

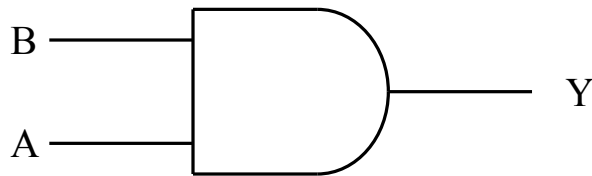
Gate Delay

- Transistors within a gate require finite amount of time to switch
- Change on Gate Input Requires finite amount of time for Output to Change
- This time is known as **Propagation Delay**
 - nominal delay
 - min/max delay
 - load conditions
- Smaller transistors have faster switching times
- Semiconductor companies are continually finding new ways to make transistors smaller
- Result is:
 - transistors are faster
 - more can fit on a die in the same area.

Propagation Delay Definitions

- t_{plh} - time between a change in an input and a low to high change on the output
 - The 'lh' part (low to high) refers to OUTPUT change, NOT input change
- Measured from 50% point on input signal to 50% point on the output signal
- t_{phl} - time between a change in an input and a high to low change on the output
 - The 'hl' part (high to low) refers to OUTPUT change, NOT input change
- Measured from 50% point on input signal to 50% point on the output signal

Propagation Delay (non inverting)



Each Input to Output path has its own delay:

$$A \rightarrow Y t_{plh}, A \rightarrow Y t_{phl}, B \rightarrow Y t_{plh}, B \rightarrow Y t_{phl}$$

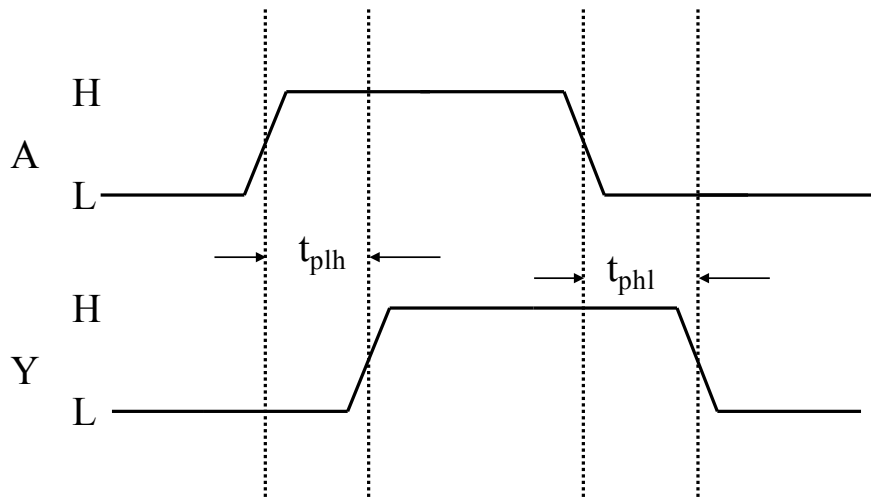
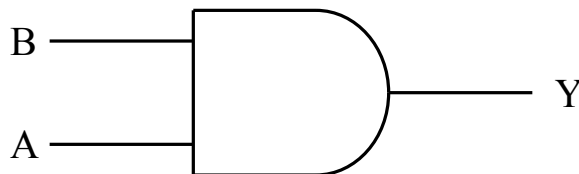
These delays can be different

For simplicity, may just assign one delay for entire gate:

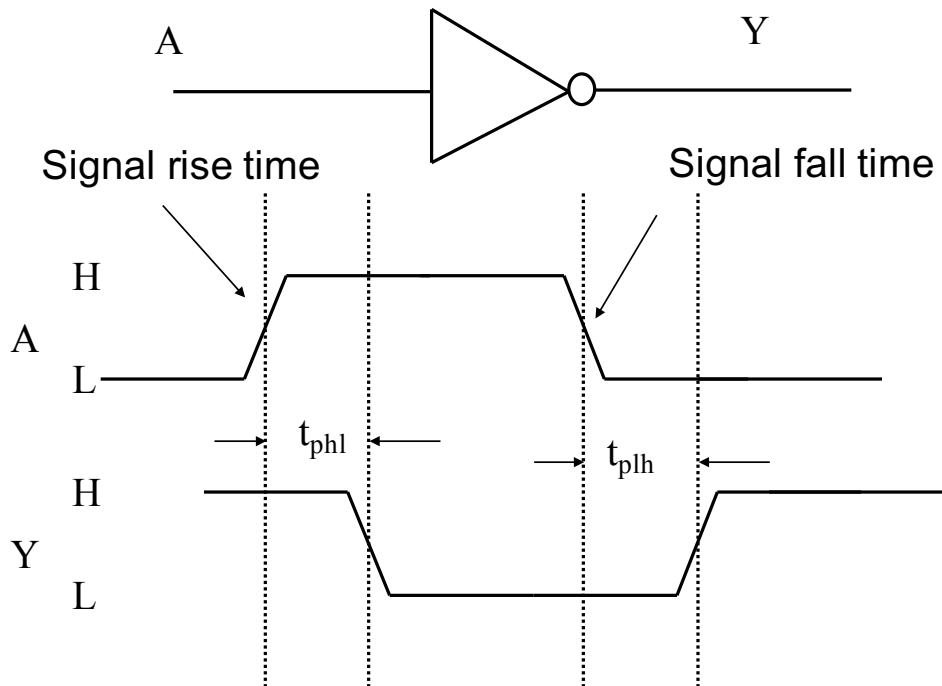
$$Y t_{pd}$$

Databooks give typical and maximum propagation delays for combinational outputs

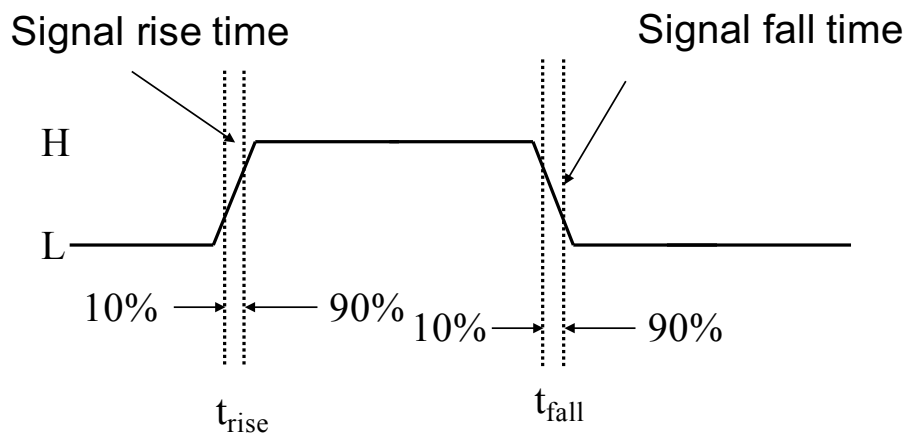
Propagation Delay (non inverting)



