Software Quality Engineering:

Testing, Quality Assurance, and Quantifiable Improvement

Jeff Tian, tian@engr.smu.edu
www.engr.smu.edu/~tian/SQEbook

Chapter 9. Boundary Testing

- Input Domain Partitioning
- Simple Domain Analysis and Testing
- Important Boundary Testing Strategies
- Extensions and Perspectives

Non-Uniform Partition Testing

- Extensions to basic partition testing ideas: Non-uniform partitioned testing.
  - ▷ Testing based on related problems
  - ▷ Usage-related problems ⇒ UBST
  - ▷ Boundary problems ⇒ What to do?

- Usage-related problems:
  - ▷ More use ⇒ more likely failures
  - ▷ Usage information in testing
    ⇒ (Musa's) operational profiles (OPs)

- Boundary problems (This Chapter):
  ⇒ input domain boundary testing (BT).

Boundary Testing: Overview

- What is it?
  - ▷ Test I/O relations.
  - ▷ Classifying/partitioning of input space: – case-like processing model.
  - ▷ Cover input space and related boundary conditions.
  - ▷ Also called (input) domain testing.

- Characteristics and applications?
  - ▷ Functional/black-box view (I/O mapping for multiple sub-domains)
  - ▷ Well-defined input data: – numerical processing and decisions.
  - ▷ Implementation information may be used.
  - ▷ Focus: boundaries and related problems.
  - ▷ Output used only in result checking.

I/O Variables and Values

- Input:
  - ▷ Input variables: $x_1, x_2, \ldots, x_n$.
  - ▷ Input space: n-dimensional.
  - ▷ Input vector: $X = [x_1, x_2, \ldots, x_n]$.
  - ▷ Test point: X with specific x_i values.
  - ▷ Domains and sub-domains: specific types of processing are defined.
  - ▷ Focus on input domain partitions.

- Output (assumed, not the focus)
  - ▷ Output variables/vectors/space/range similarly defined.
  - ▷ Mapped from input by a function.
  - ▷ Output only used as oracle.

Domain Partitioning and Sub-domains

- Input domain partitioning
  - ▷ Divide into sets of sub-domains.
  - ▷ "domain", "sub-domain", and "region" often used interchangeably

- A sub-domain is typically defined by a set of conditions in the form of:

$$f(x_1, x_2, \ldots, x_n) < K$$

where "$<$" can also be substituted by "$>$", "$=$", "$\neq$", "$\leq$", or "$\geq$".

Domain Partitioning and Sub-domains

- Domain (sub-domain) boundaries:
  - ▷ Distinguishes/defines different sub-domains.
  - ▷ Each defined by it boundary condition, e.g., $f(x_1, x_2, \ldots, x_n) = K$
  - ▷ Adjacent domains: those share common boundary(ies)

- Boundary properties and related points:
  - ▷ Linear boundary:
    $$a_1x_1 + a_2x_2 + \ldots + a_nx_n = K$$
    (Otherwise, it is a nonlinear boundary.)
  - ▷ Boundary point: on the boundary.
  - ▷ Vertex point: 2+ boundaries intersect.
  - ▷ Other properties w.r.t. domains later.

Boundary and Domain Properties

- Boundary properties w.r.t domains:
  - ▷ Closed boundary: inclusive ($\leq$, $\geq$)
  - ▷ Open boundary: exclusive ($<$, $>$)

- Domain properties and related points:
  - ▷ Closed domain: all boundaries closed
  - ▷ Open domain: all boundaries open
  - ▷ Linear/nonlinear domain:
    all linear boundary conditions?
  - ▷ Interior point: in domain and not on boundary.
  - ▷ Exterior point: not in domain and not on boundary.

Input Domain Partition Testing

- General steps:
  - ▷ Identify input variable/vector/domain.
  - ▷ Partition the input domain into sub-domains.
  - ▷ Perform domain/sub-domain analysis.
  - ▷ Define test points based on the analysis.
  - ▷ Perform test and followup activities.

