HH earnings risk matters for
  - Fiscal Policy: private vs. public insurance (e.g., Wu & Krueger)
  - Monetary Policy: MPCs (e.g., Bardóczy '20)
    - Macro models w/ micro data: bachelor household (e.g., HSV '10) "Wages and hours worked are characteristics recorded at the individual level, while consumption and welfare are typically measured at the level of the household. This presents an obvious challenge for the bachelor model as a lens for interpreting micro data".
- ▶ how does individual labor market risk  $\xrightarrow{?}$  household earnings risk
- and why does it matter?

Overview



#### Overview



Layers of "insurance" against individual income risk:

 $\rightarrow$  Household  $\rightarrow$  Assets  $\rightarrow$  Taxes/Transfers

Overview



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#### Here: zoom on link Individual $\longrightarrow$ Household Earnings

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► Focus: earnings co-variation of earners within a HH

# Joint Income Dynamics (in the 21st century)

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  - ► HH-insurance: **out-of-LF female** reacting to male income shock
  - Measurement: stably married HHs or treat new HH as independent
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- ! But...
  - ► Female labor force participation ↑ in most countries
    - Especially married women (e.g., Olsson '20)
  - Same time: divorce and formation of new couples
    - on avg. 2.5 spouses / individual in our sample
- $\Rightarrow$  Key role of

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  - ► Female labor force participation ↑ in most countries
  - Same time: divorce and formation of new couples
- $\Rightarrow$  Key role of
  - 1. Correlation of spouses' incomes (risk)
    - Sorted by: education, occupation, industry, firm, ...
  - 2. HH formation/dissolution over the life-cycle

# This Paper

Characterize earnings dynamics:

- > at individual level, for all adult individuals
- + family changes over the life-cycle
  - $\Rightarrow$  HH earnings dynamics

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- ▶ in Denmark: high female LF participation throughout

Document:

- Systematic heterogeneity in earnings co-movement of spouses
  - linked to sorting in labor market
- Heterogeneous pass-through to consumption

borrows from micro estimations:

e.g. param. of dynamic earnings/wage process using panel data

$$\begin{split} \mathbf{y}_{t}^{i} = & \mathbf{z}_{t}^{i} + \varepsilon_{t}^{i} \\ \mathbf{z}_{t}^{i} = & \mathbf{z}_{t-1}^{i} + \eta_{t}^{i} \\ \varepsilon_{t}^{i} \sim & \textit{iid}\mathcal{N}, \eta_{t}^{i} \sim & \textit{iid}\mathcal{N} \end{split}$$

We argue: empirical analysis often at odds with quant. question

- Common assumption 1: unit of obs. is either head OR family
- Common assumption 2: couples are stable

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- Common assumption 1: unit of obs. is either head OR family
- Common assumption 2: couples are stable
- $\Rightarrow$  Spouses' behavior is masked and a source of risk eliminated

Busch, Madera & Groes (LMU, SMU & CBS): Correlated Risks

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BPS estimate a process similar to this on a "stable" sample

- Find significant  $\sigma_{\varepsilon\varepsilon} > 0$ , insignificant  $\sigma_{\eta\eta}$
- Now: Households heterogeneous in sorting + not "stable"
  - $\rightarrow\,$  Look at comovement of earnings with flexible tools
  - $\rightarrow$  Enrich the process by **heterogeneity**

### Outline

# Data: Danish tax register & social security

- ▶ Whole Danish population panel 1991–2018
- Links individuals (couples)
- Info on:
  - Age, education, occupation, sector, firm
  - Earnings: total annual labor earnings
  - Taxes, transfers, assets
- (coming up) social security affiliation details for period 2008-2018
  - monthly
  - more details on extensive margin
- Sample for analysis: working age 18-65

# Danish Population and Sample



#### **Example: Occupation Pairs**



Interactive Version

# Sorting Coefficient Across Occupation-Pairs



## Taking Stock

- We use the whole adult Danish population
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- ▶ Next: are these couples different in terms of HH income risk?

### Outline

#### Income Changes in the Data

- Let Y<sub>it</sub> denote the labor earnings of individual i
- We define two types income changes

Arc Changes

$$\Delta^{arc} y_{it} = \frac{Y_{it+1} - Y_{it}}{\left(Y_{it+1} + Y_{it}\right)/2}$$

- Useful to incorporate both intensive and extensive margins
- Iimitations when linking to structural decomposition

#### Log Changes

$$\Delta y_{it} = \log Y_{it+1} - \log Y_{it}$$

- Useful for interpretation of intensive margin + structural decomp.
- limitations when extensive margin changes (0s)

# The Distribution of Everyone's Income Changes

Arc Changes, All Individuals

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# The Distribution of Joint Income Changes

All Changes, All Individuals, Sorting by Occupation

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Consider log earnings changes of head and spouse:

$$\Delta y_t^{sp} = f(\Delta y_t^{hd}) \tag{1}$$

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Specify  $f(\cdot)$  flexibly:

- 1. Non-linear in  $\Delta y_t^{hd}$
- 2. Heterogeneity by similarity of labor market characteristics
  - Education, Occupation, Industry, Firm
- 3. Other sources of heterogeneity
  - Age, Wealth
  - #Children

## Measures of Spousal Earnings Comovement

Implied spousal earnings changes for each group

$$\hat{\Delta y}_t^{sp} = f(\Delta y_t^{hd}; \hat{\beta}) \tag{2}$$



$$\hat{\epsilon}^{sp} = \frac{\hat{\Delta y}_t^{sp}}{\Delta y_t^{hd}}$$

(3)

# Spousal Change




Busch, Madera & Groes (LMU, SMU & CBS): Correlated Risks



(c) Spousal Change: Step-by-Step

Household

Busch, Madera & Groes (LMU, SMU & CBS): Correlated Risks





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### Implied Spousal Earnings Elasticity



(d) Spousal Elasticity

### Heterogeneity by Other Characteristics

- Role of labor market sorting by:
  - Age
  - Wealth (before change)

(cash+deposits+stocks+shares+property+cars-liabilities)

 $\Rightarrow$  Sorting matters within groups

### By Age Groups: Spousal Earnings





# By Wealth Groups: Spousal Earnings







### Outline

### From Income To Consumption

$$C = Y - T - \Delta A \tag{4}$$

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#### Components of budget in data:

- Y: Labor + capital income (+imputed cons. value housing)
- T: Tax payments transfer receipts

#### ΔA: Change asset value

(cash+deposits+stocks+shares+property+cars-liabilities)

### ⇒ Consumption

Lines up with Expenditure Survey

(De Giorgi, Frederiksen & Pistaferri, ReStud'20)

### Household Consumption Change

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(d) Consumption Change

### **Consumption Elasticities**

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### **Taking Stock**

- $\blacktriangleright$  Couples in  $\sim$  occupations/sectors: correlated earnings  $\Delta$
- $\blacktriangleright$  Especially in the case of negative earnings  $\Delta$
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- $\blacktriangleright$  Couples in  $\sim$  occupations/sectors: correlated earnings  $\Delta$
- Especially in the case of negative earnings  $\Delta$
- Passes through to family consumption...
- Incorporate heterogeneity in income process
   ... allows to decompose permanent vs. transitory fluctuations

## A Household Income Process for Macro Analysis

Estimate process for all individuals (singles/couples) which features

- 1. Individual-level income process (separately for men&women)
  - Couple-level corr of shocks, heterogeneous by sorting groups
- 2. Process of 'marriage' and 'divorce'
  - Assume marriage/divorce shocks & income shocks orthogonal

### An Income Process for All Households

At every age, each **single or married** male and female:

- receives (permanent and transitory) shocks to income
- and to family status

If **single**:

▶ form a couple with probability p<sup>form</sup>

### If in couple:

- divorce with probability p<sup>div</sup>:
  - income shocks correlated with outgoing spouse's shocks
  - AND receive divorce shocks
- stay in the couple:
  - income shocks correlated with spouse's shocks

*i* = spouse 1, 2

$$y_t^i = z_t^i + \varepsilon_t^i$$
  

$$z_t^i = z_{t-1}^i + \eta_t^i$$
(5)

$$arepsilon_t^i \sim \mathcal{F}_{arepsilon}(\mathbf{0}, \sigma_{arepsilon, i}^2)$$
  
 $\eta_t^i \sim \mathcal{F}_{\eta}(\mathbf{0}, \sigma_{\eta, i}^2)$ 

$$y_t^i = z_t^i + \varepsilon_t^i + \delta_t^{\varepsilon_i} \cdot \mathbf{1} \{ div_t = 1 \}$$
  

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### $\triangleright$ Household dissolution $\rightarrow$ divorce shocks (extra *risk*)

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▷ Household dissolution → divorce shocks (extra *risk*)
 ▷ Household formation → correlation between spouses

(5)

### Estimation

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Estimate in first differences

GMM: analytical moments of individual processes

$$\begin{aligned} & \operatorname{var}(\Delta y_t^i | \operatorname{div}_t = \operatorname{div}_{t+1} = 0) = \sigma_{\eta i}^2 + 2\sigma_{\varepsilon i}^2 \\ & \operatorname{cov}(\Delta y_t^i, \Delta y_{t+1}^i | \operatorname{div}_t = \operatorname{div}_{t+1} = 0) = -\sigma_{\varepsilon i}^2 \\ & \operatorname{cov}(\Delta y_t^i, \Delta y_{t+1}^i | \operatorname{div}_{t+1} = 1) = -\sigma_{\varepsilon i}^2 - \sigma_{\delta \varepsilon i}^2 \\ & \operatorname{var}(\Delta y_t^i | \operatorname{div}_{t+1} = 1) = \sigma_{\eta i}^2 + \sigma_{\delta \eta i}^2 + 2\sigma_{\varepsilon i}^2 + \sigma_{\delta \varepsilon i}^2 \end{aligned}$$