Propagation Delay (inverting)



Rise/Fall Time

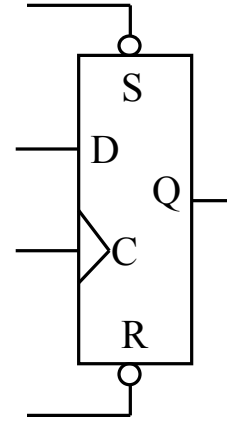


- Time from 10% of Steady State Value to 90% of Steady State Value

- Sometimes 20-80% Thresholds used

DFF Timing

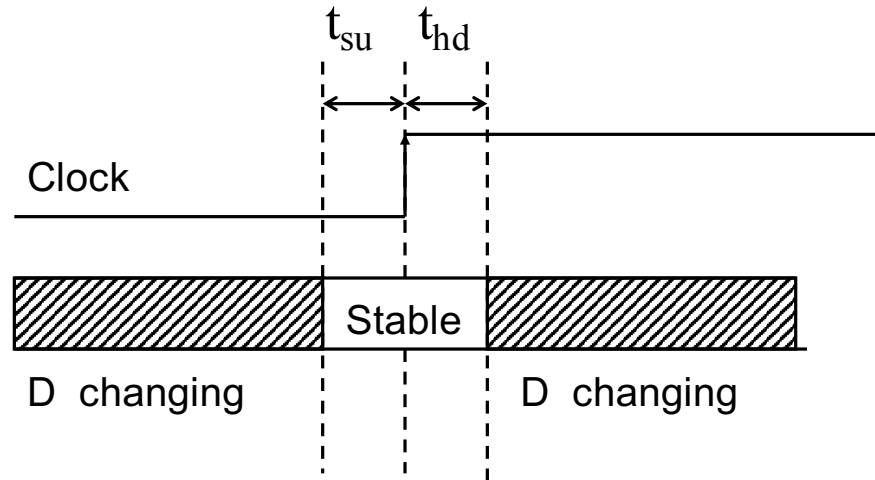
- Propagation Delay
 - t_{C2Q} : Q will change some propagation delay after change in C. Value of Q is based on D input for DFF.
 - t_{S2Q} , t_{R2Q} : Q will change some propagation delay after change on S input, R input
 - Note that there is NO propagation delay t_{D2Q} for DFF!
 - D is a Synchronous INPUT, no prop delay value for synchronous inputs



Setup, Hold Times

- Synchronous inputs (e.g. D) have Setup, Hold time specification with respect to the CLOCK input
- Setup Time: the amount of time the synchronous input (D) must be *stable before* the active edge of clock
- Hold Time: the amount of time the synchronous input (D) must be *stable after* the active edge of clock.

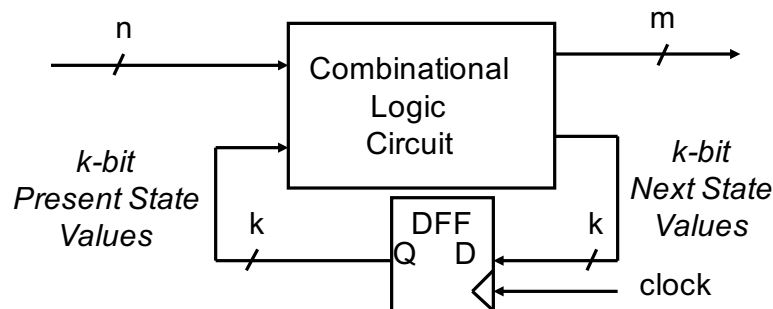
Setup, Hold Time



If changes on D input violate either setup or hold time, then correct FF operation is not guaranteed (*metastability*).

Setup/Hold measured around active clock edge

Sequential System Timing



Question: What is the MAXIMUM frequency of operation of this system?

Maximum Frequency = $1 / (\text{longest delay path})$

What are longest paths???

Longest Delay Paths in Sequential System Diagram

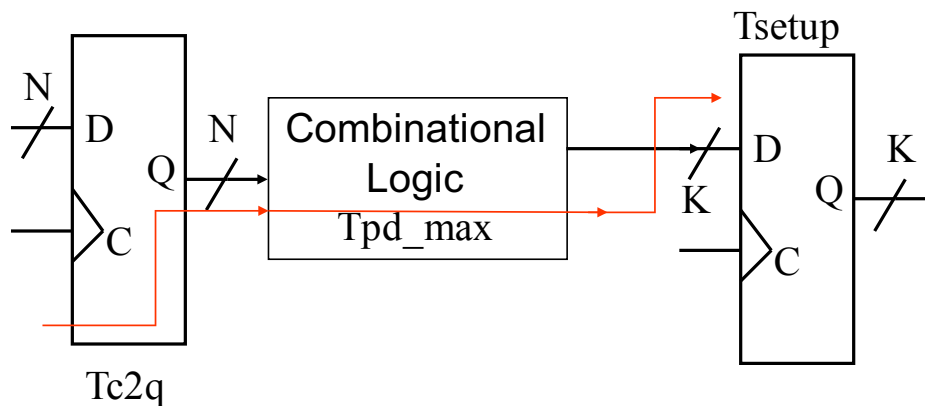
Three types of Paths to check:

- A. Clock to Output delay: $T_{c2q} + T_{comb_Q2O_max}$
 T_{comb_Q2O} is longest path from Q output to any output
- B. Register to Register delay: $T_{c2q} + T_{comb_Q2D_max} + T_{setup}$. T_{comb_Q2D} is longest path from Q dff output to D dff input
- C. Pin to Pin combinational delay: $T_{comb_I2O_max}$
(input pin to output pin, no intervening registers)

Typically, paths of type "B" are the worst cases.

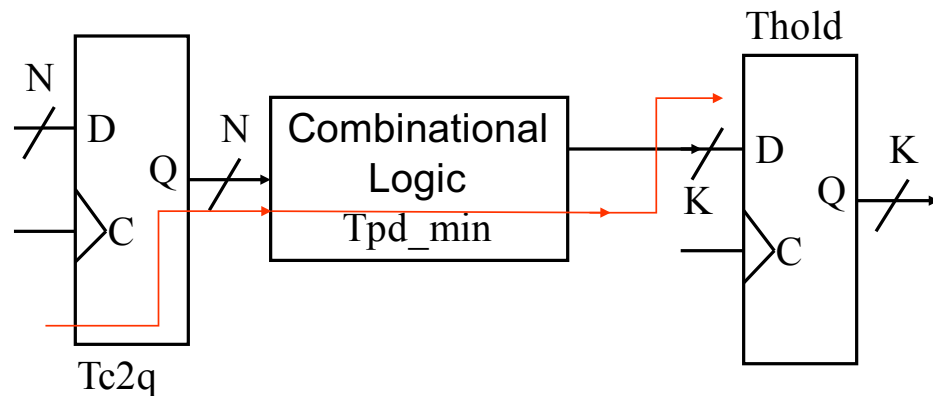
Inputs/Outputs Registered

Very often, all inputs and outputs are registered. Then register-to-register delay will almost always determine maximum frequency.



$$\text{delay} = T_{c2q} + T_{pd_max} + T_{setup}$$

Hold Time and Shortest Paths

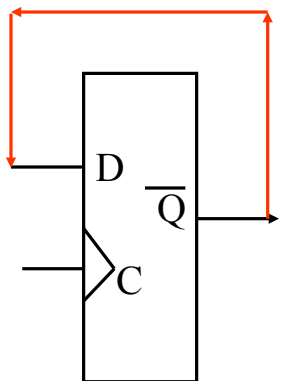


To satisfy hold time:

$$T_{c2q} + T_{pd_min} \geq T_{hold}$$

This is normally easily satisfied in a sequential system.