- Boundary testing: Above with focus on boundaries.

- Domain analysis:
  - ▷ Domain limits in each dimension.
  - ▷ Domain boundaries (more meaningful).
  - ▷ Closure consistency?
  - ▷ Plotting for 1D/2D, algebraic for 3D+.

Problems in Partitioning

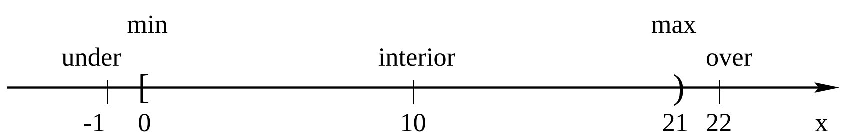
- Domain partitioning problems:
  - ▷ Ambiguity: under-defined/incomplete.
  - ▷ Contradictions: over-defined/overlap.
  - ▷ Most likely to happen at boundaries.
  - ▷ Key: sub-domains form a partition.

- Related boundary problems:
  - ▷ Closure problem.
  - ▷ Boundary shift: $f(x_1, x_2, \ldots, x_n) = K + \delta$
  - ▷ Boundary tilt: parameter change(s).
  - ▷ Missing boundary.
  - ▷ Extra boundary.

Simple Domain Analysis and EPC

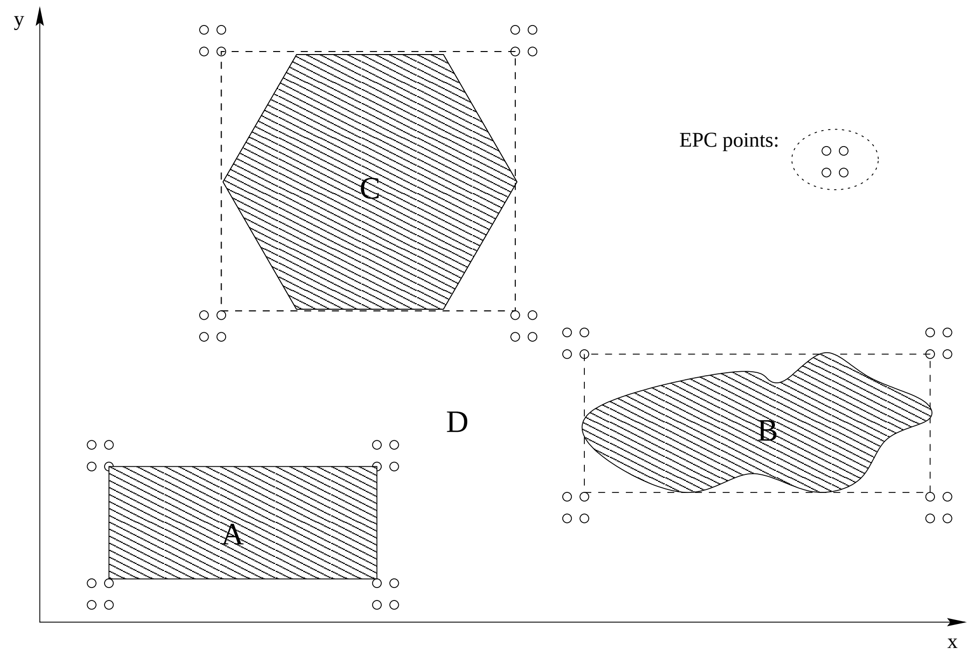
- Simple domain analysis:
  - ▷ identify domain limits in each dimension – min, max values
  - ▷ push "over" max, "under" min
  - ⇒ 4 values for each variable or dimension: under, min, max, over

- 1D example: Fig 9.1 (p.133)



- Extreme point combinations (EPC)
  - ▷ Combine above to derive test points.
  - ▷ Combine variables (×, cross-product).
  - ▷ # testcases: $4^n + 1$.