... and co-moments by sorting status s:

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... and co-moments by sorting status s:

$$cov(\Delta y_t^1, \Delta y_t^2 | s_t = s; s_{t+1} = s') = \sigma_{\eta\eta}(s') + \sigma_{\varepsilon\varepsilon}(s) + \sigma_{\varepsilon\varepsilon}(s')$$
$$cov(\Delta y_t^1, \Delta y_{t+1}^2 | s_t = s; s_{t+1} = s') = -\sigma_{\varepsilon\varepsilon}(s')$$

# Couple formation Process (p<sup>form</sup>)



# Divorce Process (*p<sup>div</sup>*)



### Estimates

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Individual Moments		
	Income $(\varepsilon, \eta)$	+ if divorce $(\delta_{\varepsilon}, \delta_{\eta})$
$\sigma_{\varepsilon}^{2}$	0.102	0.130
$\sigma_{\eta}^2$	0.272	0.205

Table: Estimates, Sorting Along Occupations

▶ BPS estimates are (for wages)  $\sim \sigma_{\varepsilon}^2 = 0.02, \sigma_{\eta}^2 = 0.03$ 

### Estimates

Couples' Moments		
	Covariances	Implied Correlations
$\sigma_{arepsilonarepsilon}(s=1)$	-0.003	-0.027
$\sigma_{arepsilonarepsilon}(oldsymbol{s}=oldsymbol{0})$	-0.009	-0.081
$\sigma_{\eta\eta}(s=1)$	0.044	0.159
$\sigma_{\eta\eta}(s=0)$	0.015	0.054
$\sigma_{\delta_arepsilon,\delta_arepsilon}$	0.011	0.092
$\sigma_{\delta_\eta,\delta_\eta}$	0.043	0.206

Table: Estimates, Sorting Along Occupations

#### ► 3 × higher correlation in permanent shocks

# Ongoing

- Increase in life-cycle increase  $\log y_t$  with our process?
  - For males and females
- Quantify relative roles of sources of risk
  - Individual lifetime risk: role of divorce risk
  - Household risk: role of sorting (given evidence on corr. risk)

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  - 1. Statistical decomposition
  - 2. Structural model (future)

### Outline

### Summary

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  - $\rightarrow~$  Translates to household outcomes: consumption

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  - ightarrow Holds within groups of age, wealth
  - $\rightarrow$  Translates to household outcomes: consumption
- Structurally, correlated risk shows up in the permanent component of earnings changes
- In a full model, this component passes through to consumption and welfare



### Next: Quantitative Model

- Sorting/distribution of couples matters for
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  - Within-household insurance ("added worker effect")
  - Evaluation of public insurance
- Model featuring:
  - Incomplete markets
  - Distribution of couples over pairs of occupation
  - Head earnings process; Spouse wage process
    - $\longrightarrow$  Endogenous labor supply of spouse
  - Tax & transfer function

Joint Dynamics: Average by Group

Spousal income changes:

$$\Delta y_t^{sp} = \beta_0 + \tilde{f}(\Delta y_t^{hd}) + \mathbf{X}_t^{sp} \gamma + \mathbf{Y}\delta + u_{st}$$
(6)

with

$$\tilde{f}(\Delta y_t^{hd}) = \left(I_{o_t^{hd} \neq o_t^{sp}} \beta^{\text{not same } x} + I_{o_t^{hd} = o_t^{sp}} \beta^{\text{same } x}\right) \Delta y_t^{hd}$$
(7)

>  $\mathbf{X}_{t}^{sp}$ : age quadratic, education dummies, occupation dummies

- ► Y: year dummies
- $\Delta y_t^i$ : 1-year income change

### Group-Specific Coefficients



(g) Elasticities for Different Sorting Vars



Busch, Madera & Groes (LMU, SMU & CBS): Correlated Risks

### Group-Specific Coefficients: By Education Pairs



(h) Elasticities-Educ⊗Sorting Var



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(i) Household Change: Step-by-Step

Household Elasticity



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Household Elasticity

## By Age Groups: Spousal Earnings



Head Earnings Change (20 bins)



## By Age Groups: Household Consumption



## By Wealth Groups: Spousal Earnings



# By Wealth Groups: Household Consumption



### By Recent Income Groups: Spousal Earnings



Elasticity

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### By Recent Income Groups: Household Consumption





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#### 676 Underlying Occupation Pairs





Negative Extensive Changes, All Individuals

Negative Extensive Changes, All Individuals



Positive Extensive Changes, All Individuals

Positive Extensive Changes, All Individuals