Toggle Frequency



$$\text{toggle frequency} = 1 / (T_{c2q} + T_{setup})$$

assume wire delay is negligible

What about setup time?

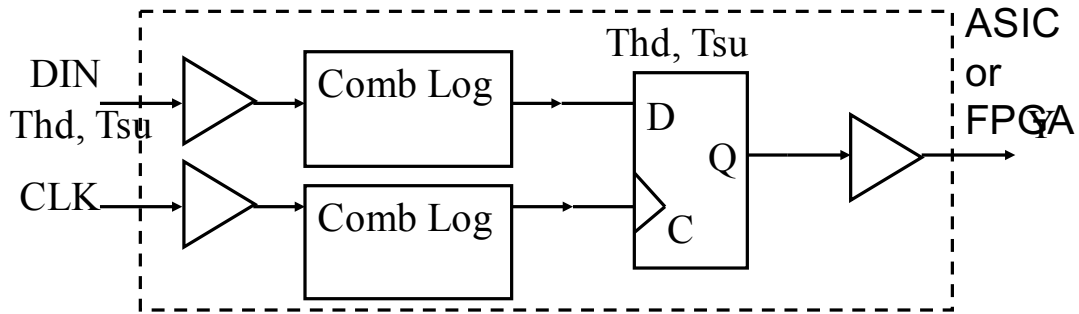
$$T_{c2q} + T_{pd_min} \geq T_{hold}$$

$$T_{c2q} > T_{hold}$$

assuming zero wire delay

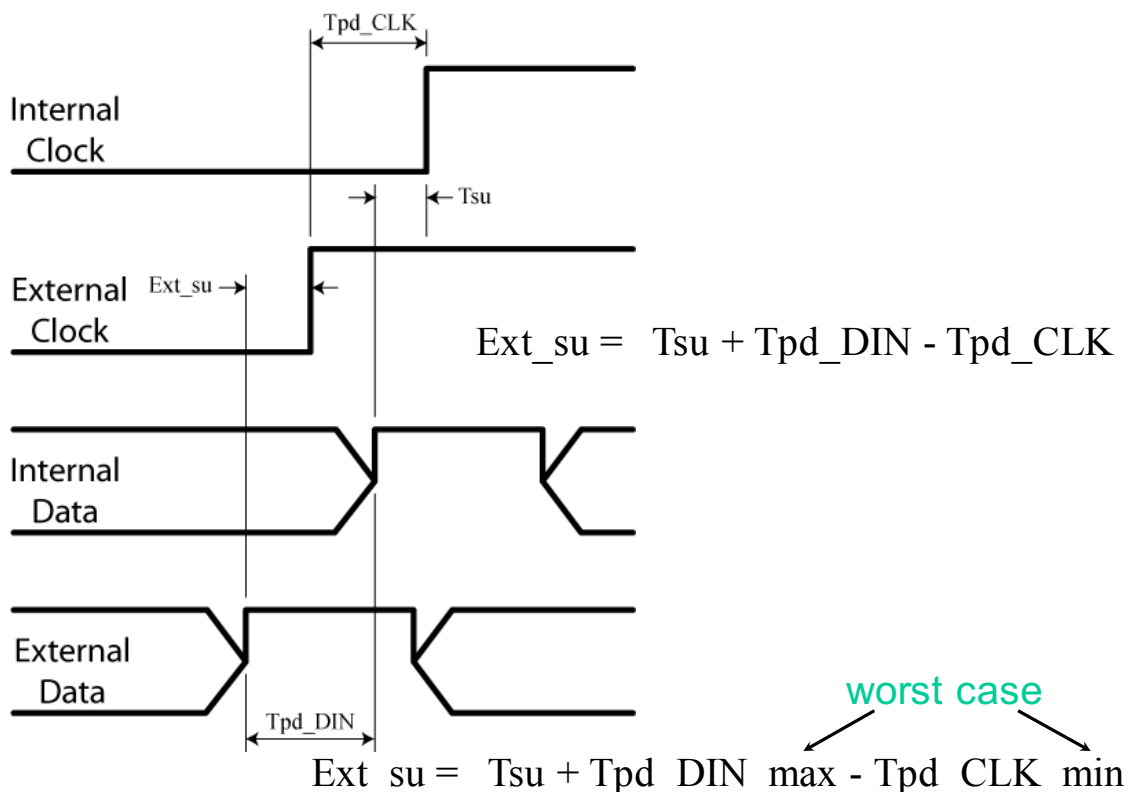
Setup, Hold Time for External Inputs

External inputs are buffered through pad drivers and may go through combinational logic before they reach a synchronous input. This buffering adds propagation delay. How does this propagation delay affect the EXTERNAL setup and hold time????

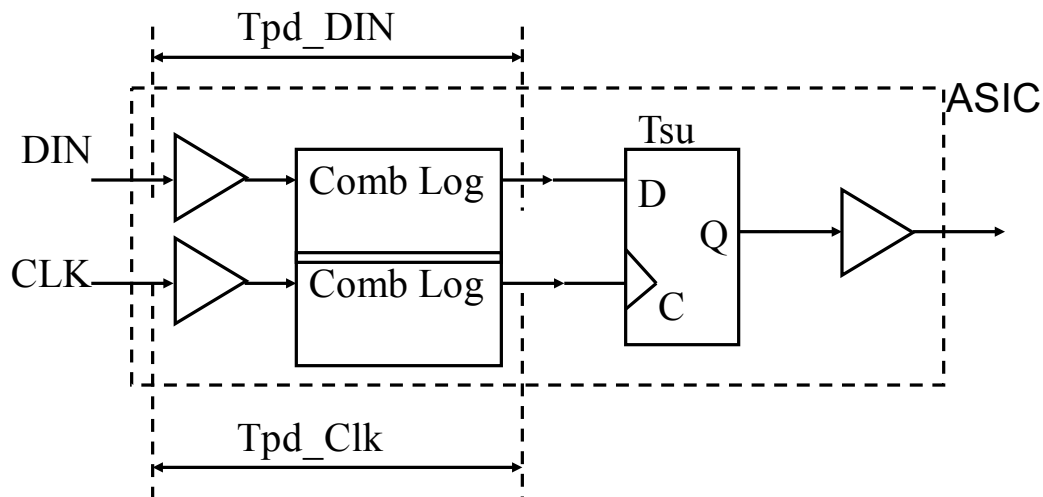


What is Thd, Tsu for DIN? It is NOT the same as for Thd, Tsu of the internal DFF!!!!!! Thd, Tsu for DIN is specified in the DATASHEET for design.