Simple Domain Analysis and EPC



- 2D examples: 9.2 (p.134)

- Problems/shortcomings with EPC:
  - ▷ Missing boundary points: 2D example. (unless boundaries perfectly aligned)
  - ▷ Exponential # testcases: $4^n + 1$.
  - ⇒ Need more effective strategies.

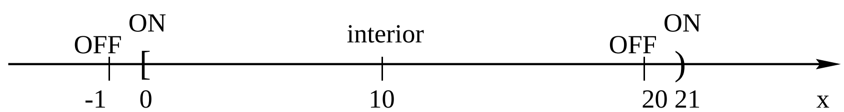
Boundary Testing Ideas

- Using points to detect boundary problems:
  - ▷ A set of points selected on or near a boundary: ON and OFF points.
  - ▷ Able to detect movement, tilt, etc.
  - ▷ Motivational examples for boundary shift.

- ϵ neighborhood and ON/OFF points
  - ▷ Region of radius ϵ around a point
  - ▷ Theoretical: could be infinitesimal
  - ▷ Practical: numerical precision
  - ▷ ON point: On the boundary
  - ▷ OFF point:
    - opposite to ON processing
    - off boundary, within ϵ distance
    - closed boundary, outside
    - open boundary, inside

Weak N x 1 Strategy

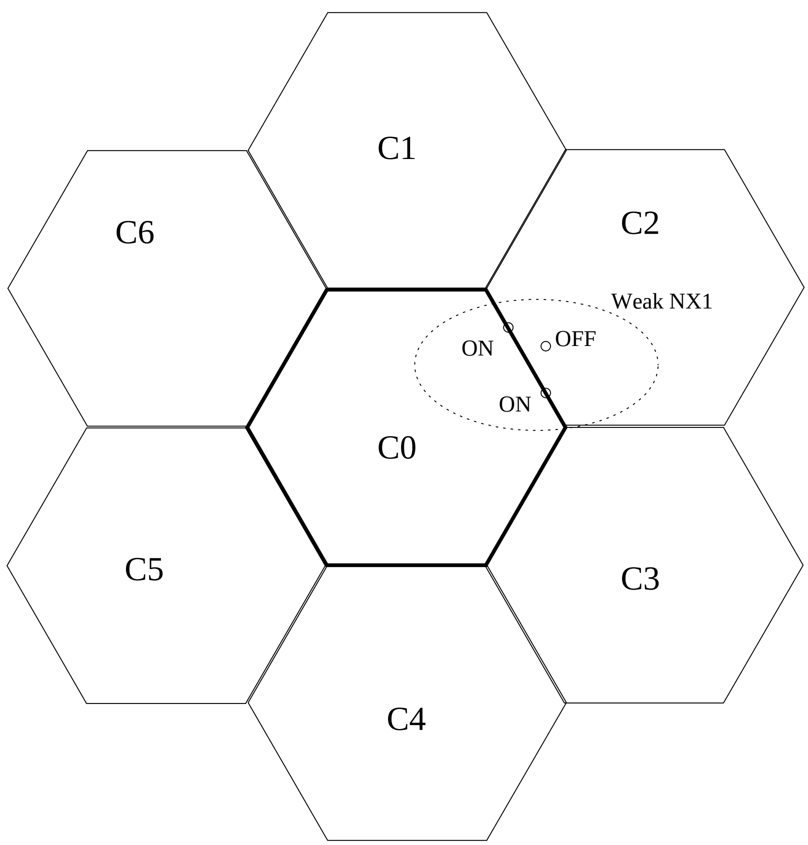
- N x 1 strategy (N-dimensional space)
  - ▷ N ON points (linearly independent): confirm (n-1)-D hyper-plane boundary.
  - ▷ 1 OFF point: centroid of ON points.
  - ▷ 1D: 1 ON, 1 OFF
  - ▷ 1D examples: Fig 9.3 (p.137)