External Setup times



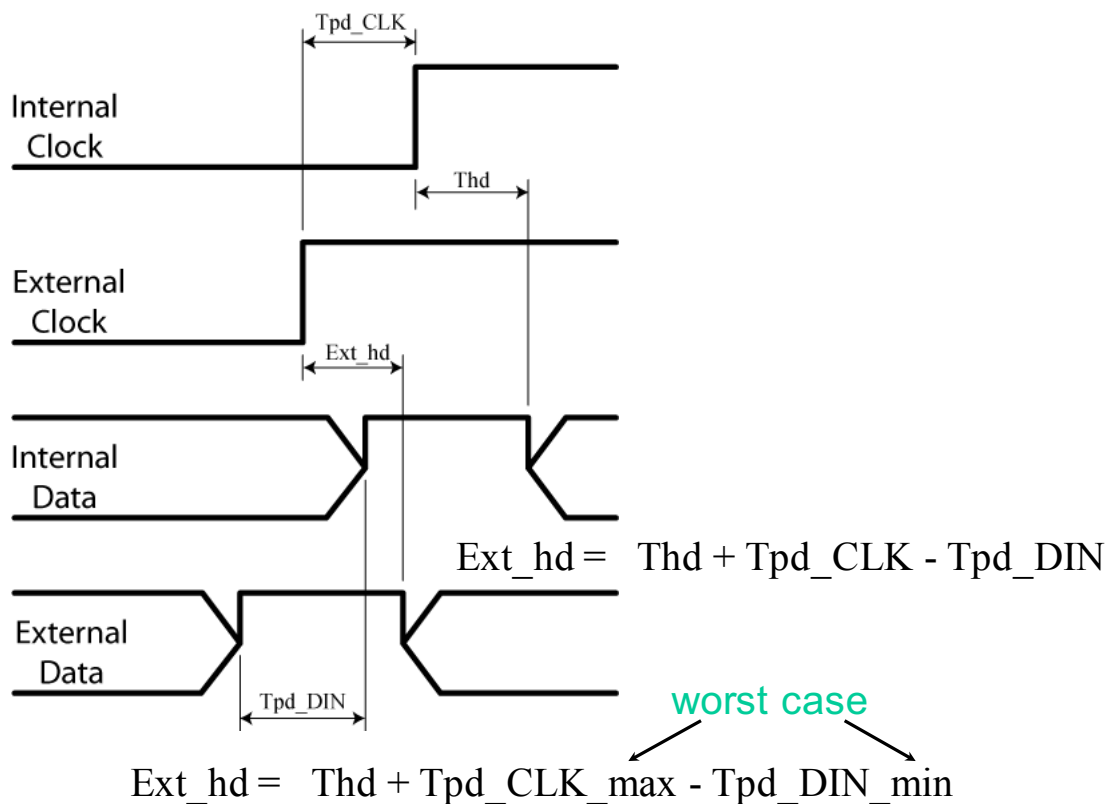
Calculating External Setup times



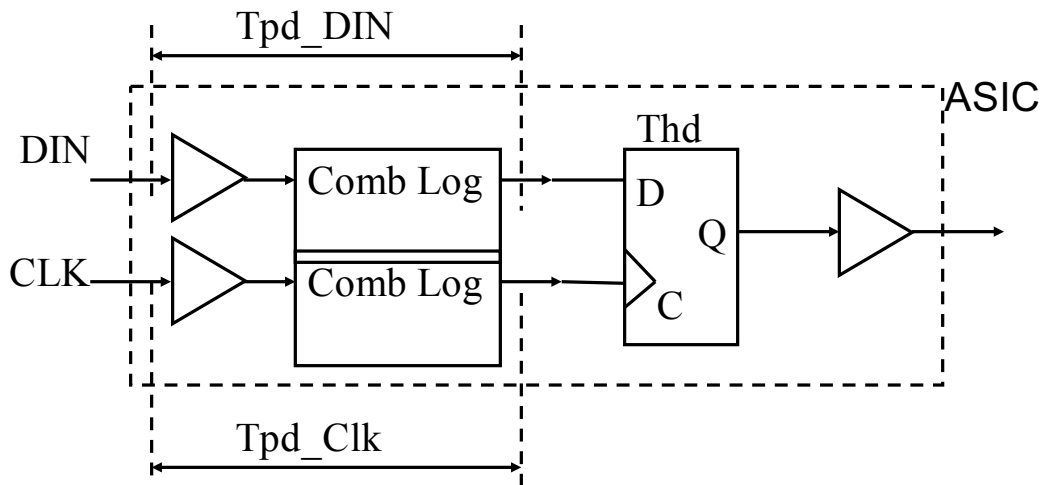
Worst case setup time for DIN occurs when 'DIN' is **DELAYED** relative to CLK. Means clock edge arrives early, requiring DIN to be ready sooner.

$$Ext_su = T_{su} + T_{pd_DIN_max} - T_{pd_CLK_min}$$

External Hold times



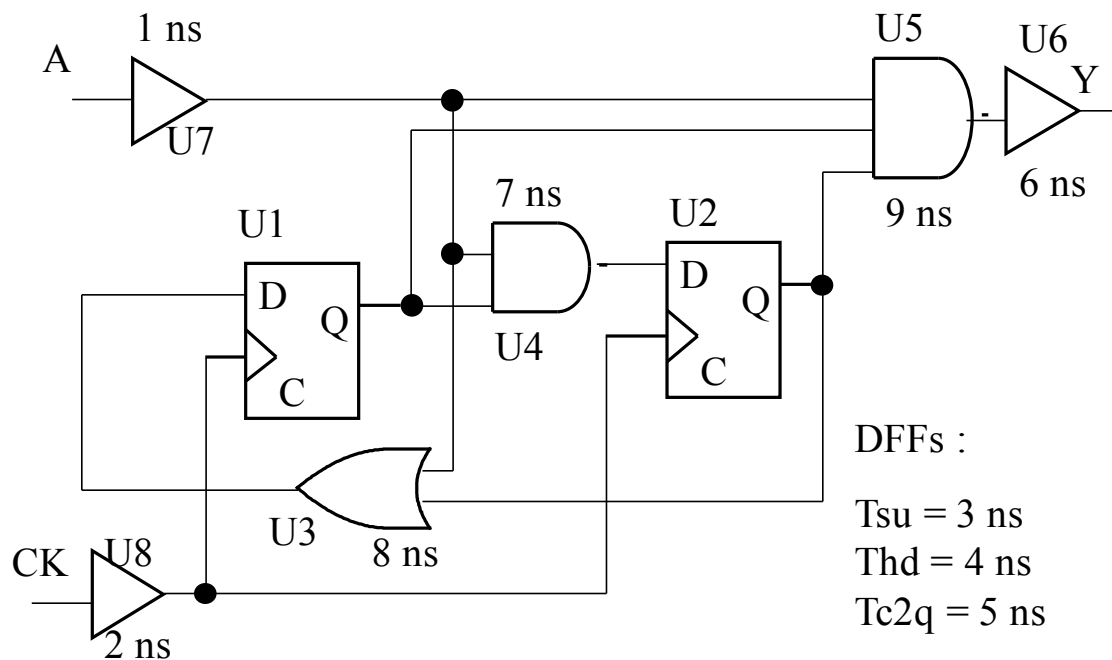
Calculating External Hold times



Worst case hold time for DIN occurs when 'CLK' is **DELAYED** relative to DIN. Means clock edge arrives late, requiring DIN to hold its value longer.

$$\text{Ext_hd} = \text{Thd} + \text{Tpd_CLK_max} - \text{Tpd_DIN_min}$$

A Timing Example



Timings

Max Register to Register Delay:

$$\begin{aligned} &= U2_Tc2q + U3_Tpd + U1_Tsu \\ &= 5 + 8 + 3 = 16 \text{ ns} \end{aligned}$$

$$\begin{aligned} A_setup_time &= Tsu + A2D_Tpd_max - Clk_Tpd_min \\ &= Tsu + (U3_Tpd + U7_Tpd) - U8_Tpd \\ &= 3 + (8 + 1) - 2 = 10 \text{ ns} \end{aligned}$$

$$\begin{aligned} A_hold_time &= Thd + Clk_Tpd_max - A2D_Tpd_min \\ &= Thd + U8_Tpd - (U4_Tpd + U7_Tpd) \\ &= 4 + 2 - (7 + 1) = -2 \text{ ns} \end{aligned}$$

Timings (Cont)

Clock to Out:

$$\begin{aligned} &= U8_Tpd + U2_Tc2q + U5_Tpd + U6_Tpd \\ &= 2 + 5 + 9 + 6 = 22 \text{ ns} \end{aligned}$$

Pin to Pin Combinational Delay (A2Y):

$$\begin{aligned} &= U7_Tpd + U5_Tpd + U6_Tpd \\ &= 1 + 9 + 6 = 16 \text{ ns} \end{aligned}$$

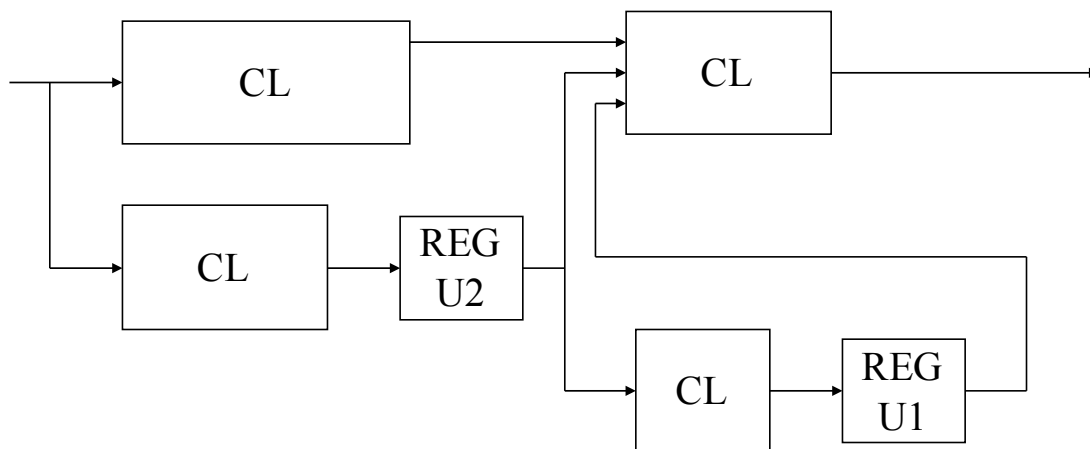
$$\begin{aligned} \text{Max Clock Freq} &= 1 / \text{Max}(\text{Reg2reg}, \text{Clk2Out}, \text{Pin2Pin}) \\ &= 1 / \text{Max}(16, 22, 16) \\ &= 1 / \text{Max}(16, 22, 16) \\ &= 45.5 \text{ Mhz} \end{aligned}$$

DataSheet

Parameter	Description	Min	Max	Units
Tclk	Clock Period	22		ns
Fclk	Clock Frequency		45.5	MHz
Atsu	A setup time	10		ns
Athd	A hold time	-2		ns
A2Y	A to Y Tpd		16	ns
Ck2Y	Clock to Y tpd		22	ns

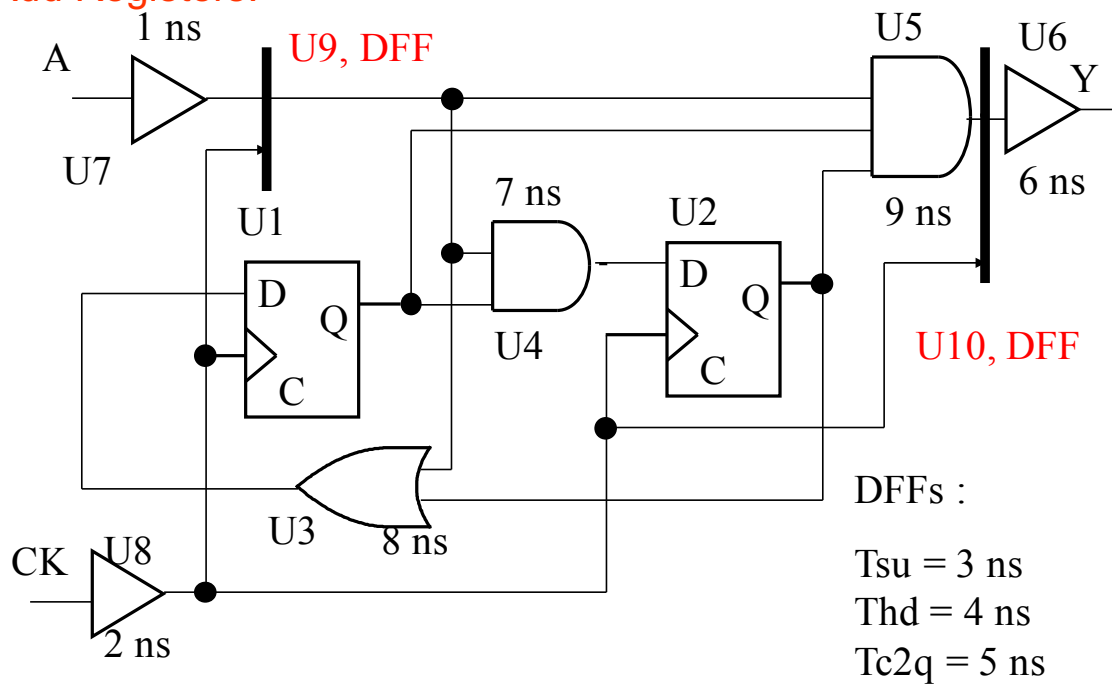
Negative hold times are typically specified as 0 ns

How do we improve timings?