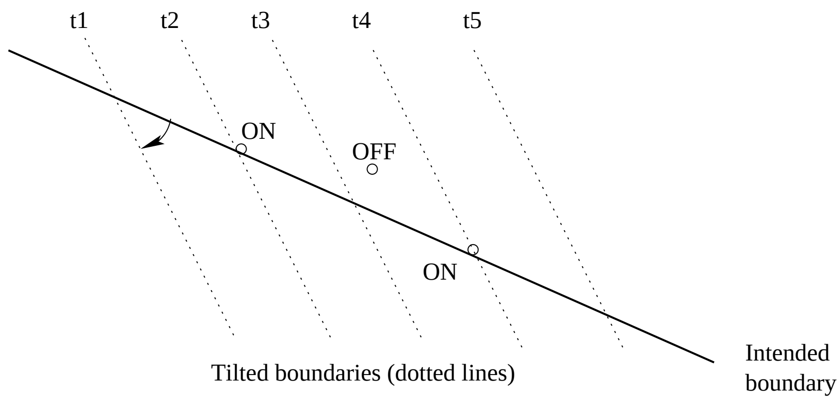
- Typical errors detected:
  - ▷ Closure bug
  - ▷ Boundary shift
  - ▷ Boundary tilt (later)
  - ▷ Extra boundary (sometimes)
  - ▷ Missing boundary

Weak N x 1 Strategy

- N x 1: N ON and 1 OFF points
  - ▷ Weak: set of tests per boundary instead of per boundary segment.
  - ▷ #test points: $(n+1) \times b + 1$
  - ▷ 2D example: Fig. 9.4 (p.137) below – advantages over EPC!



Weak N x 1 Strategy

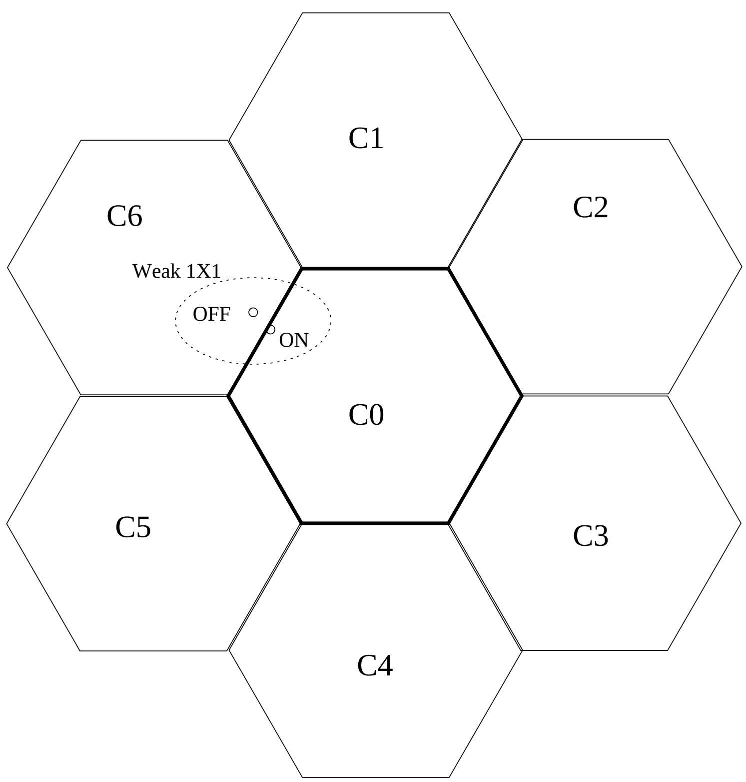


- Boundary tilt: Fig 9.5 (p.138) above
  - ▷ series of tilting points
  - ▷ some ON/OFF points combination will detect each tilt
  - ▷ (moving) illustration in class