How do we improve timings?

Add Registers!



New Timings

Max Register to Register Delay

$$U2_Tc2q + U5_Tpd + U10_Tsu = 5 + 9 + 3 = 17 \text{ ns}$$

$$A \text{ setup time} = T_{su} + A2D_Tpd_max - Clk_Tpd_min$$

$$A \text{ hold time} = T_{hd} + Clk_Tpd_max - A2D_Tpd_min$$

New Timings

Max Register to Register Delay

$$U2_Tc2q + U5_Tpd + U10_Tsu = 5 + 9 + 3 = 17 \text{ ns}$$

$$\begin{aligned} \text{A setup time} &= Tsu + A2D_Tpd_max - Clk_Tpd_min \\ &= Tsu + (U7_Tpd) - U8_Tpd \\ &= 3 + (1) - 2 = 2 \text{ ns} \end{aligned}$$

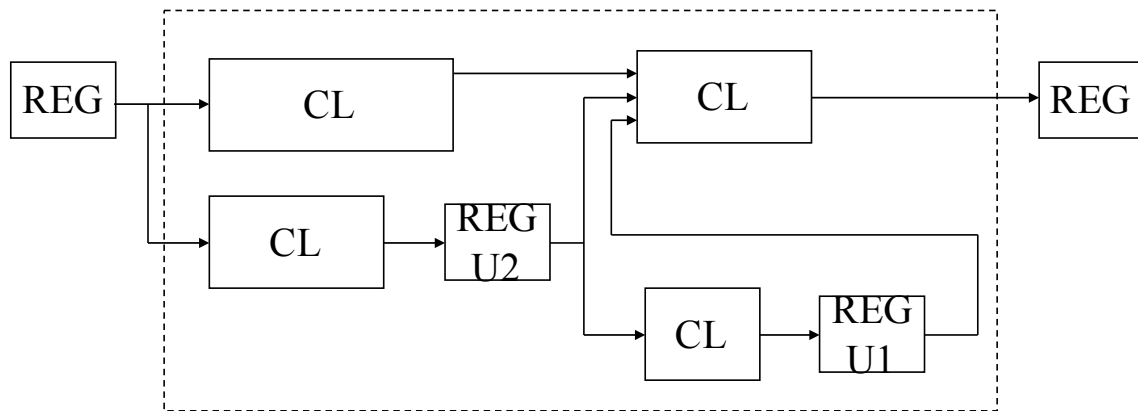
$$\begin{aligned} \text{A hold time} &= Thd + Clk_Tpd_max - A2D_Tpd_min \\ &= Thd + U8_Tpd - (U7_Tpd) \\ &= 4 + 2 - (1) = 5 \text{ ns} \end{aligned}$$

New DataSheet

Parameter	Description	Min	Max	Units
Tclk	Clock Period	17		ns
Fclk	Clock Frequency		58.8	MHz
Atsu	A setup time	2		ns
Athd	A hold time	5		ns
Ck2Y	Clock to Y tpd		13	ns

Most designs have all inputs, outputs registered.

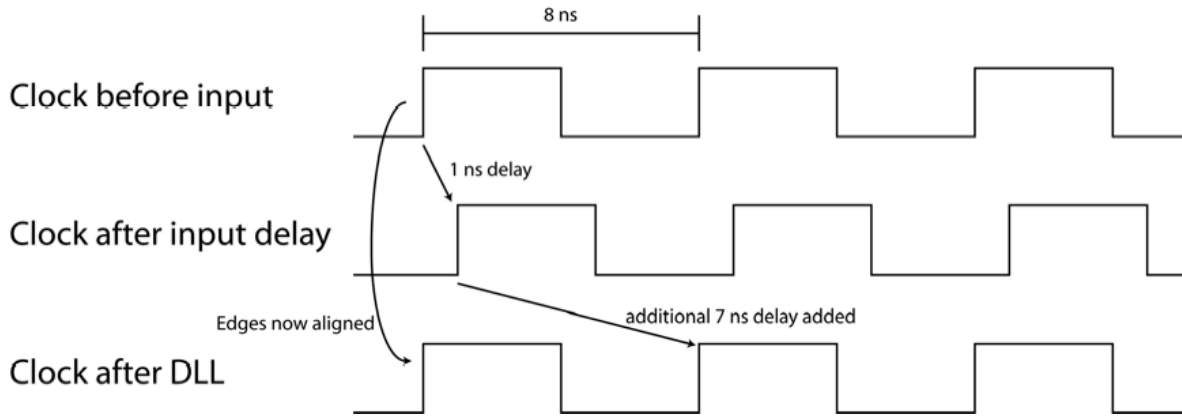
How do we improve timings?



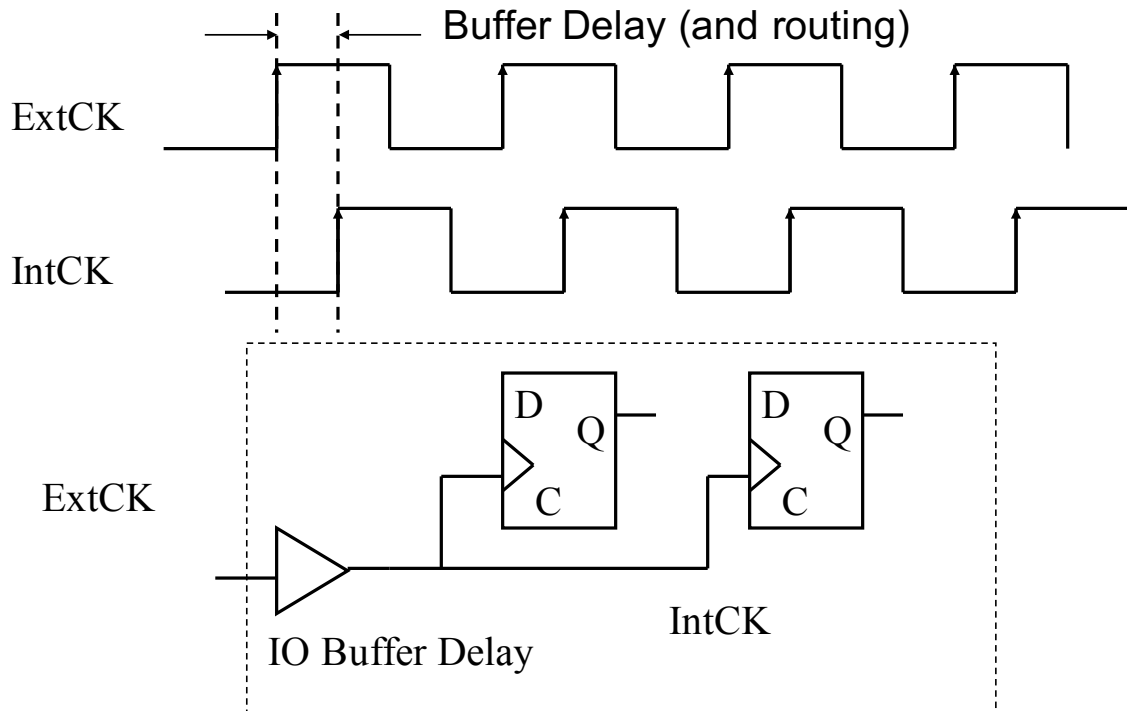
How does a PLL/DLL help?

- A Phased Locked Loop or Delay Locked Loop circuit is used to align the external clock edge at the pin with the internal clock edges at the DFF clk pins
 - Some clock skew due to clock routing network from PLL will still be present, but input buffer delay eliminated.
- PLLs and DLLs differ but we will consider them the same for this course
- This means that we can drop out the Clk_Tpd term from the equations
- **How does this change things?**

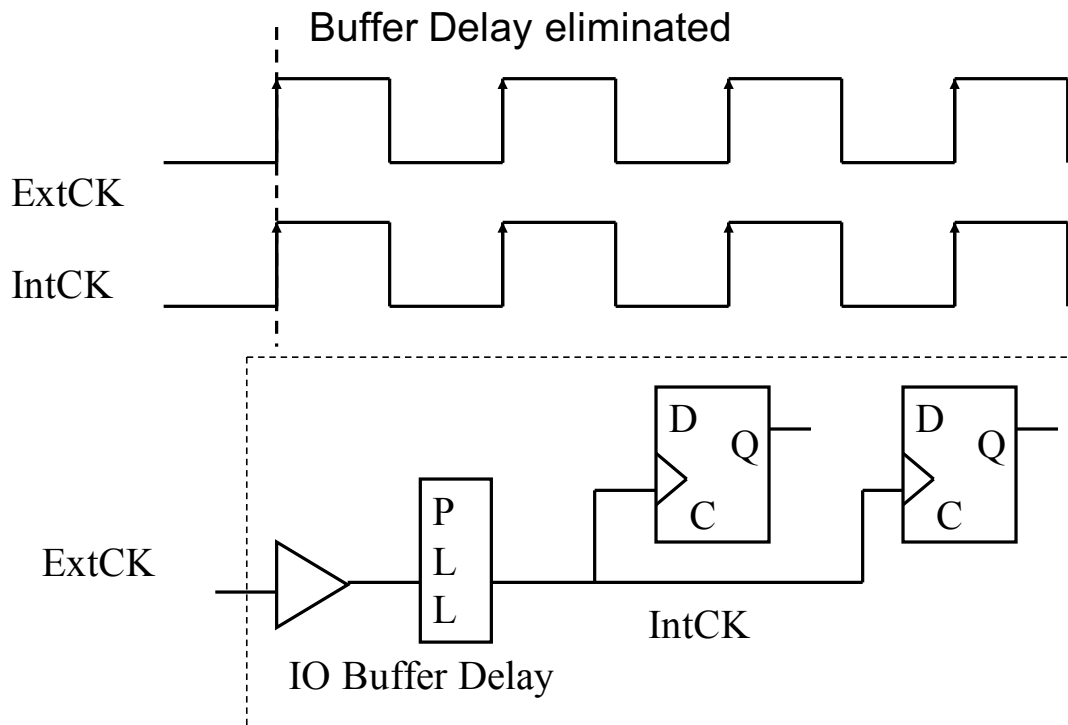
DLL Example



Without PLL



With PLL



New Timings (PLL, Inputs/Outputs Reg)

Max Register to Register Delay:

$$U2_Tc2q + U5_Tpd + U9_Tsu = 5 + 9 + 3 = 17 \text{ ns}$$

$$\begin{aligned} \text{A setup time} &= Tsu + A2D_Tpd_max - Clk_Tpd_min \\ &= Tsu + (U7_Tpd) - 0 \text{ (due to PLL)} \\ &= 3 + (1) - 0 = 4 \text{ ns} \end{aligned}$$

$$\begin{aligned} \text{A hold time} &= Thd + Clk_Tpd_max - A2D_Tpd_min \\ &= Thd + 0 \text{ (due to PLL)} - (U7_Tpd) \\ &= 4 + 0 - (1) = 3 \text{ ns} \end{aligned}$$

New Timings (PLL, Inputs/Outputs Reg)

Clock to Out:

$$\begin{aligned} &= U8_Tpd + U9_Tc2q + U6_Tpd \\ &= 0 \text{ (due to PLL)} + 5 + 6 = 11 \text{ ns} \end{aligned}$$

NO pin to Pin combinational delay! All inputs/outputs registered!

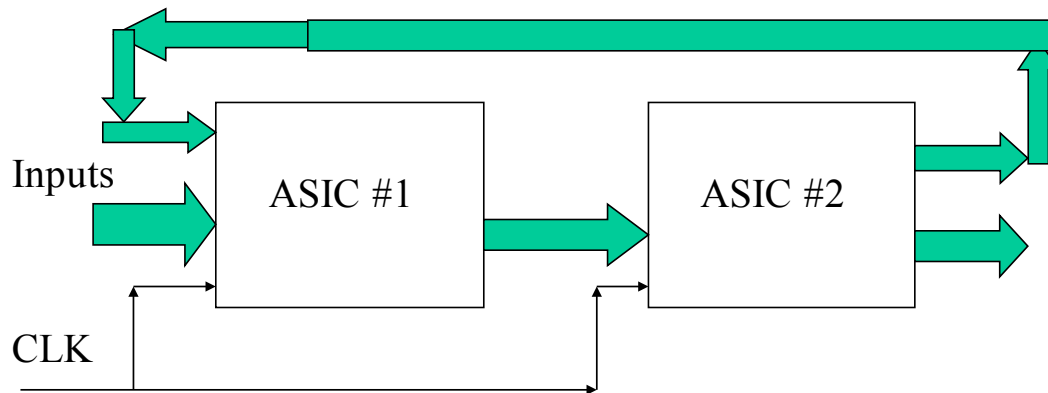
$$\begin{aligned} \text{Max Clock Freq} &= 1 / \text{Max}(\text{Reg2reg}, \text{Clk2Out}, \text{Pin2Pin}) \\ &= 1 / \text{Max}(17, 11, 0) \\ &= 58.8 \text{ MHz} \end{aligned}$$

New DataSheet (PLL, Inputs/Outputs Reg)

Parameter	Description	Min	Max	Units
Tclk	Clock Period	17		ns
Fclk	Clock Frequency		58.8	MHz
Atsu	A setup time	4		ns
Athd	A hold time	3		ns
Ck2Y	Clock to Y tpd		11	ns

Clock to Output improved; important in multiple chip designs.
External Setup/Hold times closer to setup/hold times of internal DFFs.