- Other problems detected ≈ 1D example

Weak 1 x 1

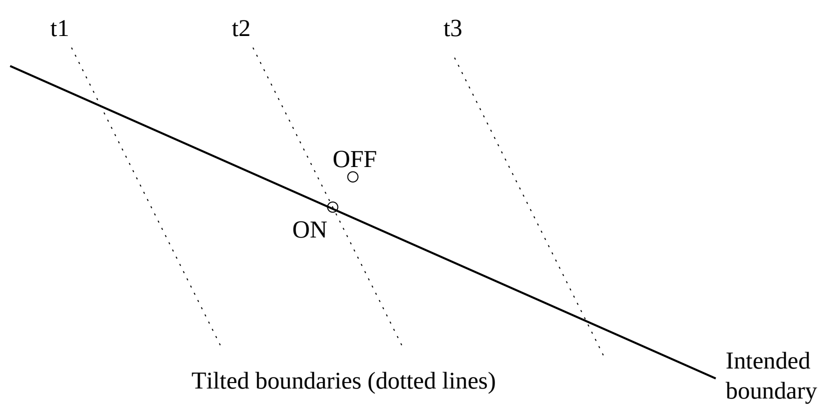
- Motivation: #test-points↓ without losing much of the problem detection capability.
  - ▷ boundary defined by 1 ON 1 OFF (n ON points in weak $N \times 1$ form an equivalent class ⇒ sampling 1)
  - ▷ 2D example: Fig 9.6 (p.139) below.



Weak 1 x 1

- Typical errors detected:
  - ▷ Closure bug
  - ▷ Boundary shift
  - ▷ Boundary tilt (not always!)
  - ▷ Missing boundary
  - ▷ Extra boundary (sometimes)

- Tilting in Fig 9.7, p.140, below (miss tilting at ON point, vs Weak N×1)



Other BT Strategies

- Strong vs. weak testing strategies:
  - ▷ Weak: 1 set of tests for each boundary
  - ▷ Strong: 1 set of tests for each segment

- Why use strong BT strategies?
  - ▷ Gap in boundary condition
  - ▷ Closure change
  - ▷ Coincidental correctness: particularly stepwise implementation
  - ▷ Code clues: complex, convoluted
  - ▷ Use in safety-critical applications

- Nonlinear boundaries: Approximate (e.g., piecewise) strategies often useful.

BT Extensions

- Direct extensions
  - ▷ Data structure boundaries.
  - ▷ Capacity testing.
  - ▷ Loop boundaries (Ch.11).
- Other extensions
  - ▷ Vertex testing:
    - – problem with boundary combinations
    - – follow after boundary test (1X1 etc.)
    - – test effective concerns
  - ▷ Output domain in special cases
    - – similar to backward chaining
    - – safety analysis, etc.
- Queuing testing example below.

BT and Queuing

- Queuing description: priority, buffer, etc.

- Priority: time vs. other:
  - ▷ time: FIFO/FCFS, LIFO/stack, etc.
  - ▷ other/explicit: SJF, priority#, etc.
  - ▷ purely random: rare

- Buffer: bounded or unbounded?

- Other information:
  - ▷ Pre-emption allowed?
  - ▷ Mixture/combination of queues
  - ▷ Batch and synchronization

Testing a Single Queue

- Test case design/selection:
  - ▷ Conformance to queuing priority.
  - ▷ Boundary test
  - ▷ Test cases: input + expected output.
  - ▷ Combined cases of the above.

- Testing specific boundary conditions:
  - ▷ lower bound: 0, 1, 2 (always)
  - ▷ server busy/idle at lower bound
  - ▷ upper bounds: B, B $\pm$ 1 (bounded Q) for bounded queue with bound B

- Other test cases:
  - ▷ Typical case: usage-based testing idea.
  - ▷ Q unbounded: some capacity testing.

BT Limitations

- Simple processing/defect models:
  - ▷ Processing: case-like, general enough?
  - ▷ Specification: ambiguous/contradictory.
  - ▷ Boundary: likely defect.
  - ▷ Vertex: ad hoc logic.

- Limitations
  - ▷ Processing model: no loops.
  - ▷ Coincidental correctness: common.
  - ▷ ϵ-limits, particularly problematic for multi-platform products.
  - ▷ OFF point selection for closed domain
    – possible undefined territory,
    – may cause crash or similar problems.
  - ▷ Detailed analysis required.