Chip to Chip Timing Calculation



Need to know external setup/hold times all inputs, clk to out of all outputs, all pin to pin combinational delays.

ASIC = Application Specific Integrated Circuit

Max Register to Register Delay 2 ASIC System

Assume no pin to pin combinational delays and that inputs/outputs of both ASICs are registered.

For any outputs from ASIC #1 which are Inputs to ASIC #2 find maximum of ASIC #1 Clk to out + ASIC#2 Setup time.

For any outputs from ASIC #2 which are Inputs to ASIC #1 find maximum of ASIC #2 Clk to out + ASIC#1 Setup time.

The maximum of these two times will be the minimum clock period.

Other Factors that effect Timing

- Voltage: the higher the voltage, the faster that gates switch
- Temperature: the lower the temperature, the faster that gates switch
- Process Technology (transistor gate width). The shorter the transistor gate length, the faster the transistor will switch (I.e, 0.09μ process versus 0.045μ process).
- In a given process run, may get fast N transistors, fast P transistors, slow N transistors, slow P transistors

Device Characterization

- Do timing analysis on ASICs at four extreme corners to make sure they meet timing specs under all conditions
- Fastest Case: Fast N transistors, Fast P transistors, High Vdd, Low temperature
- Slowest Case: Slow N transistors, slow P transistors, low Vdd, high temperature
- Other two corners can vary but two possible corners are:
 - Fast N, Slow P, Typical Temperature
 - Slow N, Fast P, Typical Temperature

Speed Grades

- Databooks often list different **speed grades** for a part at the same temperature
- Simply test parts that come off the fabrication line and see how fast they are
 - Divide the parts into different speed bins
 - For three speed grades, a design goal might be to have 20% of your parts fall in the upper bin, 50% in the middle bin, and 25% in the lower bin.
 - As the process matures, more and more fabricated parts will move into the upper speed bin, at which point you make a new upper speed bin.
 - Obviously, faster parts cost more (and are more profitable)

Static Path Analysis

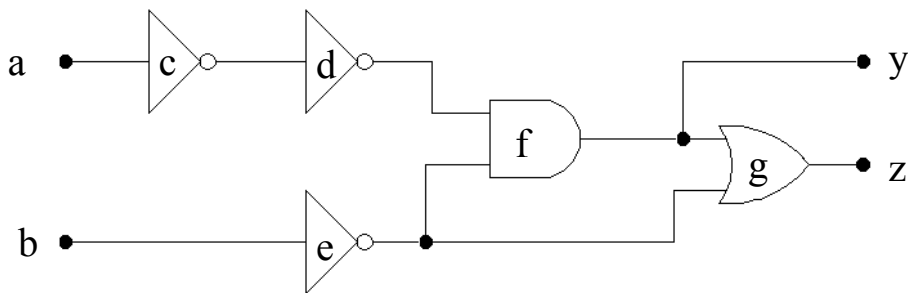
- After your gate netlist has been mapped to the FPGA, a timing analysis tool will analyze the paths in the design and compute the timings we have discussed
- The timing analyzer takes into account the routing delays in the physical routing and the speed grade of the part you have mapped to.
 - Because routing can sometimes change somewhat drastically for even small changes, often try run multiple device mappings to try to get a 'good route'.

Static Timing Analysis Reports

- The static timing analyzer will report the following times
 - Register to Register delays
 - Setup times of all external synchronous inputs
 - Clock to Output delays
 - Pin to Pin combinational delays
- The clock to output delay is sometimes reported as simply another pin-to-pin combinational delay
- Static Timing analysis reports are pessimistic since they use worst case conditions - **critical paths with simple delay models**
- Dynamic Timing analysis can be more accurate but are much more computationally intensive
- Many Dynamic Timing Analyzers use Assumptions to improve runtime that lead to optimistic delays

Critical Path Example

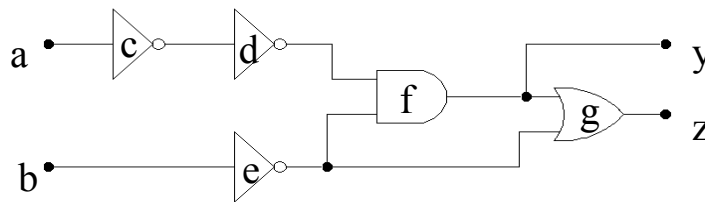
- Assume All Gates Have Unit Delay
- All Inputs Have Data Ready Time of 0
- Longest Topological Path is Critical Path in this Case



WHERE IS THE CRITICAL PATH???

Critical Path – Topology AND Logic

- Event: Transition of a Net from 0/1 or 1/0
- Problem is No Event Will Propagate Through Path
 $\{\dots, v_d, v_f, v_g, \dots\}$
- Output of v_e Must be “1” for Event to Propagate Through Vertex v_f
- Output of v_g Must be “0” for Event to Propagate Through Vertex v_g
- Impossible so $\{\dots, v_d, v_f, v_g, \dots\}$ is a **FALSE PATH**
- True Topological Critical Path is $\{v_a, v_c, v_d, v_f, v_y\}$



Delay Modeling Observations

- Some Static Analyzers use Delay Models Based on Circuit Topology and Finite Gate Delay (usually worst case) Only
- More Accurate to Consider False Paths and Delay Modeling Using Topology AND Logic
- **Finding False Paths Requires Logic Simulation** (for more than one test vector) or Other Means of Computation to do Timing Analysis
- Still an Estimate Since True Delay Also Depends on Subsequent Input Signal Changes
 - eg. Consider 3-input AND with Input Event 000/001 versus Event 000/111 (unequal settling time)

Timing Accurate Simulation

- The timings extracted by the Timing analysis tool (routing delays, gate delays for a particular speed grade, etc) are used in the simulation
- It may be tempting to ignore the delays reported by the timing analyzer, and simulate the design 'at speed' to see if it works.
 - If the design simulates correctly, only means that it works for the particular test vectors that you used!
 - Different test vectors exercise different delay paths - you must use test vectors that exercise the LONGEST paths
 - These test vectors can be difficult to find

Functional Simulation

- QuartusII Supports Functional Simulation
 - Can Simulate Logic BEFORE Mapping to Device
 - Allows for Debugging your Design Prior
 - to Technology Mapping
 - Comparing Functional to Timing Simulation
- Results can Give Information Regarding:
- Device Delay – Timing Violations
 - Appropriate Device Chosen